

MANUAL

ANT 2023: A Program for Adiabatic and Nonadiabatic Trajectories

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Abstract

ANT ("Adiabatic and Nonadiabatic Trajectories") is a Fortran 90 trajectory program designed primarily for classical, quasiclassical, and semiclassical calculations of the dynamics of atoms, molecules, and clusters in the gas phase.

ANT is especially recommended for calculations that employ analytic potential energy surfaces. It also has direct dynamics capability although it is not the most convenient code for direct dynamics.

- *ANT* can be used for dynamics governed either by a single potential energy surface (electronically adiabatic processes) or by two or more coupled potential energy surfaces (electronically nonadiabatic processes).
- For an electronically adiabatic process, the user must supply a potential energy surface and its gradients. The dynamics routines obtain this either from a user-supplied analytic potential energy surface subroutine or by direct dynamics. In direct dynamics, the is obtained by performing new electronic structure calculations whenever the dynamics algorithm needs potential information.

For an electronically nonadiabatic process the user must supply two or more surfaces and their gradients. For most of the nonadiabatic dynamics algorithms (all those except the ones labelled curvature-driven), couplings between electronic states are also required. When using an analytic potential surface this can be provided in the diabatic or adiabatic representation. When using direct dynamics, either representation may be used (although most electronic structure packages will only provide information in adiabatic representations). To use the electronically adiabatic representation for electronically nonadiabatic dynamics, the user may either provide the adiabatic surfaces and nonadiabatic couplings by direct dynamics, or the program may calculate them from diabatic surfaces and diabatic couplings, which are usually analytic. One can also use analytic fits to the surfaces and couplings to carry out calculations entirely in the diabatic representation.

For direct dynamics, the code has well tested interfaces to the *Gaussian 09*, *Gaussian 16*, *MOPAC-mn*, and *Molpro* electronic structure codes. The interfaces are included, but these electronic structure programs must be obtained separately. Users may also provide their own interfaces to other electronic structure programs.

- For electronically adiabatic processes, the code can perform either classical or quasiclassical trajectories.

For electronically nonadiabatic processes, the following semiclassical trajectory options are available:

- surface hopping by with Tully's fewest-switches (TFS) algorithm,
- surface hopping by the fewest switches with time uncertainty (FSTU) algorithm,
- FSTU with stochastic decoherence (FSTU/SD),
- mean-field methods (also called self-consistent-potential methods):

- the semiclassical Ehrenfest (SE) method,
 - coherent switching with decay of mixing (CSDM),
 - curvature-driven coherent switching with decay of mixing (κ CSDM)
 - self-consistent decay-of-mixing algorithm (SCDM)
- *ANT* can calculate
 - bimolecular reactive collisions
 - inelastic collisions
 - unimolecular processes

with various initial conditions. It can calculate cross sections and rate constants.

ANT can be run at fixed energy with various initial conditions or for thermal ensembles.

Another option is that one may begin trajectories at a dividing surface passing through a saddle point as used for unified dynamical model calculations.

An especially well developed feature of the program is initial state preparation for quasiclassical atom–diatom and diatom–diatom collisions.

A limited set of final-state analysis options is available. Or one can let program write initial and final coordinates and momenta and selected other information to a file for external (post-trajectory) analysis.

- Quantum mechanical enhancements:
 - The army ants tunneling algorithm is implemented as an option for both electronically adiabatic and electronically nonadiabatic trajectories on any unimolecular process. For electronically adiabatic processes, it may be used with classical or quasiclassical trajectories. For electronically nonadiabatic processes, it is only implemented for mean-field methods. The tunneling path can be any valence internal coordinate or any combination of two stretch coordinates.
 - Three methods (TRAPZ, mTRAPZ, and mTRAPZ* methods) are available to ensure zero-point energy maintenance in classical trajectory simulations, if desired.
- Additional capabilities:
 - The program can handle periodic boundary conditions (cubic or cuboid only) if a periodic potential is given.
 - The program can also optimize geometry by following a steepest-descent trajectory in Cartesian coordinates.

General notes about this manual

Keywords are usually in SMALL CAPS. Subroutine names are in normal caps.

Keywords in input sections are listed in alphabetical order.

The sections about initial conditions in this manual are organized for bimolecular collisions and unimolecular processes separately, and issues affecting both are repeated so users need refer to only one or another of them for their purposes. The test runs are also sorted into a section for unimolecular processes and another section for bimolecular processes.

It is useful to clarify a few points of notation and procedure that apply to all cases where coupled potential energy surfaces are used. There are two possible representations that may be used for coupled-surface processes: the electronically adiabatic representation and the electronically diabatic representation. When one uses the electronically adiabatic representation, one requires the adiabatic potential energy surfaces and their couplings. In the electronically adiabatic representation, the couplings are vectors ($3N_{\text{atom}}$ -dimensional vectors in atomic Cartesian coordinates, where N_{atom} is the number of atoms), and they are called the nonadiabatic couplings (NACs) or nonadiabatic coupling vectors. When one uses the electronically diabatic representation, one requires the diabatic potential energy surfaces and their couplings. Taken together, the diabatic surfaces and couplings constitute the diabatic potential energy matrix (DPEM). The elements of the DPEM are scalars. The diagonal elements of the DPEM are the diabatic potential energy surfaces, and the off-diagonal elements are called the diabatic couplings.

In the present version of the code, coupled-surface dynamics can be carried out by either direct dynamics or by using potential energy surface routines provided by the user. Section III of the manual discusses how one uses either

potential energy surface routines or surfaces-and-couplings routines provided by the user
or
direct dynamics information
for either single-surface or coupled-surface calculations.

Note that potential energy surfaces may also be called electronic energies. We use the usual convention that when we say electronic energies, it also includes nuclear repulsion.

We often use the word "polyatomic" to refer to a molecule with three or more atoms.

References cited in the manual are in Section XV.

The recommended citation for publications using *ANT 2023* is

Y. Shu, L. Zhang, J. Zheng, Z.-H. Li, A. W. Jasper, D. A. Bonhommeau, R. Valero, R. Meana-Pañeda, S. L. Mielke, and D. G. Truhlar, *ANT 2023*, University of Minnesota, Minneapolis, 2023. DOI:[here put zenodo DOI]

I. Code summary

ANT is a computer program written in Fortran 90 for calculating electronically adiabatic and electronically nonadiabatic trajectories by classical and semiclassical methods. The program can simulate unimolecular reactions, bimolecular nonreactive collisions, and bimolecular reactive collisions, and it can calculate inelastic or reactive collision cross sections and bimolecular or unimolecular reaction rate constants. All simulated processes are assumed to be gas-phase processes except in a few places where periodic boundary conditions are discussed.

Knowledge of the keywords is essential for proper use of the *ANT* input files. At the beginning of most of the sections of this manual we present the list of input keywords that will be explained in that section.

The code is designed to be as modular as possible.

Potential energy surfaces for electronically adiabatic processes can be calculated either from an analytic function (subroutine) or by direct dynamics (the latter option is sometimes called “on-the-fly” and it refers to requesting energies and gradients as needed from a quantum chemistry electronic structure program). Electronically nonadiabatic processes may be treated using either the adiabatic representation or a diabatic representation, and the potential surfaces and couplings may be obtained from analytic fits in a user-supplied subroutine or by direct dynamics, which involves requesting energies, gradients, and coupling as needed from a quantum chemistry electronic structure program. In the present version of *ANT*, direct dynamics simulations are accomplished by an interface with one of following quantum chemistry packages: *Gaussian 09*, *Gaussian 16*, *Molpro*, or *MOPAC-mn*. The integration with *Gaussian 09*, *Gaussian 16*, and *Molpro* is loose, i.e., an external script is used to run the quantum chemistry package; the integration with *MOPAC-mn* is tight, i.e., *MOPAC-mn* subroutines are directly called from *ANT* code. The main reason for using a semiempirical program like *MOPAC-mn* is to reduce computer time (as compared to using nonempirical wave function calculations or using density functional calculations), but much of the possible computational efficiency would be lost if one used a loose interface.

For runs based on an analytic potential function, the user provides a potential energy subroutine that returns the electronic energy (or energies and couplings in the case of electronically nonadiabatic processes) and gradients when a nuclear geometry is passed to it. A selection of potential energy subroutines is available at POTLIB-online (<http://comp.chem.umn.edu/potlib>). *ANT* supports several potential energy subroutine interfaces. These are described in Section III and in the appendix (Section A.3).

As part of setting up the simulation of a particular process, the user specifies one atom group (AG) for unimolecular processes and two AGs for bimolecular processes. Each AG is treated as an isolated group of atoms, and initial conditions for each AG are prepared by *ANT* before integrating the equations of motion. For bimolecular processes, before integrating the equations of motion, one must also set up the initial collision parameters. In this context, collision parameters are parameters that control the relative location and relative motion of the two collision partners; this includes impact parameter and molecular and rotational orientation) Different AGs may be prepared using different initial condition prescriptions, and several initial

condition prescriptions are supported. The program can handle periodic boundary conditions if a periodic potential is given. See Section IV for details of setting initial conditions.

Collision processes between an atom and a diatom can be carried out by special algorithms for the initial conditions, as described in Ref. 15. Both atom–diatom calculations and more general bimolecular calculations (atom–polyatom and molecule–molecule collisions) may be treated using a general method that is applicable to any type of bimolecular system. The general method treats the reactants and products by the harmonic oscillator, rigid rotor approximation, whereas the special atom–diatom option can use more accurate methods.

Three kinds of thermostat and one kind of barostat are available for simulations of NVT (canonical) or NPT (isothermal-isobaric) ensembles. See Section IV and the appendix for details.

The classical equations of motion are integrated in Hamiltonian form. Variable and fixed-step-size integration options are available. See Section V for details.

Nuclear propagation may be carried out electronically adiabatically (i.e., on a single potential energy surface) or electronically nonadiabatically if excited-state surfaces and their couplings are available. Several options exist for incorporating electronic transitions into trajectory simulations including the semiclassical Ehrenfest method, several surface hopping methods, and several decay of mixing methods, including the recommended CSDM method. See Section VI for details.

The methods for preparing initial reaction conditions are explained in Section IV.

The TRAPZ (TRAjectory Projection onto ZPE orbit), mTRAPZ (minimal TRAPZ), and mTRAPZ* methods that constrain the trajectory to maintain the total zero-point energy of a molecule in classical or semiclassical trajectories have been implemented. See Section VII for details.

The army ants tunneling algorithm is implemented for both electronically adiabatic and electronically nonadiabatic trajectories of unimolecular reactions. The tunneling path can be either a single valence internal coordinates or a combination of two stretch coordinates. See Section IX for details.

A limited number of special options are available. For example, the momenta may be zeroed at every step, resulting in a steepest-descent trajectory. As another example, the nuclear kinetic energy may be rescaled at regular intervals to simulate heating or cooling. See Section IX.A for details.

Another option is that one may begin trajectories at a dividing surface passing through the saddle point. See Section X.B for details.

Trajectories are propagated until a termination condition is met. Several options for termination are available, including running trajectories for a fixed time, monitoring bond-breaking events, or monitoring AG fragmentation and association (the latter was found to be very useful for reactions between metal clusters. See the input file section, Section XII for details.

A limited set of final-state analysis options is available. See Section X for details.

Propagation of nuclear coordinates can be carried out electronically adiabatically, i.e., on a single potential energy surface, or electronically nonadiabatically, i.e., on coupled surfaces; the latter requires that two or more potential energy surfaces and their couplings be available. Electronically nonadiabatic calculations are also called non-Born-Oppenheimer calculations, multi-surface calculations, or coupled-surface calculations; these calculations involve transitions between surfaces, either as discontinuous hops or by continuous switching. Several options exist for incorporating electronic transitions into the trajectory simulations, including the semiclassical Ehrenfest method (coherent switches without decoherence), several surface hopping methods (with or without time-uncertainty and with or without stochastic decoherence), and several decay of mixing methods, including the recommended coherent switching with decay of mixing (CSDM) method. See Section VI for details.

When one uses the electronically adiabatic representation, the user may either provide the adiabatic surfaces and nonadiabatic couplings as such, or the program may calculate them from the diabatic surfaces and diabatic couplings.

II. Recommended citation

All published work based on the *ANT* program should give the *ANT* reference. The recommended citation for the current *ANT* package is:

Y. Shu, L. Zhang, J. Zheng, Z.-H. Li, A. W. Jasper, D. A. Bonhommeau, R. Valero, R. Meana-Pañeda, S. L. Mielke, and D. G. Truhlar, *ANT* 2023, University of Minnesota, Minneapolis, 2023. DOI:[here put zenodo DOI]

III. Potential energy surfaces and surface couplings

Input keywords presented in this section: POTFLAG.

III.A. Sample potential energy subroutines

To perform any dynamics simulation, *ANT* either needs a potential energy subroutine, or it needs a quantum chemistry package for direct dynamics. The subroutine GETPEM (src/getpem.f) collects all potential energy subroutine calls including direct dynamics.

The *ANT* distribution contains sample potential energy subroutines for several systems; these are provided in the directory pot/. The user can also pick up other potential energy subroutines at POTLIB-online:

<http://comp.chem.umn.edu/potlib/>

Any additional potential energy subroutines provided by the user should be moved into the directory pot/, and the coordinates, energies, and gradients for input and output to such routines should be in atomic units (hartrees and bohrs).

Note that each run calls the subroutine PREPOT once. This call can be used to set up quantities that need to be initialized for subsequent potential calls. The user must supply a dummy routine if this call is not needed. The PREPOT subroutine should be included in the same file as the potential energy subroutine (so it is recognized by the compiler).

III.B. Standardized calling protocol

Calculations in *ANT* are carried out using unscaled Cartesian coordinates (without removing overall translation), but it is often convenient to use other sets of coordinates when expressing the potential energy. An interface between the two coordinate systems (Cartesians and the one used for the potential) is therefore required. A series of potential energy subroutine interfaces are provided to handle the coordinate transformations (and those for the derivatives) for several system types. In addition to handling coordinate transformations, these interfaces also handle potential energy surface conventions such as the specific ordering of atoms, etc.

For electronically nonadiabatic dynamics, potential energy surface subroutines provide the energies and gradients in the adiabatic representation, in the diabatic representation, or in both representations. One available option, if needed, is that the nonadiabatic couplings (see page 6 for definitions) can be calculated from the diabatic surfaces and diabatic couplings by subroutines provided as part of the *ANT* program.

The user selects the interface to be used with the input variable POTFLAG. The following interfaces are currently supported:

POTFLAG=0: HO-MM-1 interface.

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This is a single-surface (adiabatic), homonuclear, molecular mechanics (i.e., variable number of atoms) interface. Subroutine calls with this interface have the general form:

POT(X, Y, Z, E, DEDX, DEDY, DEDZ, NATOM, MAXATOM)

for a non-periodic potential and

POT(X, Y, Z, E, DEDX, DEDY, DEDZ, CELL, NATOM, MAXATOM)

for a periodic potential. The user can prepare his or her own periodic boundary conditions in the potential routine, or call

SUBROUTINE PERIODIMAGE(DX,DY,DZ,CELL)

before calculating distances. This subroutine returns the new DX, DY, and DZ (the differences in Cartesian coordinates between the two atoms whose distance will be calculated.). Currently, the subroutine can only deal with cubic or cuboid cells. The meanings of the parameters are as follows:

NATOM (input, integer) The number of atoms.

MAXATOM (input, integer) Sets the dimensions of the variables X, Y, Z, DEDX, DEDY, and DEDZ. Must be greater than or equal to NATOM.

X, Y, Z (input, double precision) One-dimensional arrays containing the Cartesian components of NATOM atoms.

E (output, double precision) The potential energy.

DEDX, DEDY, DEDZ (output, double precision) One-dimensional arrays containing the first derivatives of the energy with respect to the Cartesian coordinates.

CELL(6): The six cell parameters a , b , c , α , β , and γ .

POTFLAG=1: 3-2V interface.

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This interface returns a 2 x 2 diabatic potential energy surface matrix for a triatomic system. PREPOT is called once, and POT is called when an energy and/or gradient is needed. Subroutine calls with this interface have the general form:

CALL POT(R, E, DE, NVALS, NSURF)

The meanings of the parameters are as follows:

NVALS (input, integer) The energy and derivatives are computed for NVALS different geometries.

NSURF (input, integer) Labels the potential energy surface. For a single-surface potential, NSURF = 1. For a two-state potential, NSURF = 1 and 3 for the two diagonal diabatic potential energy surfaces, and NSURF = 2 for the diabatic coupling surface.

R (input, double precision) A two-dimensional array containing the internuclear bond distances. The first index labels the NVALS different geometries, and the second index labels the three internuclear distances.

E (output, double precision) An array containing the potential energies of surface NSURF at NVALS geometries.

DE (output, double precision) A two-dimensional array of the first derivatives of surface NSURF with respect to the three internuclear distances. The first index labels the three internuclear distances, and the second index labels the NVALS different geometries.

POTFLAG=2: HE-MM-1 interface.

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This is a single-surface (adiabatic), heteronuclear, molecular mechanics (i.e., variable number of atoms) interface. Subroutine calls with this interface have the general form:

```
CALL POT(SYMB, X, Y, Z, E, DEDX, DEDY, DEDZ, NATOM, MAXATOM)
```

for a non-periodic potential and

```
CALL POT(SYMB, X, Y, Z, E, DEDX, DEDY, DEDZ, CELL, NATOM, MAXATOM)
```

for a periodic potential.

The arguments are the same as for POTFLAG=0, except for SYMB (input, character*2) One-dimensional array containing the atomic symbols of all the atoms.

POTFLAG=3: NH₃ potential interface.

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This is a two-surface (adiabatic and diabatic), heteronuclear, 4-body interaction interface. Subroutine calls with this interface have the general form:

```
call pot(Xcart,U11,U22,U12,V1,V2,gcartU11,gcartU22,gcartU12,gcartV1,gcartV2)
```

Xcart: A one dimensional array of coordinate in an order of x1, y1, z1, x2, y2, z2, x3, y3, z3, x4, y4, z4.

U11, U22, U12: Ground state energy, excited state energy, and the cross-term of the two states in a diabatic representation.

V1, V2: Ground state energy, and excited state energy in an adiabatic representation.

Gcart-terms: The one dimensional derivatives of the corresponding energies.

POTFLAG=4: 4-XS interface

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This is a single-surface (adiabatic), heteronuclear, 4-body interaction interface. Subroutine calls with this interface have the general form:

```
CALL POT(X, Y, Z, E, DEDX, DEDY, DEDZ)
```

In this potential, there is a special ordering of atoms, for example for the OH+H₂ potential, the ordering is O, H, H, H, i.e. oxygen atom must be the first atom. In a reactive collision run, the current program can deal with reactants OH+H₂ and OH₃+H, but not O+H₃, which seems not a possible combination of reactants.

POTFLAG=5: Same as HE-MM-1 interface, but transfers atomic numbers instead of atomic symbols, i.e. SYMB is replaced with INDATOM, which is a one-dimensional array containing the atomic numbers of all the atoms.

POTFLAG=6: HBr potential interface.

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This is a twelve-surface (adiabatic and diabatic), heteronuclear, 2-body interaction interface. Subroutine calls with this interface have the general form:

```
call pot(Xcart,UI,UIJ,VI, gUI,gUIJ,gVI,dvec)
```

where the items in the parameter list have the following meanings:

Xcart: A one dimensional array of coordinates in the order x1, y1, z1, x2, y2, z2, where atom 1 is H and atom 2 is Br.

UI: Array with the energies of the 12 diabatic states. The diagonal elements of this matrix are zero.

UIJ: 12×12 matrix with the diabatic couplings.

VI: Array with the energies of the 12 adiabatic states.

gUI: Array with the nuclear derivatives of the 12 diabatic energies.

gUIJ: 12×12 matrix with the nuclear derivatives of the diabatic couplings. The diagonal elements of this matrix are zero.

gVI: Array with the nuclear derivatives of the 12 adiabatic energies.

dvec: nonadiabatic coupling vector.

POTFLAG=7: BrCH₂Cl potential interface.

This interface is described at POTLIB-online, <http://t1.chem.umn.edu/potlib>. This is a twenty-four-surface (adiabatic and diabatic, where the adiabatic surfaces are optionally calculated by diagonalizing the diabatic potential matrix), heteronuclear, 5-body interaction interface. Subroutine calls with this interface have the general form:

```
call pot(Xcart7,UI,UIJ,VI, gUI,gUIJ,gVI,dvec,icall)
```

where the items in the parameter list have the following meanings:

Xcart7: A one dimensional array of coordinates in the order x1, y1, z1, x2, y2, z2, x3, y3, z3, x4, y4, z4, x5, y5, z5, where atom 1 is Br, atom 2 is C, atom 3 is Cl, atom 4 is H1, and atom 5 is H2.

UI: Array with the energies of the 24 diabatic states.

UIJ: 24×24 matrix with the diabatic couplings.

VI: Array with the energies of the 24 adiabatic states.

gUI: Array with the nuclear derivatives of the 24 diabatic energies.

gUIJ: 24×24 matrix with the nuclear derivatives of the diabatic couplings.

gVI: Array with the nuclear derivatives of the 24 adiabatic energies.

dvec: nonadiabatic coupling vector.

icall: variable that controls the calculation of adiabatic energies (only with icall = 1 will they be calculated).

POTFLAG=8: This is a standard interface for a single adiabatic surface. Current examples among the distributed potentials include HN2.f, N2O-3Ap-gpip.f, and N2O-3App-gpip.f.

The potential can be called as follows

```
Call pot(V, X, GRAD)
```

where the items in the parameter list have the following meanings:

V: Potential energy in hartrees.

X: A one-dimensional array of Cartesian coordinates in the order of x1, y1, z1, x2, y2, z2, x3, y3, etc.. The units are bohr.

GRAD: A one-dimensional array of gradients. Its order is the same as the Cartesian coordinate array X.

For any new routines, the user should also provide a print statement in the prepot routine that prints an identification line for the potential and any references that should appear in the main output file.

POTFLAG=9: HX₂ potential interface.

This is a two surfaces interface for the model system HX₂, where H and X are model atoms.

The potential can be called as follow

```
Call pot(Xnat,UIJnat,VInat,gUIJnat,gVInat,dvecnat,cchx2)
```

Xnat : a one-dimensional array of Cartesian coordinates in the order of x1, y1, z1, x2, y2, z2, x3, y3, where atom 1 is H, atom 2 and 3 are X. Unit is bohr.

UIJnat: 2×2 matrix with the diabatic energies and couplings.

VInat: array with the adiabatic energy in ascending order.

gUIJnat: 2×2 matrix of the nuclear derivatives with respect to the diabatic energies and couplings.

gVInat: array of the nuclear derivative with respect to the adiabatic energies

dvecnat: nonadiabatic coupling vector

cchx2: matrix that transform diabatic energies to adiabatic energies.

POTFLAG=10: phenol potential interface.

This is coupled 33-dimensional potential energy surfaces for electronically nonadiabatic photodissociation of phenol to make phenoxy radical and a hydrogen atom.. This potential energy surface is described in K. R. Yang, X. Xu, J. Zheng, and D. G. Truhlar, Chemical Science 2014, in press. [dx.doi.org/10.1039/c4sc01967a](https://doi.org/10.1039/c4sc01967a). The potential can be called as

```
call pot(igrad,x,uu,guu,vv,gvv,dvec,ccph,repflag)
```

igrad: integer to control calculation for energy only (igrad=0) or for energy and gradients (igrad=1)

x: a two-dimension array of Cartesian coordinates, i.e. x(3, 13). The first dimension denotes x, y, and z, and the second dimension denotes the atom number. The numbering of atoms is C1, C2, C3, C4, C5, C6, O7, H8, H9, H10, H11, H12, H13

uu: 3×3 matrix with the diabatic energies and couplings

guu: a four dimensional array defined as guu(3,13,3,3) for the nuclear derivatives with respect to the diabatic energies and couplings. The first dimension denotes the x, y, and z components; the second dimension denotes the atom number; the third and the fourth dimension denote the diabatic state.

vv: a one dimensional array for adiabatic energies in ascending order

gvv: a three dimensional array defined as `gvv(3,13,3)` for the nuclear derivatives with respect to the adiabatic energies. The first dimension denotes the x , y , and z components; the second dimension denotes the atom number; the third denotes the adiabatic state.

dvec: nonadiabatic coupling vector

ccph: matrix that transform diabatic energies to adiabatic energies.

repflag: integer that denotes representation: `repflag = 0` for adiabatic state and `repflag = 1` for diabatic state.

III.C. Diatomic potential

The polyatomic potential energy surface subroutines could include specific subroutines to compute the potential of diatoms that are needed to calculate the initial conditions of atom–diatom and diatom–diatom calculations.

To use this option, a subroutine call `diapot_int` should be included in the source code previous to compiling the code. It is recommended to include these subroutines in the corresponding PES file located in the `pot` directory. An example of the `diapot_int` subroutine is the following:

```

subroutine diapot_int(r,arr,nsurf,v)
  implicit none
  integer arr,nsurf
  double precision r,v
C Diatomic arrangement:
C 1 AB
C 2 BC
C 3 AC
C 4 AD
C 5 BD
C 6 CD
  if (arr.eq.1) then
    call evfarr1(r,v,nsurf)
  else if (arr.eq.2) then
    call evfarr2(r,v,nsurf)
  else if (arr.eq.3) then
    call evfarr3(r,v,nsurf)
  else if (arr.eq.4) then
    call evfarr4(r,v,nsurf)
  else if (arr.eq.5) then
    call evfarr5(r,v,nsurf)
  else if (arr.eq.6) then
    call evfarr6(r,v,nsurf)
  else
    write(6,*) 'ERROR in diapot_int: arr = ',arr,' is not supported'
    stop
  endif
end subroutine diapot_int

```

where r is the interatomic distance in bohr, arr defines the diatomic arrangement, v is the diatomic potential in hartrees, and $nsurf$ is the number of the adiabatic potential energy surface.

The user must comment out the following lines in the `diapot.f90` file located in the `src` directory of the ANT code before compiling the code:

```
C  subroutine diapot_int(r,im,nsurf,v)
C  implicit none
C  double precision r,v
C  integer im,nsurf
C  return
C  end
```

The keyword `FLAGDIAT` has to be included in the `$ATOMDIATOM` input deck. Note that the current version of the code only uses this option for the atom–diatom method (see Section IV.C.3).

III.D. Direct Dynamics

POTFLAG=-1: direct dynamics using *Gaussian09* or *Molpro*

The subroutines in `pot/dd.f` provide a common interface for direct dynamics calls to *Gaussian 09*, *Gaussian 16*, or *Molpro*. The keyword `POTFLAG=-1` turns on the direct dynamics interface. The keyword `QCPACK` is to choose the quantum chemistry package; `QCPACK=1` is for *Gaussian 09* or *Gaussian 16* and `QCPACK=2` is for *Molpro*. The direct dynamics option for *Molpro* is not fully tested yet and should be considered to be code for developers only in the present release.

To run a direct dynamics calculation, one needs to give the following set of files in the working directory together along with the *ANT* input file.

File	Explanation
Direct dynamics with <i>Molpro</i>	
<code>m.x</code>	An executable file that contains commands to run a <i>Molpro</i> job
<code>qc.molpro</code>	A template file for <i>Molpro</i> input
Direct dynamics with <i>Gaussian 09</i> or <i>Gaussian 16</i>	
<code>g.x</code>	An executable file that contains commands to run a <i>Gaussian</i> job
<code>qc.gaussian</code>	A template file for <i>Gaussian 09</i> or <i>Gaussian 16</i> input

Examples:

`m.x` file: (with executable extension)

```
molpro -n 8 -o qc.out -s qc.in > system.out
```

g.x file: (with executable extension)

```
g09 < qc.in > qc.out
```

qc.molpro:

```
***,title
print,orbitals,civector
memory,200,m

nosym
noorient
geometry={
GEOMETRY
}

basis=svp
nn(1)=1
nn(2)=2
nn(3)=3

{rhf;wf,14,1,0}
{multi;occ,12;closed,3;wf,13,1,1;
state, 2
cpmcscf,grad,1.1,spin=0.5,accu=1.d-7,record=5101.1
cpmcscf,grad,2.1,spin=0.5,accu=1.d-7,record=5102.1
cpmcscf,nacm,1.1,2.1,accu=1.d-7,record=5103.1}
molpro_energy=energy(1)
{force
samc,5101.1;varsav}
text,MOLGRAD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
molpro_energy=energy(2)
{force
samc,5102.1;varsav}
text,MOLGRAD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
{force
samc,5103.1;varsav}
text,MOLD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
```

The *ANT* program will replace the GEOMETRY placeholder in the qc.molpro file with the proper Cartesian coordinates. This example is for running a nonadiabatic dynamics calculation with two surfaces. Note that the following lines in this example are essential for the ability of the *ANT* program to extract the energy, gradients, and nonadiabatic coupling from the tabulated values in the *Molpro* output file

```
molpro_energy=energy(1)
text,MOLGRAD
table,nn,gradx,grady,gradz
text,MOLD
table,nn,gradx,grady,gradz
```

It is important to include the keywords “nosym” and “noorient” in order to avoid *Molpro* reordering the atoms in the output file.

Additional explanations about using the *ANT-Molpro* direct dynamics interface:

(1) In the above example,

```
nn(1)=1
nn(2)=2
nn(3)=3
```

indicates that nn(1) is the first element of the molecule, and nn(2) and nn(3) are the second and third elements of the molecule. Therefore, the above example corresponds to a three-atom system. If more atoms are involved, this nn list should go up to the total number of the atoms in the molecule.

(2) In each of the MULTI cards, *Molpro* only allows at most five coupled perturbed MCSCF calculations (CPMCSCF). Therefore, if the system involves more than two electronic states, one would require at least six CPMSCF calculations. For example, when a system involves three electronic states, one would require calculations of three gradients, and three nonadiabatic coupling vectors (12, 13, and 23). In that situation, one should specify an additional MULTI card, with the identical specification of the wave functions, but with only 1 iteration (specified by keyword MAXITER,1). Following is an example of a MULTI card corresponding to ethylene nonadiabatic dynamics with SA-CASSCF (2 active electrons in 2 active orbitals) with 3 electronic states:

```
{multi
  occ,9
  closed,7
  state,3
  cpmcscf,grad,1.1,record=5100.1
  cpmcscf,grad,2.1,record=5101.1
  cpmcscf,grad,3.1,record=5102.1}
```

```
{multi
  occ,9
  closed,7
  state,3
  maxiter, 1
  cpmcscf,nacm,1.1,2.1,record=5103.1
  cpmcscf,nacm,1.1,3.1,record=5104.1
  cpmcscf,nacm,2.1,3.1,record=5105.1}
```

The complete ethylene example can be found in the test runs.

- (3) The interface program requires an ordered reading of energy and gradient for each state, followed by nonadiabatic coupling vectors. Therefore, even though all energies are computed after the MULTI card, one should not specify energies for all electronic states at once before reading of first state gradient. The following WRONG EXAMPLE shows that one first reads all electronic state energies and then read gradients. The CORRECT EXAMPLE shows that one read first state energy and first state gradient, followed by second state energy and second state gradient.

FOLLOWING IS A WRONG EXAMPLE:

```
molpro_energy=energy(1)
molpro_energy=energy(2)
```

```
{force
samc,5101.1;varsav}
text,MOLGRAD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
```

```
{force
samc,5102.1;varsav}
text,MOLGRAD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
```

THE CORRECT EXAMPLE IS:

```
molpro_energy=energy(1)
{force
samc,5101.1;varsav}
text,MOLGRAD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
```

```
molpro_energy=energy(2)
{force
samc,5102.1;varsav}
text,MOLGRAD
table,nn,gradx,grady,gradz
ftyp,f,d,d,d
```

The nonadiabatic couplings are written in the following ordering:

$\mathbf{d}_{1,2}, \mathbf{d}_{1,3}, \dots, \mathbf{d}_{1,N}, \mathbf{d}_{2,3}, \mathbf{d}_{2,4}, \dots, \mathbf{d}_{2,N}, \dots, \mathbf{d}_{N-1,N}$

where $\mathbf{d}_{I,J}$ is the nonadiabatic coupling vector between electronic states I and J .

qc.gaussian file

```
%nprocs=8
%mem=1000mb
#mp2/6-31g* force fchk NoSym Units=bohr scf=(tight,xqc)
```

Title

0 2 GEOMETRY

The *ANT* program will replace the GEOMETRY placeholder in the qc.gaussian file with the proper Cartesian coordinates. This example is for running electronically adiabatic dynamics with one surface. The *ANT* program reads the energy and gradient from the formatted checkpoint file Test.Fchk.

POTFLAG=-2: direct dynamics using *MOPAC-mn*

The subroutines in pot/potmopac.f provide an interface for direct dynamics to call *MOPAC-mn* subroutines directly for energy and gradient calculations instead of using a script to run external MOPAC calculations. By calling *MOPAC-mn* subroutines in the Fortran code directly, this interface reduces the overhead of running external jobs.

To run a direct dynamics calculation, a file named mopac.in is needed to provide all keywords used in MOPAC calculations. The file mopac.in is a MOPAC input file and the geometry in this file can be any reasonable geometry because this MOPAC input file is only run once to set up all variables used in the MOPAC calculation.

Note that direct dynamics with *MOPAC-mn* is currently only implemented for unimolecular reactions.

IV. Initial conditions

The user will first have to make some choices about the type of initial conditions; the first of these choices is to choose unimolecular processes or bimolecular processes. In the table below, the first run type is bimolecular, and the second run type is unimolecular. The table also lists three or four subtypes for each type, and user also has to choose one of these subtypes. Then the user will have to decide which particular initial conditions of a given type and subtype are to be used.

run type	subtype	description	Applicability
1		Unimolecular processes	
	1.1	State-selected initial conditions	single surface or multiple surfaces
	1.2	Vertical excitation	multiple surfaces
	1.3	Fixed energy initial conditions	single surface or multiple surfaces
	1.4	Fixed temperature initial conditions	single surface
2		Bimolecular collision	
	2.1	General bimolecular collision input	single surface or multiple surfaces
	2.2	Atom–diatom collision input	single surface or multiple surfaces
	2.3	Diatom–diatom collision input	single surface or multiple surfaces

In the above table, the two major types of initial conditions supported by the *ANT* program are bimolecular collisions and unimolecular processes. In this section, we will explain these two types and the related input keywords. Some examples are used to illustrate how to set up initial conditions for different modes.

In subsection A, we will give some general descriptions of initial rotational orientation, initial coordinates, and initial momenta of atom groups; this material applies to both modes, where the initial conditions for a bimolecular collision involve two atom groups, and the initial conditions for a unimolecular process involve one atom group. The descriptions for how to set up each individual mode are in the rest of the subsections.

For a bimolecular collision (run type 2), one needs to specify $\$NMOL = 2$, give two atom groups in the $\$DATA$ input deck, and give either the input deck $\$RXCOLLISION$ or the input deck $\$ATOMDIATOM$. For a unimolecular process (run type 1) one needs to specify $\$NMOL = 1$ and give only one atom group. The $\$RXCOLLISION$ and $\$ATOMDIATOM$ input decks are used only for bimolecular collisions.

The $\$TUNNELING$ input deck is only tested for unimolecular processes so far, and $\$CELL$ is for systems with periodic condition (which is a special case of unimolecular processes). The other input decks are generally applicable for any of the run types.

Note that subtype 2.1 can be used for atom–diatom and diatom–diatom collisions as well as for collisions of polyatomics.

IV.A. General description for preparing each Atom Group (AG)

Quantities required for computing the initial conditions that are the same for all trajectories are pre-computed by *ANT* by calling PREMOL. The specific initial conditions for each trajectory are determined by calling INITMOL. An atom group is defined as a collection of atoms; atom groups are used for initial state preparation. For example, each molecule in a bimolecular collision is an atom group and unimolecular processes have only one atom group.

INITX and INITP are keywords to control the method of providing initial geometry and to control how to select the method for generating initial momenta, respectively. When there is more than one atom group, the scheme used to prepare one AG need not be the same as that used to prepare the other. The input section (Section XII) gives the descriptions of INITX and INITP, but we also explain them in this section for reader's convenience. This subsection focuses on how to prepare the initial conditions for rotational orientation, rotational states (or energies), and vibrational states in general. Note that capitalized words are subroutine names.

IV.A.1. Rotational orientation

This subsection applies to all run types except subtypes 2.2 and 2.3.

After the initial coordinates are provided by the user or generated by random sphere, cuboid, or other methods.

1. The AG is rotated to its own coordinate system of principal axes of rotation by first calling ROTPRIN (to calculate the principal axes of rotation) and then a rotation transformation by calling ROTTRAN using the vectors of the principal axes of rotation as rotation transformation matrix.
2. A random orientation represented by a rotation transformation matrix is generated by calling RANROT. For general reactive collisions, the transformation matrix is generated by randomly changing the 3 Euler angles directly, while for other cases it is generated using a quaternion method (see <http://mathworld.wolfram.com/EulerParameters.html>, and Ref. 1 of Section XV).
3. The AG is rotated to this new orientation generated in step 2 by calling ROTTRAN, and the momenta of the atoms in this AG are subsequently transformed to the new orientation by calling ROTTRAN.

IV.A.2. Initial conditions on momenta

There are three options for generating the initial momenta of an AG, as determined by the value of the input parameter INITP.

INITP=0: Zero initial momentum

The initial momenta are set to zero.

INITP=1: Random thermal distribution

1. The user supplies a target temperature T [TEMP0IM] in Kelvin. Steps 2 and 3 are performed in RANTHERM subroutine.

2. $3N_{\text{atom}}$ random numbers (ξ_{ij}) are selected from a normalized Gaussian distribution.
3. The momentum is assigned according to

$$P_{ij} = \xi_{ij} \sqrt{k_b T M_j} \quad [\text{PP}]$$

where M_j is the mass of atom j .

INITP=-1: Initial momentum is decided by other choices, such as VIBSELECT, ROTSTATES. See Section XII for details.

IV.A.3. Rotational states

At present, state selection on rotational states can only be done for linear AGs. This is done after the AG is rotated to its own principal axes of rotation and its overall momentum of rotation is removed. The aim of the procedure consists in adding rotational components_⊥ to momenta p_i . These components are estimated by randomly generating rotational states with an energy E_{rot} . The relationship between E_{rot} and the angular momentum J then enables to determine $p_{i\perp}$. The whole procedure is described in Appendix A1.

IV.A.4. Vibrational states

In the case of the simulations for which the user desires a normal mode analysis to provide initial conditions, if vibrational quantum states or vibrational energies are not provided, the program will randomly generate a set of vibrational quantum numbers according to Boltzmann distribution (The structures provided must be local minima.). The whole procedure is described in Appendix A1.

IV.A.5. Removal of overall angular momentum

After the coordinates and momenta are assigned for each AG, the center of mass is placed at the origin, and center of mass motion is removed. Angular motion is (approximately) removed by first computing angular velocity $\boldsymbol{\omega}$

$$\boldsymbol{\omega} = \mathbf{I}^{-1} \mathbf{J},$$

where \mathbf{I} is the inertial tensor matrix, and \mathbf{J} is the total angular momentum.

The momentum for atom j and direction i ($i = x, y, \text{ or } z$) is adjusted according to

$$P_{ij} = P_{ij} - M_j [\boldsymbol{\omega} \times \mathbf{x}_i]_j.$$

Note: 1) For non-symmetric structures, this scheme only approximately removes angular motion. In the current program, this procedure is repeated until the total angular motion falls below a hard-coded small value. 2) For linear AGs, this procedure cannot be used because \mathbf{I}^{-1} cannot be calculated for linear AGs since the determinant of \mathbf{I} is zero. Instead, the overall angular momentum is removed by removing the momentum component of every atom in the AG that is perpendicular to the direction of the linear AG.

This procedure is done for each AG separately in the INITMOL subroutine and also for the whole AG (except for reactive collision run) before entering the simulation.

IV.B. Unimolecular processes

The user will provide an initial structure, which should be the optimized geometry of a local minimum by using INITX=0.

IV.B.1. State-selected initial conditions

This initial condition can be applied for both single-surface trajectories and nonadiabatic trajectories with multiple coupled surfaces. Here “state-selected” refers to vibrational state. For a nonadiabatic trajectory, the initial electronic state can be any electronic state. The representation used for nonadiabatic trajectory propagation is adiabatic by default, but the representation used for propagation can be changed to diabatic by using the keyword DIABATIC. However, we suggest to use the adiabatic representation to set up initial condition. To set up initial condition based on adiabatic representation, one has to add the specific potential energy surface called in ADTOD subroutine to get the transformation matrix between two representations. When the keyword DIABATIC is used, the propagation of the trajectory will be carried out in the diabatic representation by transforming the electronic coefficients of the adiabatic representation into electronic coefficients in the diabatic representation after the initial conditions are determined and before the propagation of the trajectory is started.

There are two choices to be made:

1. how much initial energy to put in each mode. This is determined by the keyword VIBSELECT.
2. how to distribute the coordinates and momenta consistent with the energy determined by choice 1. This is determined by the keyword VIBDIST.

Here are all options of keyword VIBSELECT.

VIBSELECT: The initial energy in vibrational mode m is called E_m . There are several choices, and they are all based in one way or another on using the harmonic approximation, but in different ways.

- 0: Default: Determined by other choices. For example, using keywords INITX=0, INITP = 1, and TE0FIXED = E , the program uses a fixed input geometry for all trajectories and the momenta are randomly determined based on the total energy E .
- 1: The user provides vibrational quantum numbers by the keyword

$$\text{VIBSTATE} = (n_1, n_2, \dots, n_{3N-6}) \quad \text{for a local minimum}$$

$$\text{VIBSTATE} = (n_1, n_2, \dots, n_{3N-7}) \quad \text{for a saddle point}$$
 The amount of energy in each mode m equals $E_m = (0.5 + n_m)h\nu$, where n_m is a quantum number, and ν is the vibrational frequency.
2. This option only applies to minimum-energy structures (not saddle points). The program assigns vibrational quantum numbers at random, selected out of a Boltzmann distribution at a user-specified temperature that is specified by the keyword TEMP0IM.
3. This option only applies to minimum-energy structures (not saddle points). The program performs a normal mode frequency analysis and uses it to generate an initial velocity from a Maxwell thermal distribution at a given

temperature TEMP0. This option should be combined with the keyword INTP=1. This is an option for canonical ensemble, not an option for state-selected ensemble.

- 4: The amount of energy in each mode is the same for each mode and is E_1 . Set VIBENE = E_1 . The unit for E_1 is eV.
- 5: The amount of energy in mode m is E_m , which can be different for each mode. Set VIBENE = $(E_1, E_2, \dots, E_{3N-6})$ or VIBENE = $(E_1, E_2, \dots, E_{3N-7})$. The units for E_m are eV.
- 6: Like VIBSELECT = 4 except that E_m is calculated by the program as $\min[(0.5 h\nu_\mu, \text{input } E_1)]$
- 7: Like VIBSELECT = 5 except that E_m is calculated by the program as $\min[(0.5 h\nu_\mu, \text{input } E_\mu)]$

When using the VIBSTATE or VIBENE keywords, note that the vibrational modes are in order of decreasing magnitude of their frequencies, independent of symmetries.

Note that only VIBSELECT = 1, 4, 5, 6, or 7 should be used for state-selected initial conditions.

VIBDIST: VIBDIST determines the type of phase space distribution for initial conditions prepared with normal mode analysis (see Section IV and Section A1 for more details). When VIBDIST is 0, 1, or 2, all the modes are treated in the same way.

- 0: Default: classical or quasiclassical distribution. This distribution is quasiclassical if VIBSELECT = 1 or 2, and it is classical if VIBSELECT \geq 4. With this option, the initial displacements are distributed between $-q_{\text{turn},m}$ and $+q_{\text{turn},m}$ in the same way as for a classical harmonic oscillator with the energy specified by VIBENE, where $q_{\text{turn},m}$ is the magnitude of the turning point determined by

$$\frac{1}{2}k_m q_{\text{turn},m}^2 = E_m$$

where q_m is the normal mode displacement coordinate, and k_m is the force constant. When this option is selected, the following steps are taken:

- (i) a random number λ is chosen (random numbers are always evenly distributed between 0 and 1), and the initial displacement is

$$q_m = q_{\text{turn},m} \cos(2\pi\lambda)$$

- (ii) The potential energy is evaluated with the actual potential function. If $V(q_m) - V(0) > E_m$, then $|q_m|$ is decreased by 10%, and this is repeated if necessary until

$$V(q_m) \leq V(0) + E_m.$$

Note that $V(0)$ denotes all the modes m' not yet assigned at $q_{m'} = 0$, those modes already assigned at their assigned values, and the current mode m at $q_m = 0$, whereas $V(q_m)$ denotes modes m' not yet assigned at $q_{m'} = 0$, those modes already assigned at their assigned values, and the current mode m at q_m . Because of this complication, the results depend on the order that the modes are assigned. For each trajectory the modes are assigned in a different order, as determined by random numbers.

- (iii) Another random number λ' is chosen to determine the sign of the momentum p_m in mode m .
- (iv) The momentum is assigned as

$$p_m = \text{sign}(\lambda') \sqrt{2\mu \left(E_m - [V(q_m) - V(0)] \right)}$$

Where μ is the normal-mode reduced mass.

- 1: If VIBSELECT=1, this option should be used only when n_m is 0. It may be called the ground-state harmonic oscillator distribution. Using a random number, the coordinate q_m is selected from the quantum mechanical harmonic oscillator coordinate distribution, which is the square of the ground-state wave function and is a Gaussian. This means that

$$\Delta q = \sigma_x \sqrt{-2 \ln(\lambda_1)} \cos(2\pi\lambda_2)$$

where λ_1 and λ_2 are two random numbers, and

$$\sigma_x = \sqrt{E_m / k_m}.$$

Then steps ii, iii, and iv above are repeated.

- 2: If VIBSELECT=1, this option should be used only when n_m is 0. A Wigner distribution obtained from the separable harmonic oscillator wave function in the normal mode representation. The distribution is generated using the Box-Muller algorithm for normal mode coordinate displacement and momentum. In particular the normal mode displacement and momentum is calculated as

$$q_m = \sigma_x \sqrt{-2 \ln(\lambda_1)} \cos(2\pi\lambda_2)$$

$$p_m = \sigma_p \sqrt{-2 \ln(\lambda_1)} \sin(2\pi\lambda_2)$$

$$\sigma_p = 1 / (2\sigma_x) \text{ and}$$

$$\sigma_x = \sqrt{E_m / k_m}.$$

Note that we use the same set of random numbers λ_1 and λ_2 in determining displacement and momentum.

- 9: This option allows one to use select option 1, 2, or 3 individually for each

IV.B.2. Vertical excitation initial conditions

Vertical excitation initial conditions have two options.

Vertical excitation Option 1 (VEO1): White light vertical excitation

1. Use options for initial conditions in state-selected systems to generate a ground-state distribution. One needs to input the ground-state minimum-energy geometry and use the keyword “NSURFI=1” to tell the program do the normal mode analysis for the ground state.
2. Use the keyword “nsurf0” to tell which surface to start propagating the trajectory, e.g., use “NSURF0=*N*” to start the trajectory on surface *N*.

With this option, the phase space distribution is determined on the ground state surface (NSURFI=1) and then the system is lifted vertically to the chosen excited state (specified by NSURF0), without changing the coordinates or momenta, where the lack of change of coordinates and momenta is the Franck-Condon principle. In practice this would occur only if the photon beam contained all frequencies (i.e., white light) since the energy gap between the surfaces varies with geometry.

Vertical excitation Option 2 (VEO2): Vertical excitation by photons with energies in a small window centered at a given fixed energy

This option is the same as option 1 except one uses the keyword VERTE to specify a photon energy (in eV) and the keyword BANDWD to specify the bandwidth of the photon energy (also in eV). Only excitations where the potential energy increases by an amount within the specified energy range ($verte \pm bandwd$) are accepted. Other phase space points are discarded.

Here are examples to illustrate the vertical excitation options.

Example: The program does normal-mode analysis on adiabatic surface 1 and determines the phase space distribution on adiabatic surface 1; then the system is lifted vertically to adiabatic surface 2 with white light (VEO1). This phase space distribution is determined by the keyword VIBSELECT=6 and VIBDIST=1 with 0.02 eV energy for each vibrational mode. Then, although the initial state is determined in the adiabatic representation, the trajectory will be carried out in the diabatic representation by transforming the electronic coefficients of the adiabatic representation into electronic coefficients in the diabatic representation after the initial conditions are determined and before the propagation of the trajectory is started.

```
$control potflag=10 hstep0=0.5 ranseed=31415926
bulstointhack eps=1.d-8 diabatic $end
$output outflag=4
22 10 11 20 21
maxprint nprint=200 minprinticon
$end
$surface nsurfi=1 nsurf0=2 nsurft=3 methflag=4 tinyrho=1e-4 $end
$termcon termflag=3 t_stime=20000
```

```

nbondbreak=1
7 13 6.0
$end
$traject ntraj=2 tflag1=0 $end
$data
nmol=1
natom=13 initx=0 initp=-1 vibselect=6 vibdist=1
0 1
C 12.000000 0.000000000 0.937824000 0.000000000
C 12.000000 -1.205700000 0.234366000 0.000000000
C 12.000000 -1.188436000 -1.160295000 0.000000000
C 12.000000 0.019898000 -1.854419000 0.000000000
C 12.000000 1.218764000 -1.138023000 0.000000000
C 12.000000 1.217257000 0.253677000 0.000000000
O 15.994915 0.052145000 2.302309000 0.000000000
H 1.0079400 -2.153827000 0.775630000 0.000000000
H 1.0079400 -2.132277000 -1.705333000 0.000000000
H 1.0079400 0.028771000 -2.943124000 0.000000000
H 1.0079400 2.170159000 -1.669900000 0.000000000
H 1.0079400 2.143024000 0.827143000 0.000000000
H 1.0079400 -0.912397652 2.641373527 0.000000000
vibene
0.02
$end

```

Example: The initialization on the lower surface (where the photon is absorbed) is like example 2, but this example uses option VEO2 with `verte=4.5` and `bandwd=0.2`. The initial distribution corresponds to a pure adiabatic state, and the trajectory will be carried out in the diabatic representation by transforming the electronic coefficients of the adiabatic representation into electronic coefficients in the diabatic representation after the initial conditions are determined and before the propagation of the trajectory is started.

```

$control potflag=10 hstep0=0.5 ranseed=31415926
bulstointhack eps=1.d-8 diabatic $end
$output outflag=4
22 10 11 20 21
maxprint nprint=200 minprinticon
$end
$surface nsurfi=1 nsurf0=2 nsurft=3 methflag=4 tinyrho=1e-4 $end
$termcon termflag=3 t_stime=20000
nbondbreak=1
7 13 6.0
$end
$traject ntraj=2 tflag1=0 $end
$data
nmol=1
natom=13 initx=0 initp=-1 vibselect=6 vibdist=1 verte=4.5 bandwd=0.2

```

```

0 1
C 12.000000  0.000000000  0.937824000  0.000000000
C 12.000000 -1.205700000  0.234366000  0.000000000
C 12.000000 -1.188436000 -1.160295000  0.000000000
C 12.000000  0.019898000 -1.854419000  0.000000000
C 12.000000  1.218764000 -1.138023000  0.000000000
C 12.000000  1.217257000  0.253677000  0.000000000
O 15.994915  0.052145000  2.302309000  0.000000000
H 1.0079400 -2.153827000  0.775630000  0.000000000
H 1.0079400 -2.132277000 -1.705333000  0.000000000
H 1.0079400  0.028771000 -2.943124000  0.000000000
H 1.0079400  2.170159000 -1.669900000  0.000000000
H 1.0079400  2.143024000  0.827143000  0.000000000
H 1.0079400 -0.912397652  2.641373527  0.000000000
vibene
0.02
$end

```

IV.B.3. Fixed-energy initial conditions

One could use the input options described in the subsection IV.B.1 to prepare a state-selected initial condition or subsection IV.B.2. to prepare a vertical excitation, but also add another keyword TE0FIXED to specify a total energy E_0 for the system. Note that the system total energy given by a state-selected initial condition or a vertical excitation initial condition could differ with the desired total energy E_0 . Therefore the code prepares a fixed-energy initial condition using two steps: (1) calculate the initial geometry and momenta based on the input state-selected initial conditions or input vertical excitation initial condition; (2) calculate the potential energy (PE), kinetic energy (KE), and adjust momentum to satisfy the desired total energy (TE) by the following criteria:

- a) If $PE > E_0$, re-generate initial geometry and momentum.
- b) If $PE \leq E_0$ then, keep the geometry, but scale the momentum by

$$P_{\text{new}}^{ij} \leftarrow P_{\text{old}}^{ij} \sqrt{\frac{E_0 - PE(\mathbf{X})}{KE(\mathbf{P}_{\text{old}})}}.$$

Note this two-step procedure is performed internally by the code using a single input file.

IV.B.4. Fixed-temperature initial conditions

To set up an ensemble at a constant temperature, the keywords NVT and TEMP0 in \$CONTROL input deck should be used to specify the system at constant temperature TEMP0. In the \$TRAJECT input deck, one should specify a thermostat by using the keyword IADJTEMP. The available thermostats are Berendsen thermostat (default), Andersen thermostat, Nosé-Hoover two-chain thermostat, and a simple thermostat by scaling the momentum with a factor of $\sqrt{T_0/T}$ (T_0 is the target temperature and T is the current temperature). User can see the Section XII for more details of these thermostats.

The keyword `INITP=1` should be given to generate random thermal distribution for momenta. The current code is only designed to generate random geometries for metal clusters for initial geometries in a fixed temperature run. For example, use `INITX=1, 2 or 3` to generate random atom coordinates.

IV.C. Bimolecular collisions

ANT has three methods to simulate bimolecular reactive collisions. One method is only for atom–diatom systems, and it has been thoroughly discussed in the book chapter of Ref. 17 (all cited references are in Section XV). The special initial conditions for the atom–diatom case are controlled in the `$ATOMDIATOM` input deck. Another method is an extension of this option to diatom–diatom conditions; this special option is not available yet, but when it is available it will be controlled in the `$DIATOMDIATOM` input deck. The third method for setting initial conditions is very general; it works for general collisions of an atom with a polyatomic molecule or for general molecule–molecule collisions as well as for atom–diatom and diatom–diatom collisions, although for the latter we recommend the use of the special atom–diatom and (when available) diatom–diatoms methods. For this general bimolecular collision method, the user may refer to general discussions of how to simulate reactive cross sections and rate constants in, for example, Refs. 17 and 18.

IV.C.1. General bimolecular collision initial conditions

The program follows a general convention, which involves shooting a second Atom Group (AG) toward the first AG, where the two AGs are initially separated by a distance `R0COLLISION`. Then the initial conditions (such as the orientation of the first AG, the initial relative translational energy (if translational energy is thermal), and the vibrational and rotational phases of the two colliding AGs) are sampled by a Monte Carlo method.

The maximum allowed distance (`R0COLLISION`) between the two AGs is provided by the user in the `$RXCOLLISION` input deck or automatically generated by the program. Other initial conditions can be prepared by the following methods:

IV.C.1.a. State-selected run

User provides vibrational states, rotational states for linear AG or rotational energies for non-linear AG, and relative translational energies. The combination of the keywords and input for this method is:

- a. In the `$RXCOLLISION` input deck, write keyword `STATESELECT`
- b. In the `$DATA` input deck, in the same line providing `INITX`, `INITP`, specify a `VIBSELECT` value (see more details in the next subsection for choice of `VIBSELECT`), and provide relative translational energy `ERELTRANS` between the two AGs by for example `ERELTRANS=0.5` (unit: $k_B T$).
- c. In the `$DATA` input deck, right after the geometry of each AG, provide information of how much energy for each vibrational state, e.g. vibrational quantum numbers and rotational quantum number (for linear AG only) or three rotational energies (for non-linear AG; unit: $k_B T$). The following is an example:

`VIBSTATES`

```

1 0 1 0 1
ROTSTATE
1

```

Or:

```

VIBSTATES
1 0 1 0 1
ROTENERGIES
0.5 1.0 2.0

```

IV.C.1.b. Initial conditions provided by an equilibration run

- a. In the \$RXCOLLISION input deck, write keyword EQUILIBRIUM.
- b. In the \$TRAJECT input deck, specify the beginning step and probability to save the initial conditions by specifying for example ITOSAVE=1000 and PICKTHR=0.5 (PICKTHR=1.0 will save at every step). The integration time step used for the equilibration run is equal to the global time step specified in the \$CONTROL input deck.
- c. The user can still provide vibrational states, but these values are only used for preparing the initial conditions for the equilibration run.
- d. The program will save NTRAJ structures and momenta in the file unit 60 (coordinate) and 61 (momentum) for the first AG, 62 and 63 for the second AG if there are. The user can specify three methods to choose these points to be saved: IPICKTRJ=0 (default): If the program finds that the original AG is fragmented before the NTRAJ points are saved, the equilibration will restart from the very beginning, discarding previous saved points and repeating this procedure until all NTRAJ points are all saved in one equilibration run; IPICKTRJ=1: Once equilibration fails (AG fragmented), do not abandon previously saved points and repeat the equilibration from very beginning until all NTRAJ points are saved; IPICKTRJ=2: Effectively put a soft wall before an atom if it breaks bonds with all other atoms by reversing its radial momentum against the center of mass of the whole AG in the equilibration. The last two methods can allow the user to save points with energy higher than the dissociation limit.
- e. The program will read from file unit 60-63 for initial geometries and momenta.
- f. After initial structures are read, the AG is transformed to its own coordinate system of principal axes of rotation.
- g. Initial rotational states (or energies) of each AG are either fixed if provided by the user or randomly generated according to Boltzmann distribution.
- h. Initial rotational orientation of AG is randomly determined.
- i. The relative translational energy between the two AGs is either fixed if provided by the user or randomly generated according to Boltzmann distribution.

It should be noted that randomly generated clusters are not local minima and thus the program cannot perform a vibrational state-selected run starting from these clusters. For these random clusters, VIBSELECT can only be specified as 0 (The program will abort in this situation.).

IV.C.1.c. State-selected initial conditions for part of initial quantum states

User can choose to provide some of quantum states, e.g. vibrational states, rotational states (or energies for non-linear AGs) or relative translational energy, by specifying a state-selected run in the \$RXCOLLISION (write keyword STATESELECT), but the other quantum states are generated randomly. The values provided for selected states will be fixed during the simulation. For example, the user can specify VIBSELECT=2 to tell the program to randomly generate initial vibrational states according to Boltzmann distribution. For randomly generated structures, the user can specify INITP=1 to randomly generate thermally distributed initial momenta for the atoms in the AG. See the Input file section (Section XII) of this manual for more details.

IV.C.2. Atom–diatom collision initial conditions

The initial conditions for atom–diatom collisions can be set up by the user by using either of two different procedures:

1. Atom–diatom collisions corresponding to specified initial quantized rotational and vibrational energies and either a fixed initial relative translational energy or a fixed total energy.
2. A general method for bimolecular collisions that can also be used for polyatomics, as described in the previous section.

Note carefully that the two methods will not yield identical results because different algorithms are used (e.g., WKB is used to assign vibrational state energies if \$ATOMDIATOM is chosen, whereas the harmonic approximation is used in the more-general treatment).

IV.C.2.a. Initial conditions corresponding to specified initial quantized rotational and vibrational energies and a fixed initial relative translations energy

The user can specify different initial conditions for collisions of an atom with some selected rovibrational state (n,j) of the diatom at some fixed center-of-mass collision energy E_{rel} . The different input options for special atom–diatom simulations are provided by the user in the \$ATOMDIATOM input deck. The available keywords are:

- a. Use the \$ATOMDIATOM input deck for special atom–diatom simulations.
- b. ESCATAD: The total energy in eV. This is also called the scattering energy, i.e. the energy of collision plus the internal energy of the diatom in the rovibrational state (n,j):

$$E_{scat} = E_{col} + E_{int}$$

- c. ECOL: The initial collision energy in eV.
- d. JZERO: An impact parameter appropriate for $J = 0$ scattering will be randomly chosen
- e. B_MIN: The lower bound on a randomly chosen impact parameter
- f. B_MAX: The upper bound on a randomly chosen impact parameter
- g. VVAD: Initial vibrational quantum number for the diatom.
- h. JJAD: Initial rotational quantum number for the diatom.
- i. RRAD0: Initial atom–diatom separation in Å.
- j. ARRAD: Integer input: Initial molecular arrangement.
 - 1: AB+C.

2: BC+A.

3: AC+B.

Note that in the atom–diatom simulation input only one AG is specified in the \$DATA input deck.

- k. In the \$DATA input deck, INITX=4 and INTP=-1, i.e. the Cartesian coordinates and initial momenta are determined by the parameters described above.

One must provide either a total energy (ESCATAD) or a collision energy (ECOL). Additionally, one must choose one of two options for assigning an impact parameter, b ; either JZERO or B_MIN and B_MAX. The user may set B_MIN = B_MAX in order to choose a specific value of b .

The five collision parameters that characterize a collision, i.e.:

- a. b : impact parameter.
- b. θ : the initial azimuthal orientation angle of the diatom internuclear axis.
- c. ϕ : the initial polar orientation angle of the diatom internuclear axis.
- d. η : the initial orientation of the diatom angular momentum.
- e. ξ : the initial phase angle of the diatom vibration.

are selected by Monte Carlo before integrating every classical trajectory. In general, the impact parameter b should be selected in a range from 0 to some maximum value large enough to compute cross sections and rate constants by the methods described in Ref. 15.

IV.C.2.b. General atom–diatom initial conditions

The second method to choose the initial conditions of the atom–diatom collision is a general method that also works for polyatomics.

The program follows a general convention, which involves shooting a second Atom Group (AG) toward the first AG, where the atom and the diatom are initially separated by a distance R0COLLISION. Then the initial conditions (such as the orientation of the diatom, the initial relative translational energy (if translational energy is thermal), and the vibrational and rotational phases of the diatom) are sampled by a Monte Carlo method.

The maximum allowed distance (R0COLLISION) between the atom and the diatom is provided by the user in the \$RXCOLLISION input deck or automatically generated by the program. Other initial conditions can be prepared by the following methods:

IV.C.2.b.1 State-selected run

User provides vibrational states, rotational states for the diatom, and relative translational energies. The combination of the keywords and input for this method is:

- a. In the \$RXCOLLISION input deck, write keyword STATESELECT
- b. In the \$DATA input deck, in the same line providing INITX, INTP, specify a VIBSELECT value (see more details in the next subsection for choice of VIBSELECT), and provide relative translational energy ERELTRANS between the atom and the diatom by for example ERELTRANS=0.5 (unit: $k_B T$).

- c. In the \$DATA input deck, right after the geometry of diatom, provide information of how much energy for each vibrational state, e.g. vibrational quantum numbers and rotational quantum number (for the diatom only). The following is an example:
1. VIBSTATES
 2. 1 0 1 0 1
 3. ROTSTATE
 4. 1

IV.C.2.b.2 Initial conditions provided by an equilibration run

- a. In the \$RXCOLLISION input deck, write keyword EQUILIBRIUM.
- b. In \$CONTROL input deck, TEMP0 defines the temperature of the run. The user can provide temperatures different from the global temperature in the \$control deck by providing a TEMP0IM input when the initial momenta of the diatom are selected by using a random thermal distribution (INITP=1).
- c. In the \$TRAJECT input deck, specify the beginning step and probability to save the initial conditions by specifying for example ITOSAVE=1000 and PICKTHR=0.5 (PICKTHR=1.0 will save at every step). The integration time step used for the equilibration run is equal to the global time step specified in the \$CONTROL input deck.
- d. The user can still provide vibrational states, but these values are only used for preparing the initial conditions for the equilibration run.
- e. The program will save NTRAJ structures and momenta in the file unit 60 (coordinate) and 61 (momentum) for the first AG, 62 and 63 for the second AG. The user can specify three methods to choose these points to be saved:
 - IPICKTRJ=0 (default): If the program finds that the original diatom is fragmented before the NTRAJ points are saved, the equilibration will restart from the very beginning, discarding previous saved points and repeating this procedure until all NTRAJ points are all saved in one equilibration run;
 - IPICKTRJ=1: Once equilibration fails (AG fragmented), do not abandon previously saved points and repeat the equilibration from very beginning until all NTRAJ points are saved;
 - IPICKTRJ=2: Effectively put a soft wall before an atom if it breaks bonds with all other atoms by reversing its radial momentum against the center of mass of the whole AG in the equilibration. The last two methods can allow the user to save points with energy higher than the dissociation limit.
- f. The program will read from file unit 60-63 for initial geometries and momenta.
- g. After initial structures are read, the diatom is transformed to its own coordinate system of principal axes of rotation.
- h. Initial rotational states of the diatom are either fixed if provided by the user or randomly generated according to Boltzmann distribution.
- i. Initial rotational orientation of the diatom is randomly determined.

- j. The relative translational energy between the atom and the diatom is either fixed if provided by the user or randomly generated according to Boltzmann distribution.

IV.C.2.b.3 State-selected initial conditions for part of initial quantum states

User can choose to provide some of quantum states, e.g. vibrational states, rotational states or relative translational energy, by specifying a state-selected run in the \$RXCOLLISION (write keyword STATESELECT), but the other quantum states are generated randomly. The values provided for selected states will be fixed during the simulation. For example, the user can specify VIBSELECT=2 to tell the program to randomly generate initial vibrational states according to Boltzmann distribution. For randomly generated structures, the user can specify INITP=1 to randomly generate thermally distributed initial momenta for the atoms in the diatom. See the Input file section (Section XII) of this manual for more details.

IV.C.3. Diatom–diatom collision initial conditions

The initial conditions for diatom–diatom collisions can be set up by the user by using either of two procedures:

1. diatom–diatom collisions corresponding to specified initial quantized rotational and vibrational quantum numbers and either a fixed initial relative translational energy or a fixed total energy.
2. a general method for bimolecular collisions that can also be used for polyatomics, as described in the previous section.

This section of the manual describes method 1, which is described by the *\$diatomdiatom* block of the input file. Note that the two methods will not yield identical results because different algorithms are used (e.g., the WKB is used to assign vibrational state energies if *\$diatomdiatom* is chosen, whereas the harmonic approximation is used in the more general treatment).

A sample input for the *\$diatomdiatom* block for fixed temperature:

```
$diatomdiatom
ecoldd=1           # collision energy in eV
bmin=0 bmax=8     # impact parameter randomly selected from 0 to 8 Å
randomjv jvtemp=500 # randomly select j and v quantum numbers at temperature 500 K
r0dd=10          # initial diatom–diatom separation in Å
arrdd=1          # initial arrangement of the four atoms, 1: AB + CD
$end
```

A sample input for the *\$diatomdiatom* block for specified initial quantum numbers:

```
$diatomdiatom
ecoldd=1           # collision energy in eV
bmin=0 bmax=8     # impact parameter randomly selected from 0 to 8 Å
vdia1=0 jdia1=0   # selected j and v quantum number for diatom 1
vdia2=1 jdia2=1   # selected j and v quantum number for diatom 2
r0dd=10          # initial diatom–diatom separation in Å
arrdd=1          # initial arrangement of the four atoms, 1: AB + CD
```

\$end

The keywords for the *\$diatomdiatom* block:

Group	Keywords	Description	Notes
1	etotdd	total energy in eV	One of these variable is required
	ecoldd	collision energy in eV	
2	bfix	<i>b</i> value in Angstrom for fixed- <i>b</i> calculations	If bfix is given, bmax and bmin are not needed.
	bmax	maximum <i>b</i> in Å	If bfix is not given, both bmax and bmin are needed.
	bmin	minimum <i>b</i> in Å	
3	randomjv	Select <i>j</i> and <i>v</i> randomly based on one temperature <i>T</i> that is the same for vibration and rotation	If randomjv is given, <i>j</i> and <i>v</i> will be randomly selected, and jvtemp is required for setting <i>T</i> .
	jvtemp	Temperature in K under which <i>j</i> and <i>v</i> will be selected	
	vdia1	vibrational quantum number for diatom 1	If randomjv is not given, vdia1 , jdia1 , vdia2 , and jdia2 are used to set the <i>j</i> and <i>v</i> values for the two diatoms.
	jdia1	rotational quantum number for diatom 1	
	vdia2	vibrational quantum number for diatom 2	
	jdia2	rotational quantum number for diatom 2	
4	r0dd	initial diatom–diatom separation in Å	r0dd must be greater than or equal to bfix or bmax .
5	arrdd	Initial arrangement of the four atoms, only one arrangement is needed, the other is set as 7-arrdd.	for 4 atoms ABCD: 1 A-B, 1-2 2 A-C, 1-3 3 A-D, 1-4 4 B-C, 2-3 5 B-D, 2-4 6 C-D, 3-4

Theoretical details of the methods used in the *\$diatomdiatom* block can be found in J. D. Bender, P. Valentini, I. Nompelis, Y. Paukku, Z. Varga, D. G. Truhlar, T. Schwartzenruber, and G. V. Candler, *J. Chem. Phys.* **143**, 054304 (2015).

A *\$diatomdiatom* calculation, the first step is to generate files that contain information about all the available rovibrational states of each of the two diatoms. If the number of surfaces specified by **nsurf0** in the *\$SURFACE* input deck is *x*, then the program looks for files named *jvstates_diatom_1_surf_x* and *jvstates_diatom_2_surf_x*. If it finds these files, it uses them. If it does not find these files it will generate them by the WKB approximation.

Once the file has been generated, it can be used for this trajectory run or later trajectory runs, and it can be used to plot an energy level diagram.

The file contains three blocks:

Block 1 is basis information for the rovibrational states, for example:

Potential energy surface number:	3
Diatomic arrangement number:	1
Total number of rotational levels:	37
Number of vibrational levels for $j = 0$:	15
Number of rovibrational levels (total, bound, quasibound):	334 286 48

Block 2 summarizes the information for each rotational state j :

Maximum vibrational quantum number: v_{max}

Local minimum point on the diatom potential energy curve [r_{min}, E_{min}]

Local maximum point on the diatom potential energy curve [r_{max}, E_{max}]

j	vmax	rmin [bohr]	emin [hartree]	rmax [bohr]	emax [hartree]
...					

Block 3 contains information for each rovibrational state:

First column is an *index* number for this state.

Fourth column is energy for this state, *edia*.

Inner and outer turning points of this state on the potential energy curve, r_{in} and r_{out}

Vibrational period of this state, *tau*

Index	j	v	edia [hartree]	rin [bohr]	rout [bohr]	tau [hbar/hartree]
...						

Descriptions for subroutines used to generate the above files and generate the initial conditions for the diatom pair:

diatom_ewkb.f90

- computes the total diatomic internal energy \mathcal{E}_{int} from the continuous rotational and vibrational quantum numbers, j and v , respectively. It calls **diatom_vwkb** in a loop, using a simple bisection method for root-finding.

diatom_genjvstate.f90

- uses the subroutines **diatom_minmax**, **diatom_vwkb**, and **diatom_ewkb** to compute:
 - the total number of rotational energy levels,
 - the number of vibrational energy levels for each rotational energy level,
 - the total number of rovibrational energy states, and how many of them are bound or quasibound,
 - the coordinates of the local minimum ($r_{min}, \mathcal{E}_{int,min}$) and the local maximum ($r_{max}, \mathcal{E}_{int,max}$) in the effective diatomic potential energy curve for each rotational energy level,
 - the total diatomic internal energy $\mathcal{E}_{int,eff}$ of each rovibrational energy state,

- the separation distances r^- and r^+ corresponding to the inner and outer turning points for each rovibrational energy state, and
- the vibrational period τ for each rovibrational energy state.

diatom_getjvstate.f90

- returns the index and various properties of a randomly selected rovibrational energy state for a diatom. The subroutine first generates random numbers and then selects a state by using the cumulative probability calculated by **diatom_jvprobs**.

diatom_init.f90

- generates initial coordinates and momenta for two atoms in a diatom specified by a diatomic arrangement identifier *arrdd* in the diatom's center-of-mass coordinate system. It requires as inputs the total diatomic internal energy ε_{int} and the separation distances at the inner and outer turning points, r^- and r^+ , respectively, all of which can be calculated by the subroutine **diatom_edia**. Also, it requires as an input the diatomic vibrational period τ , which can be calculated by the subroutine **diatom_tau**. The subroutine performs several tasks:
 1. It randomizes the orientation of the axis of symmetry of the diatom, a process that requires two randomized angles to orient a unit vector in three-dimensional space.
 2. It randomizes the orientation of the diatomic internal angular momentum, a process that requires one additional angle to orient an additional unit vector perpendicular to the first unit vector.
 3. It generates a random number ξ in the range of 0 to 2π , then integrate the diatomic equation of motion from $r = r^-$ for a time $(\xi/2\pi)\tau$ if $\xi < \pi$, or from $r = r^+$ for a time $((\xi - \pi)/2\pi)\tau$ if $\xi \geq \pi$.
- After these three tasks are performed, the subroutine generates the new coordinates and momenta (in the diatom's center-of-mass coordinate system, with the center-of-mass at the origin)

diatom_jvprobs.f90

- calculates the probabilities of finding a diatom in its allowable energy states based on one-temperature model. (By “one-temperature model,” we mean using the same temperature for rotation as for vibration.) This subroutine requires information for all available j and v states, which are computed by the subroutine **diatom_getjvstate**.

diatom_minmax.f90

- finds the local minimum point $(r_{\text{min}}, \varepsilon_{\text{int,min}})$ and local maximum point $(r_{\text{max}}, \varepsilon_{\text{int,max}})$ in an effective diatomic potential energy curve, if one or both exist.

diatom_place.f90

- places the two diatoms according to the initial separation and b parameter.

diatom_pot.f90

- returns the effective diatomic internal energy $\varepsilon_{\text{int,eff}}$ for a given geometry and rotational state.

- **THIS FILE HAS TO BE MODIFIED BY THE USER, SEE THE INSTRUCTIONS BELOW.**

diatom_tau.f90

- computes the diatomic vibrational period τ . It uses a numerical integration algorithm based on Gauss-Chebyshev quadrature. This subroutine involves calls of the subroutine **diatom_pot**. Also, it requires as inputs the diatomic separation distances at the inner and outer turning points, r^- and r^+ respectively, which are computed using the subroutine **diatom_turn**.
- See below for further theoretical background. Note that the algorithm used here is similar to but not identical to the algorithm used in the subroutine **diatom_vwkb**.

diatom_turn.f90

- calculates the diatomic separation distances at the inner and outer turning points, r^- and r^+ respectively. It uses a simple bisection method for root finding.

diatom_vwkb.f90

- computes the continuous vibrational quantum number ν from the continuous rotational quantum number j and the total diatomic internal energy ϵ_{int} . It uses the WKB approximation and a numerical integration algorithm based on Gauss-Chebyshev quadrature.
- See below for further theoretical background.

Required modifications in file diatom_pot.f90

The content of this file corresponds to the OH₃ example of diatom–diatom calculations. Namely, the two diatomic potential energy curves of the atom groups defined by **arrdd** have to be given. In this particular case of OH₃, the two diatom atom groups, the first excited state of OH and ground state of H₂, are placed far apart from each other and the coordinates of the “inactive” diatom is fixed at its equilibrium geometry and the energy of the “active” diatom is at various geometries.

In the file, the line “This part defined by user” shows where the modifications have to be made. As the example of OH₃ shows that, the diatomic energies can be obtained directly from the four-body surfaces. But if the four-body potential energy surface subroutine has distinguished diatomic potential energy curves, then it is easier call the corresponding diatomic subroutines for the two diatomic groups defined by **arrdd**. Also note that, if the system has multiple states, then picking the right states for the diatoms are important for meaningful calculations.

Theoretical background for diatom_vwkb

The effective diatomic potential energy $V_{D,\text{eff}}(r)$ is defined as the diatomic potential energy plus the centrifugal term:

$$V_{D,\text{eff}}(r) = V_D(r) + \frac{j(j+1)\hbar^2}{2\mu r^2} \quad (1)$$

Note that this same relation is valid if interpreted in atomic units.

Using the WKB approximation to estimate a solution to the Schrodinger equation, the continuous vibrational quantum number is given by the following: ¹

$$v' = -\frac{1}{2} + \frac{(2\mu)^{1/2}}{\pi\hbar} \int_{r-}^{r+} (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{1/2} dr \quad (2)$$

In atomic units, this equation becomes the following, where we have defined $a = r-$ and $b = r+$, the inner and outer turning points, respectively:

$$v' = -\frac{1}{2} + \frac{(2\mu)^{1/2}}{\pi} \int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{1/2} dr \quad (3)$$

We wish to numerically evaluate the integral in Eq. (3). First recall that the following numerical approximation can be derived using a Gauss-Chebyshev quadrature scheme:²

$$\int_{-1}^1 f(x)(1-x^2)^{1/2} dx \approx \sum_{i=1}^n \omega_i f(x_i) \quad (4)$$

Here, the *integration points* x_i and *weights* w_i are, for $i = 1, \dots, n$,

$$x_i = \cos\left(\frac{i\pi}{n+1}\right) \quad \text{and} \quad \omega_i = \frac{\pi}{n+1} \sin^2\left(\frac{i\pi}{n+1}\right) \quad (5)$$

First define the following change of variables:

$$r = r(x) = \frac{b-a}{2}x + \frac{b+a}{2} \quad (6)$$

Observe that $x = -1 \Rightarrow r = a$ and $x = 1 \Rightarrow r = b$. It is also easy to show that

$$1-x^2 = (r-a)(b-r) \left(\frac{2}{b-a}\right)^2 \quad (7)$$

Then we derive

$$\begin{aligned} & \int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{1/2} dr \\ &= \int_a^b \left(\frac{\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r)}{(r-a)(b-r)} \right)^{1/2} ((r-a)(b-r))^{1/2} \left(\frac{2}{b-a}\right) \left(\frac{b-a}{2}\right) dr \\ &= \int_a^b g(r) \left((r-a)(b-r) \left(\frac{2}{b-a}\right)^2 \right)^{1/2} \left(\frac{b-a}{2}\right) dr \\ &= \left(\frac{b-a}{2}\right) \int_a^b g(r) \left((r-a)(b-r) \left(\frac{2}{b-a}\right)^2 \right)^{1/2} dr \\ &= \left(\frac{b-a}{2}\right)^2 \int_{-1}^1 g(r(x))(1-x^2)^{1/2} dx \end{aligned} \quad (8)$$

where we have defined the function

$$g(r) = \left(\frac{\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r)}{(r-a)(b-r)} \right)^{1/2} = g(r(x)) \quad (9)$$

with $r = r(x)$ given by Eq. (6). Thus, from Eq. (4), we obtain the approximation

$$\int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{1/2} dr \approx \left(\frac{b-a}{2}\right)^2 \sum_{i=1}^n \omega_i g(r(x_i)) \quad (10)$$

and so

$$v' = -\frac{1}{2} + \frac{(2\mu)^{1/2}}{\pi} \int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{1/2} dr \approx -\frac{1}{2} + \frac{(2\mu)^{1/2}}{\pi} \left(\frac{b-a}{2}\right)^2 \sum_{i=1}^n \omega_i g(r(x_i)) \quad (11)$$

where $g(r)$ is given by Eq. (9), $r(x)$ is given by Eq. (6), and the x_i and ω_i are given by Eq. (5).

Note that convergence with this numerical integration scheme is usually very fast. In a typical test case, we found that the result for v' was quite well converged for $n = 20$.

Theoretical background for *diatom_tau*

Conservation of energy gives: ³

$$\varepsilon'_{\text{int}} = \frac{\mu}{2} \left(\frac{dr}{dt}\right)^2 + V_{D,\text{eff}}(r) \quad (12)$$

Let τ be the period of diatomic vibration. Then we immediately derive the following relationship, where we have defined $a = r_-$ and $b = r_+$, the inner and outer turning points, respectively:

$$\int_a^b dt = \frac{\tau}{2} = \left(\frac{\mu}{2}\right)^{1/2} \int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{-1/2} dr \quad (13)$$

We wish to numerically evaluate the integral in Eq. (13). First recall that the following numerical approximation can be derived using a Gauss-Chebyshev quadrature scheme: ⁴

$$\int_{-1}^1 f(x)(1-x^2)^{-1/2} dx \approx \sum_{i=1}^n \omega_i f(x_i) \quad (14)$$

Here, the *integration points* x_i and *weights* w_i are, for $i = 1, \dots, n$,

$$x_i = \cos\left(\frac{(2i-1)\pi}{2n}\right) \quad \text{and} \quad \omega_i = \frac{\pi}{n} \quad (15)$$

First define the following change of variables:

$$r = r(x) = \frac{b-a}{2}x + \frac{b+a}{2} \quad (16)$$

Observe that $x = -1 \Rightarrow r = a$ and $x = 1 \Rightarrow r = b$. It is also easy to show that

$$1-x^2 = (r-a)(b-r) \left(\frac{2}{b-a}\right)^2 \quad (17)$$

Then we derive

$$\begin{aligned}
& \int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{-1/2} dr \\
&= \int_a^b \left(\frac{(r-a)(b-r)}{\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r)} \right)^{1/2} \left(\frac{1}{(r-a)(b-r)} \right)^{1/2} \left(\frac{b-a}{2} \right) \left(\frac{2}{b-a} \right) dr \\
&= \int_a^b h(r) \left(\frac{1}{\left((r-a)(b-r) \left(\frac{2}{b-a} \right)^2 \right)^{1/2}} \right)^{1/2} \left(\frac{2}{b-a} \right) dr \\
&= \int_{-1}^1 h(r(x)) (1-x^2)^{-1/2} dx
\end{aligned} \tag{18}$$

where we have defined the function

$$h(r) = \left(\frac{(r-a)(b-r)}{\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r)} \right)^{1/2} = h(r(x)) \tag{19}$$

with $r = r(x)$ given by Eq. (16). Thus, from Eq. (15), we obtain the approximation

$$\int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{-1/2} dr \approx \sum_{i=1}^n \omega_i h(r(x_i)) \tag{10}$$

and so

$$\frac{\tau}{2} = \left(\frac{\mu}{2} \right)^{1/2} \int_a^b (\varepsilon'_{\text{int}} - V_{D,\text{eff}}(r))^{-1/2} dr \approx \left(\frac{\mu}{2} \right)^{1/2} \left(\frac{\pi}{n} \right) \sum_{i=1}^n h(r(x_i)) \tag{11}$$

where $h(r)$ is given by Eq. (19), $r(x)$ is given by Eq. (17), and the x_i and ω_i are given by Eq. (15).

Note that convergence with this numerical integration scheme is usually very fast. In a typical test case, we found that the result for v' was quite well converged for $n = 20$.

Example of diatom–diatom calculations

The directory of `testrun_oh3/` contains an example for diatom–diatom calculations. The corresponding surface subroutine file (`oh3_pes.f90`) is located in directory `pot/`. To carry out the WKB calculations for the diatoms defined as atom groups, the corresponding diatomic potential energy curves are defined in file `diatom_pot.f90` in directory `src/diatom`.

¹See Eqs. (91) and (92) in D. G. Truhlar and J. T. Muckerman, in *Atom-Molecule Collision Theory: A Guide for the Experimentalist*, edited by R. B. Bernstein (Plenum Press, New York, 1979), pp. 533-534.

Also see Chap. 8 and especially Eq. (8.51) in D. J. Griffiths, *Introduction to Quantum Mechanics*, 2nd ed. (Pearson Prentice Hall, Upper Saddle River, NJ, 2005).

Further discussion of WKB theory can be found in Chap. 10 of C. M. Bender and S. A. Orszag, *Advanced Mathematical Methods for Scientists and Engineers I: Asymptotic Methods and Perturbation Theory* (Springer, New York, 1999).

Finally, note the interpretation of the continuous rotational and vibrational quantum numbers in terms of action variables. See, for example, the discussion of Eq. (14.15) in T. W. B. Kibble and F. H. Berkshire, *Classical Mechanics*, 5th ed. (Imperial College Press, London, 2009).

²See Eqs. (27.46) and (27.47) in K. F. Riley, M. P. Hobson, and S. J. Bence, *Mathematical Methods for Physics and Engineering*, 3rd ed. (Cambridge University Press, Cambridge, UK, 2006), p. 1009.

Also see the discussion in D. G. Truhlar and J. T. Muckerman, in *Atom-Molecule Collision Theory: A Guide for the Experimentalist*, edited by R. B. Bernstein (Plenum Press, New York, 1979), pp. 514-515.

³See, for example, Eq. (4.12) in T. W. B. Kibble and F. H. Berkshire, *Classical Mechanics*, 5th ed. (Imperial College Press, London, 2009).

⁴See Eqs. (27.44) and (27.45) in K. F. Riley, M. P. Hobson, and S. J. Bence, *Mathematical Methods for Physics and Engineering*, 3rd ed. (Cambridge University Press, Cambridge, UK, 2006), p. 1009.

Also see the discussion in D. G. Truhlar and J. T. Muckerman, in *Atom-Molecule Collision Theory: A Guide for the Experimentalist*, edited by R. B. Bernstein (Plenum Press, New York, 1979), pp. 514-515.

V. Integration

Input keywords presented in this section:

BULSTOINTHACK, BULSTOINT, RUNKUT4, VERLET0, VVERLET, BEEMAN, LIOUVILLE.

All $3N_{\text{atom}}$ Cartesian coordinates and momenta for the nuclei, the real and imaginary parts of the electronic wave function (for electronically nonadiabatic simulations), and other quantities are integrated in the subroutine TAKESTEP. The integration algorithm calls DERIVS whenever a set of time derivatives is needed. DERIVS packs the nuclear and electronic coordinates into a single array Y, calls GETGRAD to obtain the information necessary to compute the time derivatives of Y (called DY) and returns DY. The integrator then uses one or more values of Y and DY to advance the system in time.

Several integration schemes are available, and the desired integration scheme is controlled by the following input keywords.

BULSTOINTHACK: The Bulirsch-Stoer method with adaptive step size and an accurate scheme for hopping or switching probabilities. See *Numerical Recipes* for details [Ref. 2 in Section XV] of the Bulirsch-Stoer integration scheme. The accurate scheme for calculation of hopping or switching probabilities is described in Hack et al. [Ref. 4 in Section XV]. This option is used for all the electronically nonadiabatic methods except for the semiclassical Ehrenfest (SE) method, which does not use hopping or switching probabilities. The user supplies an initial step size (in fs) and an algorithmic tolerance (in atomic units). A value of 10^{-7} for the integrator tolerance is recommended as an initial guess. For serious production runs, this value should be optimized with respect to both CPU time and conservation of total energy and total angular momentum. This is the only method recommended for electronically nonadiabatic calculations.

BULSTOINT: The Bulirsch-Stoer method with adaptive step size. For more than one potential surface, this keyword activates an approximate method for calculation of hopping/switching probabilities.

Use of this option is only recommended for single-surface calculations and the semiclassical Ehrenfest method for nonadiabatic processes. In electronically nonadiabatic calculations this scheme typically requires a very small value of the integrator tolerance and convergence is not guaranteed. Therefore, if used for nonadiabatic calculations it should be used only for testing and debugging purposes or not at all.

RUNKUT4: The 4th order Runge-Kutta method with fixed step size. See *Numerical Recipes* for details [Ref. 2 in Section XV]. The user supplies a step size (in fs).

VERLET0: The simple Verlet integrator.

VVERLET: The velocity Verlet integrator.

BEEMAN: The Beeman integrator.

LIUVILLE: The Liouville approach to the velocity Verlet integrator, which can be coupled with Nosé-Hoover (NH) thermostat.

VI. Non-Born-Oppenheimer trajectory methods

Input keywords presented in this section: ADIABATIC, DIABATIC, METHFLAG.

For systems where multiple potential energy surfaces and their couplings are available, non-Born–Oppenheimer (non-BO) trajectory methods may be used. (We note that for curvature-driven algorithms are not needed when nonadiabatic couplings are available.) Non-Born–Oppenheimer trajectories involve electronic and nuclear motions. All of the non-BO methods are coded in terms of the electronic wave function (rather than the electronic density matrix). The coefficients of the electronic wave functions are propagated along the classical trajectory as the solution to the classical path electronic Schrödinger equation. The details of the non-Born–Oppenheimer methods in *ANT* are described in Ref. 30, which is a book chapter that summarizes many details from the original publications in a single place and also presents a few details that were not previously published. All details needed to carry out CSDM calculations are available in that chapter.

Either the adiabatic or diabatic electronic representation may be used. The input keywords ADIABATIC (default) and DIABATIC are used to select which set of potential energy surfaces (adiabatic or diabatic) to use for setting up the initial conditions and for propagating the nuclear and electronic variables. For curvature-driven coherent switching with decay of mixing, only adiabatic representation should be used.

Note: The classical path equations for the electronic state populations neglect the “kinetic energy” nonadiabatic coupling term. In this formulation, the adiabatic and diabatic representations are equivalent (for a given nuclear trajectory) for two electronic states only.

ADIABATIC: Adiabatic representation (default).

DIABATIC: Diabatic representation.

The specific non-BO algorithm is selected using the input keyword METHFLAG.

METHFLAG=0: Single-surface propagation.

METHFLAG=1: Tully’s fewest switches (FS) method.

See Ref. 5 in Section XV, for a discussion of the FS method. Frustrated hops are ignored.

METHFLAG=2: Semiclassical Ehrenfest (SE) method.

Note: The final state analysis for the vibrational action does not work properly for this method. The code assumes that the system is in a single electronic state, which is not, in general, the case for this method. Only the vibrational action is affected.

See Ref. 6 in Section XV, for a discussion of the SE method.

METHFLAG=3: Self-consistent decay of mixing (SCDM) method.

The decay of mixing time is computed with $E_0 = 0.1 E_h$ and $C = 1$.
See Ref. 6 in Section XV, for a discussion of the SCDM method.

METHFLAG=4: Coherent switching with decay of mixing (CSDM) method.

The decay of mixing time is computed with $E_0 = 0.1 E_h$ and $C = 1$ as default.

See Ref. 6 in Section XV, for the description of the CSDM method.

METHFLAG=5: Fewest switches with time uncertainty (FSTU) method.

METHFLAG=6: Curvature-driven coherent switching with decay of mixing (κ CSDM) method.

The decay of mixing time is computed with $E_0 = 0.1 E_h$ and $C = 1$ as default. And the nuclear equation of motion is propagated with effective nonadiabatic coupling vector.

See Refs. 36 and 37 in Section XV, for the description of the κ CSDM method and effective nonadiabatic coupling vector.

METHFLAG=7: Curvature-driven coherent switching with decay of mixing (κ CSDM) method.

The decay of mixing time is computed with $E_0 = 0.1 E_h$ and $C = 1$ as default. And the nuclear equation of motion is propagated with nonadiabatic coupling vector.

See Ref. 8 in Section XV, for a discussion of the FSTU method. Frustrated hops can be ignored, reflected, or treated using the gradV method. See Ref. 9 in Section XV, for a discussion of the gradV method.

Note 1: The stochastic decoherence (SD) scheme (see Refs. 10, 11, and 14 in Section XV) can be used with either FSTU or FS. Its use is recommended in combination with FSTU (FSTU/SD method). Usage of SD is activated setting 'STODECOFLAG=1' in the \$surface input deck. See Section XII below.

Note 2: The TRAPZ (TRAjectory Projection onto ZPE orbit), mTRAPZ (minimal TRAPZ), and mTRAPZ* methods can be used to impose ZPE maintenance during surface-hopping simulations (FS, FSTU, and FSTU/SD methods). These three methods may also be used in combination with initial normal mode analysis obtained from a projected or an unprojected Hessian. Calls of these methods as well as calls of projected or unprojected Hessians are controlled by the keyword 'NTRAPZ=0, 1, 2, or 3' in the \$SURFACE input deck. See Section XII below. For a description of the TRAPZ, mTRAPZ, and mTRAPZ* methods see Refs. 12, 13, and 14 in Section XV, and for a description of the Projected Hessian algorithm see Ref. 16 in Section XV.

VII. The TRAPZ and mTRAPZ methods for maintaining zero-point energy

The mTRAPZ (minimal TRAPZ) method is an improvement of the TRAPZ (Trajectory Projection onto ZPE orbit) method. The mTRAPZ method ensures local zero-point energy (ZPE) maintenance during semiclassical simulations. The implementation of the method is based on Refs. 12, 13, and 14 in Section XV, especially on the third article in which the mTRAPZ algorithm is applied to a photoreactive molecular system, *i.e.*, NH₃.

VII.A. Description of the TRAPZ method

In what follows, the local number of atoms is denoted NATOMS2.

The TRAPZ method involves seven steps:

1. Calculation of mass-scaled coordinates and momenta [PMS(3*NATOMS2)] according to

$$\tilde{x}_J = \sqrt{\frac{m_j}{\mu}} x_{ij}^c$$

$$\tilde{p}_J = \sqrt{\frac{\mu}{m_j}} p_{ij}^c$$

where J is defined as $3(j-1)+i$, x^c and p^c are Cartesian coordinates and linear momenta.

2. Mass-scaled coordinates are used to determine the instantaneous projected Hessian. Diagonalizing this Hessian matrix allows one to determine the instantaneous frequency of each mode k , denoted Ω_k [FREQ2(3*NATOMS2)], as well as the instantaneous normal modes L_k [NMVEC2(3*NATOMS2, 3*NATOMS2)]. See Refs. 14 and 16 for more details about this point.

3. Determination of the mass-scaled vector of first derivatives [FMOD(3*NATOMS2)] according to

$$f_J = \sqrt{\frac{\mu}{m_j}} \frac{dV}{dx_{ij}^c}$$

where J is defined as $3(j-1)+i$, and x^c are Cartesian unscaled coordinates.

4. Calculation of the instantaneous vibrational energy E_k [EMOD(3*NATOMS2-6) or EMOD(3*NATOMS2-5)] for each mode k at the current time t_0 as follows

$$E_k(t_0) = \frac{1}{2\mu} \left[P_k^2 + \left(\frac{D_k(t_0)}{\Omega_k(t_0)} \right)^2 \right]$$

where

$$P_k = \sum_{j=1}^{3N} L_p^{jk}(t_0) \tilde{p}_j [\text{PMOD}(3*\text{NATOMS2})]$$

and

$$D_k = \sum_{j=1}^{3N} L_p^{jk}(t_0) f_j [\text{DMOD}(3*\text{NATOMS2})],$$

In the rest of the explanation, we assume that the molecule is not linear. Therefore, there are, at most, $3N - 6$ real positive frequencies. In general, some frequencies may be imaginary and there are only $3N - q(t_0)$ real positive frequencies, with $q(t_0) \geq 6$.

5. If $E_k(t_0) < \frac{1}{2} \hbar \Omega_k(t_0)$ then

$$P'_k = \text{sign}(P_k) \sqrt{\mu \hbar \Omega_k(t_0) - \left(\frac{D_k(t_0)}{\Omega_k(t_0)} \right)^2} [\text{PMODP}(3*\text{NATOMS2})]$$

Otherwise,

$$V'_k = \beta V_k$$

with

$$\beta = \sqrt{\frac{\sum_{k=1}^{3N-q(t_0)} P_k^2 - \sum_{k=1}^{n(t_0)} P_k'^2}{\sum_{k=n(t_0)+1}^{3N-q(t_0)} P_k^2}},$$

where $n(t_0)$ is the number of modes that violate the ZPE maintenance.

Remark: if β is not real then

$$V'_k = \gamma V_k,$$

with

$$\gamma = \sqrt{\frac{\sum_{k=1}^{3N-q(t_0)} P_k^2}{\sum_{k=1}^{n(t_0)} P_k^2}},$$

when $E_k(t_0) < \frac{1}{2} \hbar \Omega_k(t_0)$ and $P'_k = 0$ otherwise.

6. After determining P' we build new mass-scaled momenta [PNEW(3*NATOMS2)] according to

$$p_k^{new} = \sum_{j=1}^{3N-q(t_0)} L_p^{kj}(t_0) P_j' + \sum_{j=3N-q(t_0)+1}^{3N} \sum_{i=1}^{3N} L_p^{kj} L_p^{ij} P_i$$

The first term corresponds to the contribution of modified momenta, and the second term is the translational and rotational contribution (this last contribution should be zero when working in the center-of-mass frame without overall rotation, $J = 0$).

7. We then reverse the mass-scaling to get new Cartesian linear momenta [PPM(3,NATOMS2)]

$$p_{ij}^{c,new} = \sqrt{\frac{m_j}{\mu}} P_J^{new}$$

where J is defined as $3(j-1)+i$, and $p^{c,new}$ are the new Cartesian linear momenta.

VII.B. The mTRAPZ method

The TRAPZ method is applied whenever the instantaneous vibrational energy of any mode drops below its local ZPE. This criterion was found to be too restrictive and to lead to unphysical results for ammonia. A better choice consists in applying momenta transformations when the *total* instantaneous vibrational energy drops below the *total* local ZPE (mTRAPZ method) or the *total* local product ZPE (mTRAPZ* method). These methods were shown to give much better results (see Ref. 14).

VII.C. Problems with TRAPZ-like methods

Several problems were brought to light when applying the TRAPZ-like methods:

- a) The center-of-mass location and linear momentum were not properly conserved during the dynamics. This is, at least partly, due to the limited accuracy of the eigenvectors that are used to generate the new momenta. The RMVCOM subroutine is used at each time step to alleviate this issue.
- b) The projected Hessian seemed not to be properly calculated at some NH₃ geometries. This is the consequence of using Cartesian coordinates. True rotational motions have to be expressed in curvilinear rather than Cartesian coordinates. The unphysical nature of Cartesian rotational eigenvectors is directly transmitted to the projected Hessian. However, discarding all these geometries is impractical and we have thus decided to apply TRAPZ-like methods only when the number of modes is above $3N-6$ (resp. $3N-5$) for nonlinear geometries (resp. linear geometries). On the one hand, this criterion does not corrupt the ZPE maintenance at all and, on the other hand, it has the advantage to significantly remove the problems concerning the total angular momentum (see Ref. 29). We have indeed noticed (see Ref. **Error! Reference source not found.**) that the total angular momentum was not well conserved for some trajectories (always below 1-2 %) when trying to discard all the geometries for which the projected Hessian was not properly determined, certainly because of the impossibility to remove all these geometries.

VIII. Army ants tunneling algorithm

The present version of *ANT* contains the army ants tunneling algorithm for use either in single-surface (i.e., electronically adiabatic) trajectories or nonadiabatic trajectories of unimolecular processes (including unimolecular dissociation). For nonadiabatic processes, army ant tunneling algorithm is only implemented for the mean-field methods, not for surface-hopping methods. This algorithm is explained in

"Army Ants Tunneling for Classical Simulations," J. Zheng, X. Xu, R. Meana-Pañeda, and D. G. Truhlar, *Chemical Science* 5, 2091-2099 (2014).

"Including Tunneling in Non-Born-Oppenheimer Simulations," J. Zheng, R. Meana-Pañeda, and D. G. Truhlar, *Journal of Physical Chemistry Letters* 5, 2039-2043 (2014).

These are Refs. 31 and 32 in Section XV.

VIII.A. Computation of the turning point

Let \mathbf{x} be a vector whose components are the $3N$ Cartesian coordinates of the system. Note: in other sections of this manual, N is often called N_{atom} .

The trajectory is monitored at every integration step to see if it reaches a turning point of the tunneling coordinate (coordinate i), where that coordinate reaches a maximum or minimum, i.e., where $\mathbf{p} \cdot \mathbf{d}_1$ is zero, where \mathbf{p} is the momentum and \mathbf{d}_1 is the unit vector along the tunneling direction; both \mathbf{p} and \mathbf{d}_1 are in $3N$ -dimensional (unscaled) Cartesian coordinates.

To find these turning points the code uses one of these two criteria:

- i) the value of the product $\mathbf{p} \cdot \mathbf{d}_1$ is very small, or
- ii) the value of $\mathbf{p} \cdot \mathbf{d}_1$ has changed sign from the previous step to the current one.

In the latter case we re-integrate from the previous step with a smaller time step to find the turning point more precisely.

Note that \mathbf{d}_1 depends on \mathbf{x}_0 and \mathbf{x}_1 , where \mathbf{x}_0 is the geometry of the turning point in Cartesian coordinates, and \mathbf{x}_1 is a new geometry in the tunneling direction. The unit vector \mathbf{d}_1 defines the initial direction of the tunneling in Cartesian coordinates, and it is computed as the difference between two geometries along the tunneling path:

$$\mathbf{d}_1 = \frac{(\mathbf{x}_1 - \mathbf{x}_0)}{|\mathbf{x}_1 - \mathbf{x}_0|} \quad (1)$$

The geometry \mathbf{x}_1 is obtained by the following procedure:

1. Evaluate of the internal coordinates q_0 of the turning point.
2. Compute the internal-coordinate displacement vector

$$\Delta \mathbf{q}_1 = \mathbf{q}_1 - \mathbf{q}_0 \quad (2)$$

where all elements are zero except a small displacement ζ associated with the internal coordinate i . Because \mathbf{d}_1 is a Cartesian coordinate, the displacement of internal coordinate $\Delta \mathbf{q}_1$ should be small enough.

3. Calculate Wilson's B and A matrices. Wilson's A matrix is the generalized inverse of the B matrix

$$\mathbf{A} = \mathbf{UB}^T (\mathbf{BUB}^T)^{-1} \quad (3)$$

where in principle U is *any* nonsingular $3N$ by $3N$ matrix (with N being the number of nuclei), but we take U as a diagonal matrix with the reciprocals of the atomic masses as the diagonal elements. Note that B and A depend on the coordinates, and for the first iteration they are evaluated at the turning point.

4. The first order equation

$$\mathbf{x}_1 = \mathbf{x}_0 + \mathbf{A}(\mathbf{q}_1 - \mathbf{q}_0) \quad (4)$$

provides the Cartesian coordinates of x_1 . This equation is solved iteratively where the A matrix is updated at each iteration until the geometry x_1 converges.

VIII.B. Evaluation of the imaginary action integral for electronically adiabatic tunneling path

When a turning point is found the next step is to evaluate the value of the imaginary action integral. We present two algorithms below, and only the general algorithm is implemented in the current *ANT* code for electronically adiabatic tunneling path.

VIII.B.1. Algorithm for the case in which the tunneling coordinate is a bond stretch

This first method only works when the tunneling coordinate is a single stretching coordinate. The reason that this case is simpler is that the tunneling path is a straight line in both internal coordinate and isoinertial coordinates.

All geometries of the trajectory along the tunneling path are computed by

$$\mathbf{x} = \mathbf{x}_0 + \xi \mathbf{d} \quad (5)$$

where ξ is the distance along the path from \mathbf{x}_0 to \mathbf{x} , and \mathbf{d} is the tunneling direction along a bond. New geometries are calculated until the difference of the potential with respect to the energy of the turning point,

$$\Delta V = V(\mathbf{x}_0 + \xi \mathbf{d}) - V(\mathbf{x}_0) \quad (6)$$

becomes negative (i.e. it is zero at the beginning of the tunneling path, then positive, then comes back to zero at the end of the tunneling path and then is negative). To search the value ξ_{\max} at which $\Delta V = 0$ we use the bisection method starting from the first point where $\Delta V < 0$ and the last point where $\Delta V > 0$.

The geometry of the turning point at the end of the tunneling path in Cartesian coordinates is given by

$$\mathbf{x}_{\text{end}} = \mathbf{x}_0 + \xi_{\max} \mathbf{d} \quad (7)$$

Both geometries \mathbf{x}_0 and \mathbf{x}_{end} may be converted to isoinertial coordinates by

$$\tilde{\mathbf{x}} = \mathbf{m}^{1/2} \mathbf{x} / \mu^{1/2} \quad (8)$$

where we have defined coordinates \mathbf{x} and distances ξ without a tilde as being in Cartesian coordinates, and $\tilde{\mathbf{x}}$ and $\tilde{\xi}$ with a tilde will denote coordinates and distances in isoinertial coordinates. Note that isoinertial coordinates may also be called mass-scaled coordinates, and we will use the fact that the isoinertial coordinate system has the same reduced mass μ in all directions of $3N$ -dimensional space. For the present case where the tunneling coordinate is a single bond stretch, the distance along the tunneling path in isoinertial coordinates is

$$\tilde{\xi}_{\max} = \left| \tilde{\mathbf{x}}_{\text{end}} - \tilde{\mathbf{x}}_0 \right| \quad (9)$$

and the direction of the tunneling path in isoinertial coordinates is

$$\mathbf{d} = \frac{(\tilde{\mathbf{x}} - \tilde{\mathbf{x}}_0)}{|\tilde{\mathbf{x}} - \tilde{\mathbf{x}}_0|} \quad (10)$$

With these definitions, we can compute the imaginary action integral

$$\theta = \frac{1}{\hbar} \int_0^{\tilde{\xi}_{\max}} \sqrt{2\mu \left[V(\tilde{\mathbf{x}}_0 + \tilde{\xi} \mathbf{d}) - V(\tilde{\mathbf{x}}_0) \right]} d\tilde{\xi} \quad (11)$$

using the Gauss-Legendre method.

VIII.B.2. General Algorithm

This is a general method and it works for when the tunneling coordinate is any internal coordinate or any linear combination of internal coordinates. Note that in the general case, when a tunneling path is along an internal coordinate, it is not a straight line in either Cartesian coordinates or isoinertial coordinates.

The imaginary action integral is calculated by

$$\theta = \frac{1}{\hbar} \int_0^{\tilde{\xi}_{\max}} \sqrt{2\mu [V(\tilde{\mathbf{x}}) - V(\tilde{\mathbf{x}}_0)]} d\tilde{\xi} \quad (12)$$

where the $\tilde{\xi}$ is the arc length of position $\tilde{\mathbf{x}}$ from the starting point $\tilde{\mathbf{x}}_0$ of the tunneling path. Before calculating a tunneling path, its length $\tilde{\xi}_{\max}$ is unknown. To compute the imaginary action integral we need to calculate the length of tunneling path and to calculate the geometry and potential at given quadrature nodes $\tilde{\mathbf{x}}$. We accomplish this by a sequence of two steps:

Step 1: First we predefine a long enough tunneling path (this path should be longer than any actual tunneling path we expect to encounter) and divide this predefined path into segments. The potential energy of the end point of each segment relative to the starting point of the tunneling path is calculated, and if the relative potential energy is positive, the segment should be fully included in the real tunneling path; if segment M is the first segment whose end point has negative energy, a small step (for example, 10^{-3} bohr for bond length and 0.1 degree for torsion angle) is used to search the precise ending point of the tunneling path. Note that the Cartesian coordinates for any point along tunneling path are calculated by using Wilson's A matrix iteratively.

Step 2: To calculate the distances $\tilde{\xi}_i$ of points i from the start of a curved path in isoinertial coordinates, an evenly spaced fine grid is created in internal coordinates along the tunneling path, and the distance ξ_i^{int} in internal coordinates is calculated for each grid point. Then $\tilde{\xi}_i$ in isoinertial coordinates is approximated as a sum of small chord lengths, i.e. $\tilde{\xi}_i = \sum_{j=1}^i |\tilde{\mathbf{x}}_j - \tilde{\mathbf{x}}_{j-1}|$. Gauss-Legendre quadrature is applied to the whole

tunneling path. For a given Gauss-Legendre node $\tilde{\xi}_k$ that falls between $\tilde{\xi}_i$ and $\tilde{\xi}_{i-1}$, we use linear interpolation to calculate the corresponding length in internal coordinate ξ_k^{int} ,

$$\text{i.e., } \xi_k^{\text{int}} = \frac{(\tilde{\xi}_k - \tilde{\xi}_{i-1})\xi_i^{\text{int}} + (\tilde{\xi}_i - \tilde{\xi}_k)\xi_{i-1}^{\text{int}}}{\tilde{\xi}_i - \tilde{\xi}_{i-1}}. \text{ Once the } \xi_k^{\text{int}} \text{ is known, the Cartesian}$$

coordinates of node k are calculated using Wilson's A matrix iteratively, and then the potential energy is calculated for that Cartesian geometry.

VIII.C. Evaluation of the imaginary action integral for electronically nonadiabatic tunneling path

In mean-field and decay-of-mixing methods, the nuclear motion is governed by an effective potential \bar{V} , which is a function not only of nuclear position \mathbf{q} but also of the coefficients c_i in the expansion of the multi-configurational electronic wave function in terms of either adiabatic or diabatic states. When propagating trajectory along a nonadiabatic tunneling path, we assume electronic wave functions are fully coherent, i.e. semiclassical Ehrenfest (SE) method is used that is independent with the method used to propagating trajectories in classical allowed region. The new issue is that we need to convert the time derivatives \dot{c}_i of the SE electronic wave function coefficients to their rate of change along the tunneling path, which requires assigning a time to each point on the tunneling path.

The WKB approximation is used to resolve the question of traversal time for a tunneling particle, which gives traversal time for tunneling of a particle with mass μ

$$\Delta t = \frac{\Delta \xi}{\sqrt{2(V - V_0) / \mu}} \quad (13)$$

where ξ is again the distance along the tunneling path in isoinertial coordinates scaled to mass μ , V is the potential energy at $\Delta \xi$ in the tunneling path, and V_0 is the energy of the turning point. Then it yields

$$\frac{dc_i}{d\xi} = \frac{\dot{c}_i}{\sqrt{2(\bar{V}(\mathbf{q}) - \bar{V}(\mathbf{q}_0)) / \mu}} \quad (14)$$

Since we have to propagate both tunneling coordinates and electronic coefficients at the same time, the Gauss-Legendre quadrature cannot be applied in nonadiabatic tunneling path. Instead, we use the Trapezoidal rule integral for imaginary action integral by taking small step size, e.g. 10^{-3} bohr for $\Delta \xi$. For each step, the electronic coefficients are integrated by using the 4th order of Runge-Kutta method.

VIII.D. Army ants algorithm for branching

The tunneling probability is $P_t = e^{-2\theta}$. When a tunneling probability P_t is calculated for a possible tunneling path, one computes $\gamma = \max(\eta, P_t)$ where η is a parameter (taken here as 0.95 as the default, but it can be changed by the user with the keyword ETA in the \$TUNNELING section), and picks a random number λ_1 .

If $\lambda_1 > \gamma$, there is no tunneling, and the classical trajectory continues with unit weight. If $\lambda_1 < \gamma$, one picks another random number λ_2 , and if $\lambda_2 > 0.5$, there is still no tunneling, but the weight of the trajectory is decreased by a factor $2(1 - P_t/\gamma)$. However if $\lambda_2 < 0.5$, one accepts the tunneling path and weights it $2P_t/\gamma$. Consequently we follow tunneling events about half the time, but they are weighted to ensure that the result

converges to the same probability of tunneling as in the anteatr method. Since, very often, $P_t \ll 0.5$, the statistics on tunneling events are greatly improved, and we can efficiently explore regions of space reached only by tunneling.

To conserve total angular momentum and total energy at the end of the tunneling path, the final atomic momenta are adjusted to satisfy

$$\sum_{i=1}^N \mathbf{x}'_i \times \mathbf{p}'_i = \sum_{i=1}^N \mathbf{x}_{0,i} \times \mathbf{p}_{0,i} \quad (15)$$

$$|\mathbf{p}'_i| = |\mathbf{p}_{0,i}| \quad i = 1, \dots, N \quad (16)$$

where $\mathbf{x}_{0,i}$ and $\mathbf{p}_{0,i}$ denote respectively the initial position vector of atom i in the unscaled Cartesian coordinates and the initial momentum of atom i . The primed variables in eqs. 15 and 16 denote the same quantities as $\mathbf{x}_{0,i}$ and $\mathbf{p}_{0,i}$ but at the end of the tunneling step. The adjustment is accomplished as follows. The total angular momentum \mathbf{J} , which must be conserved, is

$$\mathbf{J} = \sum_{i=1}^N \mathbf{x}_i \times \mathbf{p}_i \quad (17)$$

where \mathbf{x}_i can be $\mathbf{x}_{0,i}$ or \mathbf{x}'_i and where \mathbf{p}_i can be $\mathbf{p}_{0,i}$ or \mathbf{p}'_i . The change of Cartesian coordinates for atom i along the whole tunneling path is $\Delta \mathbf{x}_i$ so that

$$\mathbf{x}'_i = \mathbf{x}_{0,i} + \Delta \mathbf{x}_i \quad i = 1, \dots, N \quad (18)$$

Equation 16 conserves the magnitudes of the atomic momenta, but not their directions. We denote the initial and final atomic momenta as

$$\mathbf{p}_{0,i} = |\mathbf{p}_{0,i}| \mathbf{u}_{0,i} = p_{0,i} \mathbf{u}_{0,i} \quad i = 1, \dots, N \quad (19)$$

$$\mathbf{p}'_i = |\mathbf{p}_{0,i}| \mathbf{u}'_i = p_{0,i} \mathbf{u}'_i \quad i = 1, \dots, N \quad (20)$$

where we have used eq. 16, and where $\mathbf{u}_{0,i}$ and \mathbf{u}'_i are unit vectors. We choose to minimize the changes in direction subject to the constraints of eqs. 15 and 16. Thus we minimize the quantity

$$\begin{aligned} f &= \sum_{i=1}^N |\mathbf{u}_{0,i} - \mathbf{u}'_i|^2 \\ &= \sum_{i=1}^N \sum_{\gamma=x,y,z} (u_{0,i\gamma} - u'_{i\gamma})^2 \end{aligned} \quad (21)$$

subject to the constraint of eq. 15. Note that $u_{0,i\gamma}$ and $u'_{i\gamma}$ are direction cosines. Adding three Lagrange multipliers ($\lambda_i, i=1,2,3$) to enforce the constraint gives a new objective function:

$$\begin{aligned}
g = \sum_i \sum_{\gamma=x,y,z} (u_{0,i\gamma} - u'_{i\gamma})^2 + \lambda_1 \left[J_x - \sum_i p_{0,i} (x'_{iy} u'_{iz} - x'_{iz} u'_{iy}) \right] \\
+ \lambda_2 \left[J_y - \sum_i p_{0,i} (x'_{iz} u'_{ix} - x'_{ix} u'_{iz}) \right] + \lambda_3 \left[J_z - \sum_i p_{0,i} (x'_{ix} u'_{iy} - x'_{iy} u'_{ix}) \right]
\end{aligned} \tag{22}$$

Then we combine all the final direction cosines into a single algebraic vector:

$$v_1 = u'_{1x}, v_2 = u'_{1y}, v_3 = u'_{1z}, v_4 = u'_{2x}, \text{ etc.} \tag{23}$$

Then the equations to be solved for the final direction cosines $u'_{i\gamma}$ are

$$\frac{\partial g}{\partial v_j} = 0, \quad j = 1, \dots, 3N \tag{24}$$

$$\frac{\partial g}{\partial \lambda_k} = 0, \quad k = 1, 2, 3 \tag{25}$$

Equations 24 and 25 constitute $3N + 3$ nonlinear equations, and they can be solved iteratively by the Newton-Raphson method for the $3N$ component of \mathbf{V} and the three components of λ . Using the resulting \mathbf{V} along with eqs. 20 and 23, one obtains the momentum components after the tunneling event.

IX. Special options

IX.A. TFLAG1 options

Special options are indicated using keywords TFLAG1. The following options are supported.

TFLAG1=0: No special options (default).

TFLAG1=1: Steepest-descent minimization.
The momenta are zeroed at every step.

TFLAG1=2: Momentum ramping.
After each interval of N_RAMP + NEQUILRAMP steps, the momenta are scaled by a factor of RAMPFACT. The momenta are scaled NRAMP times before the trajectory ends. When this option is selected, unit 40 is written, which records information between rescalings. The time is reset at each temperature rescaling.

TFLAG1=3: Simulated annealing (heating/cooling).
After each interval of N_RAMP + NEQUILRAMP steps, the temperature is changed by RAMPFACT K. The temperatures are changed NRAMP times before the trajectory ends. When this option is selected, unit 40 is written, which records information between temperature changes. The time is reset at each temperature changes.

TFLAG1=4: Same as TFLAG1=3 except the program will do an extra geometry optimization using the BFGS method when the heating/cooling ends.

TFLAG1=5: Same as TFLAG1=3 except the program will do extra geometry optimizations at intermediate steps using the BFGS method: at each step the program will generate a uniformly distributed random number (0-1), if it is smaller than or equal to PICKTHR, a geometry optimization is performed. The program will save the optimized geometries in file unit 28 and print out the lowest energy structure at the end of the trajectory. This is designed to search for global minimum using a simulated annealing method.

IX.B. Starting trajectories at a saddle point

Another option in the code is that one may start trajectories at a rectilinear hypersurface that passes through saddle point and is normal to the imaginary-frequency normal mode. This kind of calculation may be run for various purposes, for example, for calculations by the trajectory method of Anderson [33] or for calculations by the unified dynamical theory [34].

This type of calculation is selected by setting VIBTYPE=1. The user must provide the geometry of a first order saddle point. The quasiclassical initial conditions scheme discussed in section IV is used for the $3N-7$ (or $3N-6$ for a linear molecule) bound degrees of freedom. The remaining internal degree of freedom is associated with the imaginary frequency and with the local reaction coordinate. The user may choose to add energy along

this degree of freedom. The initial coordinate in the unbound direction is not displaced from its saddle point value. See the keywords VIBTYPE and VIBSTATES for details.

X. Final-state analysis routines

A small selection of final-state analysis routines is provided in the analysis/ subdirectory. A brief description is given here.

ANT30.pl Analyzes fort.30, which contains information for the atom–diatom scattering. Computes average probabilities, rovibrational moments (using histogramming), and internal energies.

minE.pl For use with the steepest-descent option (INITp = 0). Analyzes unit 20 and prints the energy, the number of times this energy was obtained during the entire simulation, and the geometry of the minimum-energy structure.

raddist.pl Computes the radial distribution function RDF from unit 10 or unit 20, averaged over all of the structures. Execute using

analysis/raddist.pl FILE N

where FILE is the output file to be analyzed and N is the number of particles. Output is the bin number i , value of the radial distance at the center of the bin R_i , and value of the RDF for that bin. The code counts bonds for each bin and normalizes each bin by dividing by $N_{\text{struct}} N_{\text{atom}} 4\pi R_i^2 dR$, where N_{struct} is the number of structures, N_{atom} is the number of atoms, and dR is the width of the bin.

cn.pl Computes coordination number information from unit 10 or unit 20. Execute using

analysis/cn.pl FILE N

where FILE is the output file to be analyzed and N is the number of particles. The code produces the following information for each structure: Structure number, energy per atom in eV, diameter (defined as the largest atom-atom distance) in Å, average coordination number, number of interior atoms (defined as having a distance from the origin less than some number), average coordination number for the interior atoms, and a list of the number of atoms in the structure with each coordination number. The parameter that is used to count neighbors (RNN) and the interior atom cutoff distance (RCUT) are hard-coded as 2.4 and 5 Å, respectively. Structures are sorted by energy.

treat.tar.gz Gathers several scripts and codes (in fortran 77) to treat data (Generated directory: TREAT-DATA/). This suite of codes aims at providing the user with some basic tools to (i) concatenate several batches of trajectories, (ii) extract some information from the ANT08 output file, and (iii) plot

distributions by using the moment method based on Legendre polynomials. A description of the content of this directory is indicated in the README.txt file located in TREAT-DATA/.

phenol_FinalStateAnaly.tgz

This a collection of all scripts and codes to do the final state analysis for phenol photodissociation trajectories. The detailed explanation of each code is written in the beginning of each script/code.

XI. Installation, compilation, and compatibility

ANT is distributed as a tar.gz file, which may be untarred by executing

```
tar -zxvf ANT.tar.gz
```

Before running test runs it is advisable to check that the distribution is complete. The next section provides details of the contents of the directories provided.

XI.A. Content of the *ANT* distribution

The *ANT* distribution contains the following directories:

analysis/	A collection of analysis routines.
doc/	Contains five documents: <ul style="list-style-type: none"> • <i>ANT 2023</i> manual for users • revision_history.txt for developers • developmentnote.txt for developers • C82.pdf, which is a copy of "Reactive Scattering Cross Sections: Quasiclassical and Semiclassical Methods," D. G. Truhlar and J. T. Muckerman, in <i>Atom-Molecule Collision Theory: A Guide for the Experimentalist</i>, edited by R. B. Bernstein (Plenum Press, New York, 1979), pp. 505-566. • C828including-corrections.pdf, which is a copy of "Non-Born-Oppenheimer Molecular Dynamics for Conical Intersections, Avoided Crossings, and Weak Interactions," A. W. Jasper and D. G. Truhlar, in <i>Conical Intersections: Theory, Computation, and Experiment</i>, edited by W. Domcke, D. R. Yarkony, and H. Köppel (World Scientific, Singapore, 2011), pp. 375-412.
exe/	Initially empty; contains executables when they are compiled.
mopac_src/	Initially empty; contains <i>MOPAC-mn</i> source code for direct dynamics, which needs to be obtained separately.
pot/	Contains potential energy subroutines needed of the analytic potential test runs.
sprng/	SPRNG random number generator routines
sprng2.0/	SPRNG random number generator routines
src/	Source code and Makefile
tests_bimol/	Sample input and output files for bimolecular test runs using analytic potential energy surfaces
tests_unimol/	Sample input and output files for unimolecular test runs using analytic potential energy surfaces

tests_dd/

Sample input and output files for direct dynamics

Directory	Contents of the directory
analysis/	6 files: ANT30.pl, cn.pl, lowE.pl, raddist.pl, treat.tar.gz, phenol_FinalStateAnaly.tgz
doc/	3 files: ANT2023-Manual.pdf developmentnote.txt revision_history.txt
exe/	Initially empty
mopac_src/	Initially empty
pot/	44 files: BrCH2Cl-openmp.for BrCH2Cl-openmp.for-original CH2BrClpotders.f CH2BrClpotders.f-NEW CH2BrClpotders.f-original dd.f ER2d.f HalPd.f HBrpot.f HN2.f hoco.f HX2ad.f HX2exb.f HX2OH.f LiFHJ.f MCH_SB.f MCH_TL.f N2O-3Ap-gpip.f N2O-3App-gpip.f n4pes-gpip-v2_edited.f nh3potg.f nh3potg-new.f nh3potnocg.f nh3-zy.f NP-Ad.f NP-Ad-li.f NP-Ad-p.f NP-Bd.f NP-Bd-p.f NP-Bd-v3.f NP-Bd-v3-openmp.for o3_q.f90 o3_t.f90 oh3.f oh3_3state.f90 phoh_aprp.f phsch3.f90 potmopac.f reGold.f tb101AJ.f tb101AJ_Nate.f tb101WM.f VBO-al-del13.f yrh_0.2.f
sprng/	54 files: CHANGES.TEXT, Makefile, README, VERSION, check.ccmrg, check.clcg, check.clcg64, check.clfg, check.cmlfg, check.fcmrg, check.flcg, check.flcg64, check.flfg, check.fmlfg, check_ptr.ccmrg, check_ptr.clcg, check_ptr.clcg64, check_ptr.clfg, check_ptr.cmlfg, check_ptr.fcmrg, check_ptr.flcg, check_ptr.flcg64, check_ptr.flfg, check_ptr.fmlfg, check_sim.ccmrg, check_sim.clcg, check_sim.clcg64, check_sim.clfg, check_sim.cmlfg, check_sim.fcmrg, check_sim.flcg, check_sim.flcg64, check_sim.flfg, check_sim.fmlfg, checksprng, cmrg.data, lcg.data, lcg64.data, lfg.data, make.CHOICES, mlfg.data, sprng_f.h.all, sprng_f.h.i386, timecmrg, timefcmrg, timeflcg, timeflcg64, timeflfg, timefmlfg, timefcg, timefcg64, timefcfg, timefcfg64, timesprng 6 subdirectories: Doc/, Examples/, SRC/, TESTS/, include/, lib/

	<p>Doc/ (2 files): README, sprng.html.tar.Z</p> <p>EXAMPLES/ (47 files): 2streams_mpi.c, 2streamsf_mpi.F, Makefile, README, checkpoint-simple.c, checkpoint.c, checkpointf-simple.F, checkpointf.F, convert.c, convertf.F, displaybytes.c, fsprng-simple_mpi.c, fsprng_mpi.c, fsprngf-simple_mpi.F, fsprngf_mpi.F, invalid_ID.c, invalid_IDf.F, make.test, message-simple_mpi.c, message_mpi.c, messagef-simple_mpi.F, messagef_mpi.F, myrandom.c, pi-simple.c, pi-simple_mpi.c, pif-simple.F, seed-simple.c, seed-simple_mpi.c, seed.c, seed_mpi.c, seedf-simple.F, seedf-simple_mpi.F, seedf.F, seedf_mpi.F, simple-simple.c, simple-simple.F, spawn.c, spawnf.F, sprng-simple.c, sprng-simple_mpi.c, sprng.c, sprng_mpi.c, sprngf-simple.F, sprngf-simple_mpi.F, sprngf.F, sprngf_mpi.F, subroutenef.F</p> <p>SRC/ (50 files): Makefile, README, check_gen.c, check_gen_ptr.c, check_gen_simple.c, check_genf.F, check_genf_ptr.F, check_genf_simple.F, checkid.c, cmrg, communicate.c, cputime.c, cputime.h, drand.c, fwrap.h, fwrap_.h, fwrap_mpi.c, insertlib, interface.h, lcg, lcg64, lfg, make.CONVEX, make.DEC, make.GENERIC, make.HP, make.LINUX, make.O2K, make.SGI, make.SOLARIS, make.SP2, make.SUN, make.T3D, make.T3E, makeseed.c, memory.c, memory.h, mlfg, multiply.h, pmlcg, simple.c, simple_.h, simple_mpi.c, sprng.h, sprng_f.h, sprng_f_orig.h, store.c, store.h, timing.c, timingf.F</p> <p>TESTS/ (25 files): Makefile, NEWGEN.TEXT, README, chisquare.c, collisions.c, communicate.c, coupon.c, equidist.c, fft.c, gap.c, init_tests.c, maxt.c, metropolis.c, mytest.c, perm.c, poker.c, random_walk.c, runs.c, serial.c, stirling.c, sum.c, tests.h, util.c, util.h, wolff.c</p> <p>include/ (2 files): interface.h, sprng_f.h</p> <p>lib/ (6 files): Makefile, libcmrg.a, liblcmrg.a, liblcmrg64.a, liblcmrg.a, libmlfg.a</p>
sprng2.0/	<p>54 files: AGAINstub CHANGES.TEXT check.csprng check.fsprng check_ptr.csprng check_ptr.fsprng check_sim.csprng check_sim.fsprng checksprng gen0_lfg gen0_lfg.data gen1_lcg gen1_lcg.data gen2_lcg64 gen2_lcg64.data gen3_cmrg gen3_cmrg.data gen4_mlfg gen4_mlfg.data make.CHOICES Makefile README READMEEver2.CHANGES timesprng timingscsprng timingfsprng VERSION</p>

7 subdirectories: aa/, DOC/, EXAMPLES/, SRC/, TESTS/, include/, lib/

aa/ (4 files): simple-simple simple-simple.c sprngf sprngf.F

DOC/ (5 files): 1 new_sprng.ps new_sprng.ps.Z README sprng.html.tar.Z

EXAMPLES/ (75 files): 2streams_mpi.F 2streams_mpi.c Changes_in_EXAMPLES checkpoint checkpoint.c checkpointf checkpointf.F checkpointf-simple checkpointf-simple.F checkpoint-simple checkpoint-simple.c convert.c convertf.F displaybytes.c fsprngf_mpi.F fsprngf-simple_mpi.F fsprng_mpi.c fsprng-simple_mpi.c genf_types_header genf_types_menu.h gen_types_header gen_types_menu.h invalid_ID invalid_ID.c invalid_IDf invalid_IDf.F Makefile make.test messagef_mpi.F messagef-simple_mpi.F message_mpi.c message-simple_mpi.c myrandom.c pif-simple pif-simple.F pi-simple pi-simple.c pi-simple_mpi.c README seed seed.c seedf seedf.F seedf_mpi.F seedf-simple seedf-simple.F seedf-simple_mpi.F seed_mpi.c seed-simple seed-simple.c seed-simple_mpi.c simplef-simple simplef-simple.F simple-simple simple-simple.c spawn spawn.c spawnf spawnf.F sprng sprng.c sprngD sprngf sprngf.F sprngf_mpi.F sprngf-simple sprngf-simple.F sprngf-simple_mpi.F sprng_mpi.c sprng-simple sprng-simple.c sprng-simple_mpi.c store subroutinef.F tip

SRC/ (81 files): check_gen.c check_genf.F check_genf.o check_genf_ptr.F check_genf_ptr.o check_genf_simple.F check_genf_simple.o check_gen.o check_gen_ptr check_gen_ptr.c check_gen_ptr.o check_gen_simple check_gen_simple.c check_gen_simple.o checkid.c checkid.o cmrg communicate.c communicate.o cputime.c cputime.h cputime.o drand.c #fwrap_.h# fwrap_.h fwrap.h fwrap_mpi.c fwrap_mpi.o insertcheck insertlib insertmenu inserttimecheck interface.h lcg lcg64 lfg make.CONVEX make.DEC Makefile Makefile.old make.GENERIC make.HP make.INTEL make.O2K makeseed.c makeseed.o make.SGI make.SP2 make.SUN make.T3D make.T3E memory.c memory.h memory.o mlfg multiply.h pmlcg primelist_32.h primelist_64.h primes_32.c primes_32.h primes_32.o primes_64.c primes_64.h primes_64.o README READMEver2.CHANGES simple.c simple_.h simple_mpi.c simple_mpi.o sprng sprng_f.h sprng.h store.c store.h store.o timing.c timingf.F timingf.o timing.o

TESTS/ (58 files): chisquare.c chisquare.o collisions.c collisions.o collisions.sprng communicate.c communicate.o coupon.c coupon.o coupon.sprng equidist.c equidist.o equidist.sprng fft.c gap.c gap.o

	<p>gap.sprng init_tests.c init_tests.o Makefile Makefile.old maxt.c maxt.o maxt.sprng metropolis.c metropolis.o metropolis.sprng mytest.c NEWGEN.TEXT perm.c perm.o perm.sprng poker.c poker.o poker.sprng random_walk.c random_walk.o random_walk.sprng README READMEEver2.CHANGES runs.c runs.o runs.sprng serial.c serial.o serial.sprng stirling.c stirling.o sum.c sum.o sum.sprng tests.h util.c util.h util.o wolff.c wolff.o wolff.sprng</p> <p>include/ (4 files): d~ interface.h sprng_f.h sprng.h</p> <p>lib/ (4 files): libsprng.a libsprngtest.a Makefile Makefile~</p>
src/	<p>131 files: actionint.f90 actionint_nt.f90 adjpress.f90 adjtemp.f90 adtod.f90 amsol.h angmom.f90 ant.f90 arcom.f90 atomdata.f90 atomdiatom.f90 bmat.f90 brent.f90 bsstep.f90 cartojac.f90 c_dd.f90 c_diatom.f90 checkfrus.f90 checkhop.f90 c_initial.f90 c_mopac.f90 cnsvangmom.f90 comgen.f90 c_output.f90 c_struct.f90 c_sys.f90 c_term.f90 c_traj.f90 decocheck.f90 defaults.f90 derivs.f90 detmtbt.f90 diamin_max.f90 diapot.f90 diatom diatomdiatom.f90 dlaev2.f driver.f90 driverim.f90 elecdeco.f90 erotc.f90 ewkb2.f90 ewkb.f90 fileopen.f90 finalstate.f90 fragcom.f90 frag.f90 func.f90 gaussq.f gen_prt.f90 geom_opt.f90 gepol_mod.f gepol_unmod.f90 getdvec2.f90 getdvec.f90 getevibanh.f90 getgrad2.f90 getgrad.f90 getpem.f90 getpress.f90 getrhocsdm.f90 getrho.f90 gettemp.f90 hardwall.f90 header.f90 honey.f90 hop.f90 ifsames2.f90 ifsames.f90 initelec.f90 initmol.bad initmol.f90 initrot.f90 inittrans.f90 intcart.f90 intcoord.f90 integhop.f90 invmtbt.f90 lindemann.f90 liouville.f90 Makefile matprint.f90 mmid.f90 momigen.f90 noang.f90 nocompp.f90 normod.f90 normod-trapz.f90 obj_opt param.f90 period.f90 periodimage.f90 pjctmomen.f90 pjsplit.f90 popmod.f90 popnorm.f90 preatomdiatom.f90 prediatomdiatom.f90 premol.f90 projection.f90 pzextr.f90 qtrfit.f90 radialdist.f90 ranclucub.f90 rancluns.f90 ranclusp.f90 ranmolcub.f90 ranrot.f90 rantherm.f90 readin.f90 relenerg.f90 rijmatr.f90 rk4.f90 rminfrag.f90 rng_int.F90 rotmol.f90 rotprin.f90 rottran.f90 rttox.f90 setupvolume.f90 stodeco.f90 takestep2.f90 takestep.f90 trapz.f90 turn.f90 turnpt.f90 utility.f verlet.f90 volume_interface.f90 vwkb.f90 xptoy.f90</p> <p>obj_opt/ (empty)</p> <p>diatom/ (14 files): diatom_brent.f90, diatom_ewkb.f90, diatom_genjvstate.f90, diatom_getjvstate.f90, diatom_getm.f90, diatom_init.f90, diatom_jvprobs.f90, diatom_minmax.f90, diatom_param.f90, diatom_place.f90, diatom_pot.f90, diatom_tau.f90, diatom_turn.f90, diatom_vwkb.f90</p>

tests_bimol/	<p>22 files: A12-A12-rx-normod-400-1.0.in A12-A1-rx-normod-400-1.0.in A1-A159-rx-2000.in LiFH-SEa.in LiFH-SEd.in LiFH-u22.in LiFH-v1.in MCH-CSDMa.in MCH-CSDMd.in MCH-SCDMa.in MCH-SCDMd.in n2o-3pp.in oh3_diatom_diatom.in OH+H2-rx-normod-1000-0.5.in o+o2_q1_quintetAp.in o+o2_q2_quintetAp.in YRH-FSa.in YRH-FSd.in YRH-FSTUa.in YRH-FSTUd.in runall comp.sh</p> <p>5 subdirectories: output/ (empty), output2015, output2015-2, output2016, output2023</p> <p>output2023/ (112 files) A12-A12-rx-normod-400-1.0.10 A12-A12-rx-normod-400-1.0.11 A12-A12-rx-normod-400-1.0.20 A12-A12-rx-normod-400-1.0.21 A12-A12-rx-normod-400-1.0.out A12-A1-rx-normod-400-1.0.10 A12-A1-rx-normod-400-1.0.11 A12-A1-rx-normod-400-1.0.20 A12-A1-rx-normod-400-1.0.21 A12-A1-rx-normod-400-1.0.out A1-A159-rx-2000.10 A1-A159-rx-2000.11 A1-A159-rx-2000.20 A1-A159-rx-2000.21 A1-A159-rx-2000.out jvstates_diatom_1_surf_3 jvstates_diatom_2_surf_3 LiFH-SEa.10 LiFH-SEa.11 LiFH-SEa.20 LiFH-SEa.21 LiFH-SEa.30 LiFH-SEa.out LiFH-SEd.10 LiFH-SEd.11 LiFH-SEd.20 LiFH-SEd.21 LiFH-SEd.30 LiFH-SEd.out LiFH-u22.10 LiFH-u22.11 LiFH-u22.20 LiFH-u22.21 LiFH-u22.30 LiFH-u22.out LiFH-v1.10 LiFH-v1.11 LiFH-v1.20 LiFH-v1.21 LiFH-v1.30 LiFH-v1.out MCH-CSDMa.10 MCH-CSDMa.11 MCH-CSDMa.20 MCH-CSDMa.21 MCH-CSDMa.30 MCH-CSDMa.out MCH-CSDMd.10 MCH-CSDMd.11 MCH-CSDMd.20 MCH-CSDMd.21 MCH-CSDMd.30 MCH-CSDMd.out MCH-SCDMa.10 MCH-SCDMa.11 MCH-SCDMa.20 MCH-SCDMa.21 MCH-SCDMa.30 MCH-SCDMa.out MCH-SCDMd.10 MCH-SCDMd.11 MCH-SCDMd.20 MCH-SCDMd.21 MCH-SCDMd.30 MCH-SCDMd.out n2o-3pp.10 n2o-3pp.11 n2o-3pp.20 n2o-3pp.21 n2o-3pp.30 n2o-3pp.out oh3_diatom_diatom.10 oh3_diatom_diatom.11 oh3_diatom_diatom.20 oh3_diatom_diatom.21 oh3_diatom_diatom.out o+o2_q1_quintetAp.10 o+o2_q1_quintetAp.11 o+o2_q1_quintetAp.20 o+o2_q1_quintetAp.21 o+o2_q1_quintetAp.30 o+o2_q1_quintetAp.out o+o2_q2_quintetAp.10 o+o2_q2_quintetAp.11 o+o2_q2_quintetAp.20 o+o2_q2_quintetAp.21 o+o2_q2_quintetAp.30 o+o2_q2_quintetAp.out YRH-FSa.10 YRH-FSa.11 YRH-FSa.20 YRH-FSa.21 YRH-FSa.30 YRH-FSa.out YRH-FSd.10 YRH-FSd.11 YRH-FSd.20 YRH-FSd.21 YRH-FSd.30 YRH-FSd.out YRH-FSTUa.10 YRH-FSTUa.11 YRH-FSTUa.20 YRH-FSTUa.21 YRH-FSTUa.30 YRH-FSTUa.out YRH-FSTUd.10 YRH-FSTUd.11 YRH-FSTUd.20 YRH-FSTUd.21 YRH-FSTUd.30 YRH-FSTUd.out</p>
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test_unimol/	<p>27 files: Al13-melt.in Al20-arb-dyn-nvt-400-1.0-RK4.in Al20-rancub-dyn-nvt-400-1.0-RK4.in Al20-ransph-dyn-nvt-400-1.0-an-RK4.in Al20-ransph-dyn-nvt-400-1.0-BS.in Al20-ransph-dyn-nvt-400-1.0-nh-RK4.in Al20-ransph-dyn-nvt-400-1.0-RK4.in Al2-opt.in Al3-frag.in CH2BrCIPES-CSDMd7en50ev.in HBr-CSDMa.in HBr-FSTUa.in HBr-FSTUSDa.in HN2-tunneling.in nh3-CSDMa.in nh3-CSDMd.in nh3-FSTUa.in nh3-FSTUaSaddle.in nh3-FSTUd.in nh3-FSTUSDa.in nh3-FSTUSDamTRAPZ.in nh3-SCDMa.in nh3-SCDMd.in phohapr-CSDMtunn.in thioanisole_kCSDMa.in runall comp.sh</p> <p>5 subdirectories: output/ (empty), output2015, output2015-2, output2016, output2023</p> <p>output2023/ (146 files) Al13-melt.10 Al13-melt.11 Al13-melt.20 Al13-melt.21 Al13-melt.out Al20-arb-dyn-nvt-400-1.0-RK4.10 Al20-arb-dyn-nvt-400-1.0-RK4.11 Al20-arb-dyn-nvt-400-1.0-RK4.20 Al20-arb-dyn-nvt-400-1.0-RK4.21 Al20-arb-dyn-nvt-400-1.0-RK4.out Al20-rancub-dyn-nvt-400-1.0-RK4.10 Al20-rancub-dyn-nvt-400-1.0-RK4.11 Al20-rancub-dyn-nvt-400-1.0-RK4.20 Al20-rancub-dyn-nvt-400-1.0-RK4.21 Al20-rancub-dyn-nvt-400-1.0-RK4.out Al20-ransph-dyn-nvt-400-1.0-an-RK4.10 Al20-ransph-dyn-nvt-400-1.0-an-RK4.11 Al20-ransph-dyn-nvt-400-1.0-an-RK4.20 Al20-ransph-dyn-nvt-400-1.0-an-RK4.21 Al20-ransph-dyn-nvt-400-1.0-an-RK4.out Al20-ransph-dyn-nvt-400-1.0-BS.10 Al20-ransph-dyn-nvt-400-1.0-BS.11 Al20-ransph-dyn-nvt-400-1.0-BS.20 Al20-ransph-dyn-nvt-400-1.0-BS.21 Al20-ransph-dyn-nvt-400-1.0-BS.out Al20-ransph-dyn-nvt-400-1.0-nh-RK4.10 Al20-ransph-dyn-nvt-400-1.0-nh-RK4.11 Al20-ransph-dyn-nvt-400-1.0-nh-RK4.20 Al20-ransph-dyn-nvt-400-1.0-nh-RK4.21 Al20-ransph-dyn-nvt-400-1.0-nh-RK4.out Al20-ransph-dyn-nvt-400-1.0-RK4.10 Al20-ransph-dyn-nvt-400-1.0-RK4.11 Al20-ransph-dyn-nvt-400-1.0-RK4.20 Al20-ransph-dyn-nvt-400-1.0-RK4.21 Al20-ransph-dyn-nvt-400-1.0-RK4.out Al2-opt.10 Al2-opt.11 Al2-opt.20 Al2-opt.21 Al2-opt.out Al3-frag.10 Al3-frag.11 Al3-frag.20 Al3-frag.21 Al3-frag.out CH2BrCIPES-CSDMd7en50ev.10 CH2BrCIPES-CSDMd7en50ev.11 CH2BrCIPES-CSDMd7en50ev.20 CH2BrCIPES-CSDMd7en50ev.21 CH2BrCIPES-CSDMd7en50ev.22 CH2BrCIPES-CSDMd7en50ev.23 CH2BrCIPES-CSDMd7en50ev.out HBr-CSDMa.10 HBr-CSDMa.11 HBr-CSDMa.20 HBr-CSDMa.21 HBr-CSDMa.out HBr-FSTUa.10 HBr-FSTUa.11 HBr-FSTUa.20 HBr-FSTUa.21 HBr-FSTUa.out HBr-FSTUSDa.10 HBr-FSTUSDa.11 HBr-FSTUSDa.20 HBr-FSTUSDa.21 HBr-FSTUSDa.out HN2-tunneling.10 HN2-tunneling.11 HN2-tunneling.20 HN2-tunneling.21 HN2-tunneling.34 HN2-tunneling.out nh3-CSDMa.10 nh3-CSDMa.11 nh3-CSDMa.20</p>

	nh3-CSDMa.21 nh3-CSDMa.29 nh3-CSDMa.out nh3-CSDMd.10 nh3-CSDMd.11 nh3-CSDMd.20 nh3-CSDMd.21 nh3-CSDMd.out nh3-FSTUa.10 nh3-FSTUa.11 nh3-FSTUa.20 nh3-FSTUa.21 nh3- FSTUa.29 nh3-FSTUa.out nh3-FSTUaSaddle.10 nh3- FSTUaSaddle.11 nh3-FSTUaSaddle.20 nh3-FSTUaSaddle.21 nh3- FSTUaSaddle.29 nh3-FSTUaSaddle.out nh3-FSTUd.10 nh3- FSTUd.11 nh3-FSTUd.20 nh3-FSTUd.21 nh3-FSTUd.29 nh3- FSTUd.out nh3-FSTUSDa.10 nh3-FSTUSDa.11 nh3-FSTUSDa.20 nh3-FSTUSDa.21 nh3-FSTUSDa.29 nh3-FSTUSDamTRAPZ.10 nh3- FSTUSDamTRAPZ.11 nh3-FSTUSDamTRAPZ.20 nh3- FSTUSDamTRAPZ.21 nh3-FSTUSDamTRAPZ.29 nh3- FSTUSDamTRAPZ.out nh3-FSTUSDa.out nh3-SCDMa.10 nh3- SCDMa.11 nh3-SCDMa.20 nh3-SCDMa.21 nh3-SCDMa.29 nh3- SCDMa.out nh3-SCDMd.10 nh3-SCDMd.11 nh3-SCDMd.20 nh3- SCDMd.21 nh3-SCDMd.29 nh3-SCDMd.out phohaprp- CSDMtunn.10 phohaprp-CSDMtunn.11 phohaprp-CSDMtunn.20 phohaprp-CSDMtunn.21 phohaprp-CSDMtunn.22 phohaprp- CSDMtunn.221 phohaprp-CSDMtunn.222 phohaprp-CSDMtunn.223 phohaprp-CSDMtunn.out thioanisole_kCSDMa.10 thioanisole_kCSDMa.11 thioanisole_kCSDMa.20 thioanisole_kCSDMa.21 thioanisole_kCSDMa.22 thioanisole_kCSDMa.221 thioanisole_kCSDMa.222 thioanisole_kCSDMa.223 thioanisole_kCSDMa.23 thioanisole_kCSDMa.27 thioanisole_kCSDMa.out
testruns_dd	Six subdirectories: DH2/, Gaussian16_DH2_MP2/, HCOH-Htransfer/ HCOH-torsion/, Molpro_DH2_CASSCF/, Molpro_ethylene/

XI.B. Compilation and Compatibility

XI.B.1. Compilation of SPRNG random number generator

The random number generator is compiled by executing

```
gmake
```

in the sprng/SRC/ subdirectory. The user may need to modify the file sprng/make.CHOICES. Information about where to find documentation for SPRNG can be found in Section A4. This step needs to be done only once for each installation of *ANT*.

XI.B.2. Compilation using analytic potential energy surfaces

The user must place the potential energy subroutines that he/she wishes to use in the subdirectory `pot/`. We assume here that the name of the potential energy subroutine is `SAMPLEPOT.F`. To compile *ANT*, go to the `src/` subdirectory and execute

```
gmake POT=SAMPLEPOT
```

GMAKE will automatically read the Makefile and compile the executable. The Makefile automatically sets proper compiler options for the various type of hosts (The user can obtain host type information under the shell with command “`echo $HOSTTYPE`”). The default compiler for i386 type of hosts is `g77`, `xlf` for RS6000 type of hosts, and `ifort` for X86_64 type of hosts. Changing the compiler and compiler options should be careful, which is not recommended for non-experts. After compilation, GMAKE will generate an executable named *ANT-SAMPLEPOT.x.opt*. Alternatively, one may execute

```
gmake no_opt POT=SAMPLEPOT
```

to compile the code without optimization and with the name `ANT-SAMPLEPOT.x`. The executables, once compiled, are stored in the `exe/` subdirectory.

The program needs to call the `DGESV` and `DSYEV` subroutines in the LAPACK library. The user may need to change the location of these libraries (`LDFLAGS`) or use an alternative library in the Makefile (`COMPLIB`).

If an OpenMP parallelized potential is provided, the code is compiled with

```
gmake POT=SAMPLEPOT MP=MPI
```

Currently, this only works with the `xlf` compiler and the AIX OS.

The code is executed using (from the `runs/` subdirectory in this example)

```
../exe/ANT-SAMPLEPOT.x.opt < RUN.IN > OUTPUT
```

where “`RUN.IN`” is a properly formatted input file. The code will write general information to standard output (unit 6) as well as several additional output files.

XI.B.3. Compilation for direct dynamics

- **Direct dynamics with *Gaussian09* or *Molpro*:**

To generate an executable for direct dynamics using *Gaussian09* or *Molpro*, go to the `src/` subdirectory and run

```
gmake POT=dd
```

The GMAKE will automatically read the Makefile and compile the executable. An executable named *ANT-dd.x.opt* will be generated in the *exe/* subdirectory. This executable can be used for direct dynamics either with *Gaussian09* or with *Molpro*.

- **Direct dynamics with MOPAC-mn:**

To generate an executable for direct dynamics using *MOPAC-mn*, one first need to obtain the source of *MOPAC-mn* separately and copy the source code to the directory *mopac_src/*, and then run the command

```
gmake POT= potmopac
```

The GMAKE will automatically read the Makefile, compile both *ANT* subroutines and *MOPAC-mn* subroutines, and link them together to generate an executable named *ANT-potmopac.x.opt* in the *exe/* subdirectory.

XI.C. Running the program

After the program is compiled, if you used *POT=potname*, then use

```
./ANT-potname.x.opt < inputfile > outputfile
```

to run the program.

XII. Input file

The input file consists of several input decks. A deck begins with e.g. \$CONTROL and ends with \$END. There are three ways to input the values that the program needs:

1. Only a keyword is needed, e.g. NVT, BULSTOINTHACK.
2. A keyword followed by a value, e.g. POTFLAG=1, TEMP0=200.0. No space is allowed between the keyword and “=” and the value provided.
3. A keyword indicating one or more values will be needed as input from the second line of this keyword, e.g.

```
VIBSTATE
0 1 1 1
```

Keywords specified with input data type all need data input after the keywords (keyword=value). The keywords are case insensitive. A line beginning with “#” will be deemed as comment line and will not be read. Default values set by the program can be found in the file defaults.f. Atomic data are collected in file atomdata.f.

XII.A. \$CONTROL input deck

\$CONTROL: Common control variables.

ATOMDIATOM: Tells the program to run the special option for bimolecular collision of an atom with a diatom. Alternatively, the user can provide the \$ATOMDIATOM deck.

BEEMAN: Beeman algorithm [Ref. 21 in Section XV] is chosen for trajectory integration.

BULSTOINT: Choose Bulirsch-Stoer adaptive step size method [Ref. 2 in Section XV] with approximate calculation of hopping/switching probabilities for the integration method. Both EPS and HSTEP0 are needed as input. Only recommended for single-surface calculations and nonadiabatic calculations with semiclassical Ehrenfest method. If used for nonadiabatic calculations it is only recommended for testing and debugging purposes.

BULSTOINTHACK: Choose Bulirsch-Stoer adaptive step size method [Ref. 2 in Section XV] with accurate calculation of hopping/switching probabilities for the integration method [Ref. 4 in Section XV]. Both EPS and HSTEP0 are needed as input. This is the only method recommended for nonadiabatic trajectories except using semiclassical Ehrenfest method.

DELTATE: Double precision. The range of the initial total energy of the AG can be varied around the given total energy by keyword TE0FIXED. Default 0.0 eV.

- DIABATIC: Tells the program to work in diabatic representation for nonadiabatic trajectory. Default: ADIABATIC.
- EPS: Double precision: Tolerance for Bulirsch-Stoer or Bulirsch-Stoer-Hack integrators (in atomic units). Default: 10^{-7} atomic units.
- HSTEP0: Double precision. Time step (fs) for trajectory integration. Default: 1.0 fs. If Bulirsch-Stoer adaptive step size method is selected, hstep0 is the initial time step. If a fixed step size method, e.g. 4th order Runge-Kutta method, is selected, it is the time step for every step.
- IZPETEMP: Adds correction to temperature specified by the keyword temp0 due to zero-point vibrational energy. This correction is $E_{ZPE} / N_{\text{vib}}k_B$, where E_{ZPE} is zero-point energy for a given AG and N_{vib} number of vibrational modes.
- LIOUVILLE: Liouville approach to velocity Verlet algorithm [Refs. 22, 23 in Section XV].
- NPT: Denotes a fixed pressure ensemble to be used. This keyword does not let the program set up a fixed pressure ensemble by itself, e.g. NPT ensemble, it rather tells program to keep pressure to be constant using a given barostat.
- NVE: Denotes a fixed energy ensemble to be used. Note that this keyword does not specify the initial condition for a microcanonical ensemble by itself. (default).
- NVT: Denotes a fixed temperature ensemble to be used. This keyword does not let the program set up a fixed temperature ensemble by itself, e.g. NVT ensemble, it rather tells program to keep temperature to be constant using a given thermostat.
- POTFLAG: -2: Interface with *MOPAC-mn*.
 -1: Direct dynamics.
 0: Default: HO-MM-1 interface.
 1: 3V-2 interface.
 2: HE-MM-1 interface.
 3: NH₃ interface.
 4: 4-XS interface.
 5: HE-MM-1 interface, pass atomic number instead of atomic symbols.
 6: HBr interface.
 7: BrCH₂Cl interface.
 8: HN₂ interface
 See Section III.B and appendix (SectionA3) for the detailed description of potential surface interfaces.

- 9: HX2 interface for a model system HX2.
 10: phenol APRP photodissociation potential interface

PRESSURE:	Double precision. Pressure of the run (in atm). Default: 1 atm.
QCPACK:	1: Use <i>Gaussian09</i> for direct dynamics. 2: Use <i>Molpro</i> for direct dynamics (default).
RANSEED:	Integer input: Nine-digit integer used to initialize the SPRNG random number generator. Program will determine one randomly by default.
REACTCOL:	Tells the program to run a reactive collision simulation. Alternatively, the user can provide the \$RXCOLLISION deck.
RUNKUT4:	The 4 th order Runge-Kutta method fixed step size integration method. This is the default.
TEMP0:	Double precision. Temperature of the trajectories or initial temperature if temperature ramping is used. Default: 298.15 K.
TE0FIXED:	Double precision. The initial total energy (in eV) of the Atom Group (AG) will be fixed to TE0FIXED ± DELTATE. If DELTATE = 0, this value is fixed by scaling the linear momentum of each atom. Otherwise, the program will re-generate initial geometry and momentum until the initial total energy falls into this range. Currently works only for single AG simulation.
VERLET0:	Original Verlet algorithm [Ref. 19 in Section XV] for trajectory integration.
VVERLET:	Velocity Verlet algorithm [Ref. 20 in Section XV] for trajectory integration.
	Two general references for the molecular dynamics integration algorithms are Refs. 23 and 24 in Section XV.

XII.B. \$CELL input deck

\$CELL:	Cell information. In the next line where keyword CUBIC or CUBOID is, the user must provide a for cubic cells, (a, b, c) for cuboid cells, or $(a, b, c, \alpha, \beta, \gamma)$ for other types of cells.
ARBITRARY:	Other types of cells other than cubic and cuboid.

- CUBIC: Tells the program the simulation is performed in a cubic ($a=b=c$, $\alpha=\beta=\gamma=\pi/2$).
- CUBOID: Tells the program the simulation is performed in a cuboid ($\alpha=\beta=\gamma=\pi/2$).
- ISOLATE: Default: Isolated AG in vacuum.

XII.C. \$RXCOLLISION input deck

\$RXCOLLISION: Reactive collision control deck.

B0IMPACT: Double precision: Impact parameter, distance (in Å) between the two reactants where the first AG is placed at the origin, and the second AG is placed at the (+y,-z) quadrant with an initial velocity +z toward the first AG (See Fig. 1 for an illustration of the relationship between R0COLLISION and B0IMPACT). If a value is provided by the user, then it will be fixed during every trajectory. If not provided, the program will integrate over all possible B0IMPACT with Monte Carlo sampling method (see the *initial conditions for reaction collision* in Section IV and Section A1 for how the program generates B0IMPACT).

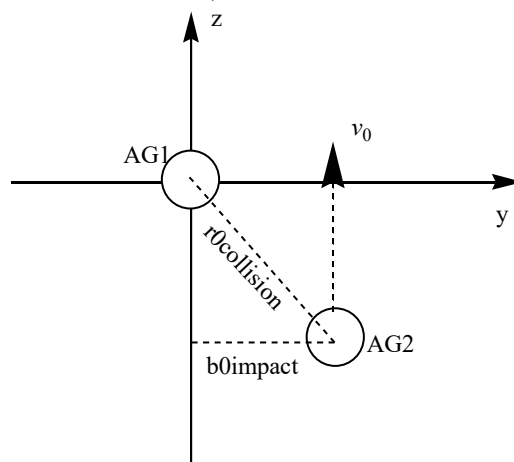


Figure 1

- EQUILIBRIUM: Default: Do an equilibration run before collision. The user can still provide vibrational states, but these values are used to generate the initial conditions only for the equilibration run. The user can choose a proper thermostat used for the equilibration run in the \$TRAJECT deck with the keyword IEQTHERM.
- R0COLLISION: Double precision: Maximum allowed distance between two reactants in Å. By default, the program will automatically generate this distance along the direction binding the two AGs, which is 2.2 times the sum of the diameters of the two AGs. Once R0COLLISION is

provided or generated by the program, it will be fixed in all trajectories.

- R0EFFECTCOL: Double precision: Effective collision radius of two reactants in Angstrom. This means that the two reactants are initially separated by the mean free path (MFP). R0EFFECTCOL is now the maximum value for the y coordinate of the second AG (incident AG).
- STATESELECT: Do a state-selected simulation. The user can provide vibrational state (or energies), rotational states (or energies), and relative translation energy. The values provided will be fixed during a state-selected run.

XII.D. \$ATOMDIATOM input deck

\$ATOMDIATOM: Input deck for setting up special initial condition for an atom–diatom simulation.

- ARRAD: Integer input: Initial molecular arrangement. Default: 1.
 1: AB+C.
 2: BC+A.
 3: AC+B.
- ESCATAD: Double precision: Total energy in eV.
- ECOL: Double precision: Collision energy in eV.
- JJAD: Integer input: Initial rotational quantum number for the diatom. Default: 0.
- RRAD0: Double precision: Initial atom–diatom separation in Å.
- VVAD: Integer input: Initial vibrational quantum number for the diatom. Default: 0.
- JZERO: Text keyword indicating that the impact parameter is chosen from a range consistent with $J = 0$ scattering.
- B_MIN: Double precision: The lower bound on the impact parameter in Å.
- B_MAX: Double precision: The upper bound on the impact parameter in Å.

One needs to specify either ESCATAD or ECOL and either JZERO or B_MIN and B_MAX; all of the remaining keywords (ARRAD, JJAD, VVAD, AND RRAD0) are mandatory.

XII.E. \$SURFACE input deck

- \$SURFACE: Input deck for non-Born-Oppenheimer trajectories.
- CPARAM: Double precision: The constant C in the decay time (decoherence time) used for the CSDM, SCDM, TSF-EDC or FSTU-EDC methods. Default: 1.0.
- E0PARAM: Double precision: The constant E_0 in the decay time (decoherence time) used for the CSDM, SCDM, TSF-EDC or FSTU-EDC methods. Default: 0.1 atomic units.
- FRUSMETH: 0: Default: ignore all frustrated hops.
 1: Reflect all frustrated hops.
 2: Use the gradV prescription for all frustrated hops. See Ref. 9 in Section XV, for a discussion of the gradV method.
- LMODPOP: Logical: The Boolean that determines whether a harmonic analysis of mode populations must be carried out or not. VIBDIST is automatically set to 0 if mode populations are studied. Default: not used.
- METHFLAG: 0: Default: single-surface propagation.
 1: Tully's fewest switches (TFS) non-BO method.
 2: Semiclassical Ehrenfest (SE) non-BO method.
 3: Self-consistent decay of mixing (SCDM) non-BO method.
 4: Coherent switching with decay of mixing (CSDM) non-BO method.
 5: Fewest switches with time uncertainty (FSTU) non-BO method.
 6: Curvature driven coherent switching with decay of mixing (κ CSDM) non-BO method with nuclear EOM propagated with effective NAC.
 7: Curvature driven coherent switching with decay of mixing (κ CSDM) non-BO method with nuclear EOM propagated with NAC.
- NSURF0: Integer input: Initial electronic surface for all trajectories. Default: NSURF0=1.
- NSURFI: Integer input: Initial electronic surface for the normal mode analysis. Default: NSURFI=1.
- NSURFT: Integer input: Total number of electronic surfaces. Default: NSURFI=1.

- NTRAPZ: 0: The unprojected Hessian is used for the initial normal mode analysis and no ZPE maintenance method is applied during the dynamics. This is the default.
- 1: The projected Hessian is used for the initial normal mode analysis and no ZPE maintenance method is applied during the dynamics.
- 2: The unprojected Hessian is used for the initial normal mode analysis and one of the three methods for ZPE maintenance (TRAPZ, mTRAPZ, and mTRAPZ*) is called during the dynamics (NVERS controls the method to be used).
- 3: The projected Hessian is used for the initial normal mode analysis and one of the three methods for ZPE maintenance (TRAPZ, mTRAPZ, and mTRAPZ*) is called during the dynamics (NVERS controls the method to be used).
- The TRAPZ, mTRAPZ, and mTRAPZ* methods allow one to maintain ZPE in semiclassical trajectories. See Refs. 12, 13, and 14 in Section XV. These methods are only programmed in combination with FS, FSTU, and FSTU/SD. Use of mTRAPZ is recommended in combination with the projected Hessian for the initial normal mode analysis (NTRAPZ=3).
- NVERS: 0: The TRAPZ method is called.
- 1: The mTRAPZ method is called. This is the default.
- 2: The mTRAPZ* method is called.
- PRODZPE: Real product zero-point energy used with mTRAPZ*, expressed in eV. The default is set to a very high value (10^6 eV).
- RALPHA: Double precision: The real coefficient used to decrease (input a value larger than 1) the initial vibrational energy supplied to the molecule to study its dynamics in a potential well. Default: 1.0. The vibrational energy for mode m is calculated as $(0.5 + n_m)\hbar\omega_m / ralpha$.
- REPFLGI: Integer input: Initial representation for the normal mode analysis. Default: REPFLAG.
- STODECOFLAG: 0: Stochastic decoherence (SD) is not used (default).
- 1: Use stochastic decoherence (SD) to treat frustrated hops caused by inaccuracies in the treatment of decoherence. See Ref. 10 in Section XV for a description and application of the SD scheme used with FSTU and Refs. 11 and 14 in Section XV, for further applications of FSTU/SD.
- This is only meaningful in combination with FS and FSTU, and it is recommended for use with FSTU. This option could also be used with TFS but the results are expected to be less accurate.

Note that the formula given in Ref. 9 [A. W. Jasper and D. G. Truhlar, *J. Chem. Phys.* **127**, article no. 194306 (2007)] for the decoherence time was incorrect and has been corrected. In particular, in eq. (5) of that paper, $P(\Delta t) = \exp(-\Delta t/\tau)$, the variable Δt was defined as $t - t_h$, where t_h is the stochastic decoherence time, and τ is the characteristic decoherence time. The correct definition of Δt as equal to the time step of the trajectory propagation has now been implemented in the code. The literature reference for the correction is:

"Coupled-Surface Investigation of the Photodissociation of $\text{NH}_3(\tilde{\text{A}})$: Effect of Exciting the Symmetric and Antisymmetric Stretching Modes," D. Bonhommeau, R. Valero, D. G. Truhlar, and A. Jasper, *Journal of Chemical Physics* **130**, article no. 234303 (2009).

- EDCFLAG: 0: Energy-based decoherence correction (EDC) is not used (default).
 1: Use energy-based decoherence correction (EDC) to include decoherence in TFS or FSTU. See Refs. 6 and 7 in Section XV for a description.
- TINYRHO: Double precision: a parameter used to avoid dividing by zero (or by a number that is very close to zero) in non-Born-Oppenheimer decay-of-mixing trajectories when using eq. (69) of Ref. 30. (TINYRHO is used for CSDM, SCDM, TSF-EDC or FSTU-EDC methods, and it is not used for single-surface trajectories, for surface-hopping trajectories without EDC, or for the semiclassical Ehrenfest method.) Equation (69) is only calculated if ρ_{KK} is greater than TINYRHO. The default value of TINYRHO is 1.0E-04, but the user can change this if necessary or desirable. (When TINYRHO is too small, some trajectories may develop inaccurate expansion coefficients at points in the trajectory where ρ_{KK} is very small.)
- COUPLINGDECAY: Integer input: number of bond distances that will be checked for setting the long-range coupling to zero.
 This keyword is used for calculations in both adiabatic and diabatic representations.
 If COUPLINGDECAY is zero, nothing is done. The default is zero, and if this keyword is not given, the default is used.
 If COUPLINGDECAY is nonzero, then all couplings (including NACs, diabatic couplings, and time-derivative couplings) will be set to zero for any time step for which any one or more of the specified interatomic distances is larger than the threshold. If COUPLINGDECAY= n , then n interatomic distances will be specified (in Å) in n following lines.
 Example:

```

couplingdecay=3
1 2 4.0
1 3 4.0
2 3 4.0

```

XII.F. \$TERMCN input deck

- \$TERMCN:** Termination condition
- BONDBRTHRE:** Double precision: If the bond between two atoms is BONDBRTHRE times of its covalent bond length, a bond is completely broken. Default: 2.5.
- BONDFMTHRE:** Double precision: If the bond between two atoms is BONDFMTHRE times of its covalent bond (covalent bond lengths are the sum of the covalent radii of the two bonding atoms, which are taken from <http://www.webelements.com/>. Definition of covalent radius: When two atoms of the same kind are bonded through a *single* bond in a neutral molecule, then one half of the bond length is referred to as the covalent radius.), a bond is formed. Used only for bond forming processes. Default: 1.5.
- N_ATOMTYPES:** Integer input: number of different types of atoms in the fragment to be monitored. Used only for TERMFLAG=4 and TERMFLAG=7. A reaction is over if the minimum distance between the atoms in two fragments is greater than BONDBRTHRE times of its covalent bond length.
Atomic number and the number of this type of atoms are read from the next line of N_ATOMTYPES, for example, to monitor H₂O fragment (regardless of bonding patterns):
N_ATOMTYPES=2
6 1
1 2
- N_FRAGS:** Integer input: number of fragments to be monitored. Default: 2. Set to zero to monitor any type of fragmentation patterns. Used only for TERMFLAG=7.
- N_TURN:** Integer input, used only for reactive collision simulation: If the projected CoM motion of the second AG (incident AG) onto the CoM vector between the two AGs ($\vec{R}_{CoM(2)} - \vec{R}_{CoM(1)}$) changes sign N_TURN times, a collision is deemed as reactive. Default: 3.
- NBONDBREAK:** Integer input: Number of breaking bonds to be monitored.

Similar input method as monitoring bond forming is used, but the distance threshold is the distance a bond can be deemed as broken.

- NBONDFORM:** Integer input: number of forming bonds to be monitored.
The indices of the atom pairs monitored and bond distance threshold (Å, bond distance less than this value would be deemed as formed) are read from the next line of NBONDFORM:
NBONDFORM=2
1 2 1.40
4 3 2.10
- NBONDTYPE:** Integer input: The user provides the covalent bond distance (R_{co}) used for judging bond breaking and forming: atoms with bond distances less than $BONDFMTHRE * R_{co}$ are deemed to be bonded. The atomic symbols of the two atoms whose covalent bond distance will be changed and the desired value (Å) are read from the next line of NBONDTYPE:
NBONDTYPE=2
C H 1.40
Al Al 2.10
- NOAGDEFRAG:** Used only for TERMFLAG=4. Do not monitor AG fragmentation. Default: monitor.
- NOAGMERGE:** Used only for TERMFLAG=4. Do not monitor AG merge. Default: monitor.
- NOATTRANS:** Used only for TERMFLAG=4. Do not monitor atom/group transfer/exchange between AGs. Default: monitor.
- NTORSION** Used only for TERMFLAG=8. It specifies the number of torsion angles to be monitored and the range of torsion angles for stopping the trajectory.

NTORSION=1
1 2 3 4 130 180
The above two lines specify that one torsion angle (1-2-3-4) is monitored, and trajectories are stopped when this torsion angle is in the range of [130, 180] degree or [-180, -130] degree. Note that the specified values in the input file must be positive.
- T_GRADMAG:** Double precision: The trajectory terminates when the absolute value of any of the components of the gradient is less than T_GRADMAG in eV/Å. Default value is 10^{-4} eV/Å.

- T_GRADMAGX: Double precision: The trajectory terminates when the root mean square of the gradient is less than T_GRADMAGX in eV/Å. Default value is 5×10^{-4} eV/Å.
- T_NSTEP: Integer input: Total number of steps for each trajectory. If the input is -1, then the number of the steps is unlimited. The default value is 5000. It is often used together with the other termination condition.
- T_STIME: Double precision: Trajectories will propagate for T_STIME fs. Default: T_STIME=5000.
- TERMFLAG: 0: Default: run for T_NSTEP steps.
 1: Run for T_STIME fs.
 2: Converge the RMS of the gradients to T_GRADMAG; for geometry optimization only.
 3: Monitoring specific atom pairs with either bond breaking or forming or both.
 4: Fragment monitor: AG merge, AG fragmentation, atom/group transfer/exchange between AGs. Attention: intra-AG reactions (intra-AG bond forming, breaking, or atom/group transfer/move) cannot be monitored by this method.
 5: Monitoring any bond breaking or forming. The user can change the default bonding threshold by the input deck of NBONDTYPE.
 6: Monitoring sticking time, for reactive collision only. Once $R_{\min(i1,j2)} \leq \text{BONDFMTHRE} * R_{\text{co}(i1,j2)}$, a reaction occurs and the current time is saved as t_0 , here $R_{\min(i1,j2)}$ is minimum of the bond distances of all atom pairs that do not belong to the same reactant, $i1$ means atom i belongs to the first reactant and $j2$ means atom j belongs to the second reactant; BONDFMTHRE, an adjustable input parameter; $R_{\text{co}(i1,j2)}$, covalent bond distance between $i1$ and $j2$, which is also adjustable by the input parameter NBONDTYPE. Then after monitoring it dissociate into the same type of reactants again, i.e. $R_{\min(i1,j2)} \geq \text{BONDFMTHRE} * R_{\text{co}(i1,j2)}$, the time is saved as t_1 . If $R_{\min(i1,j2)} \geq \text{BONDFMTHRE} * R_{\text{co}(i1,j2)}$ is observed for TERMSTEPS successive steps after time t_1 , then time $(t_1 - t_0)$ is the sticking time of the two AGs.
 7: Monitor unimolecular fragmentation probability. Input T_STIME is required. Default: not to. See below for more detailed description.
 8. Monitor unimolecular isomerization by changing torsion angles. Input T_STIME is required. It requires the NTORSION keyword to specify the number of torsion angles.

Notes on TERMFLAG=4 or 7:

For each trajectory, at every step, the program will call RIJMATR to calculate the distance matrix and calculate the bonding information matrix. Bonding criteria can be

adjusted by the user. See Section XII for details. Once bonding information matrix is obtained, the program can:

- 1) Compare initial bonding information matrix with the present matrix to find which bond is broken or formed.
- 2) Do a fragment analysis by calling FRAG, to determine the fragments in the system so as to determine AG merge, fragmentation or fragment transfer. The user can monitor a specific fragment product or a specific fragmentation channel. In monitoring fragmentation process, the user can choose a large bond threshold for example the cutoff of the potential so that once two fragments are separated by the cutoff distance, they will never come back because there is no force to pull them back.
- 3) The time of the reaction is recorded once a specified reaction pattern is observed, and this trajectory is terminated. The program prints out the fragmentation pattern, and time information in a format like:

“nfrag natinfrag time = 2 17 1 4595.99999999984266 fs”.

The first integer after “=” is the total number of fragments (NFRAG), and the following NFRAG integers are the number of atoms in each fragments, and then the terminating time for this trajectory. The user can extract this information out and analyze it.

- 4) Finally, the program will report the reaction probability and calculate unimolecular reaction rate constant by a simple equation:

$$k = \ln(1 - P_{\text{react}}) / t$$

where P_{react} is the reaction probability (ratio of reactive trajectories), t is the maximum simulation time set for all trajectories. Note: This equation holds only when 1) the reaction channel to be monitored is the governing channel; or 2) P_{react} counts in all possible reaction channels.

TERMSTEPS: Integer input. Used only for TERMFLAG = 3, 4, 5, or 6. A trajectory is deemed as reactive after monitoring bond forming, breaking, fragmentation, AG merge, atom/group transfer/exchange for a successive TERMSTEPS steps. Default: 50 steps. This choice is very important on judging if a reaction has occurred or ended (especially for TERMFLAG=6).

XII.G. \$TRAJECT input deck

\$TRAJECT: Trajectory control deck.

DEMIN: Double precision: the initial energy of the AG must be larger than or equal to this value. Default: -10^{50} atomic units.

DEMAX: Double precision: the initial energy of the AG must be smaller than this value. Default: 10^{50} atomic units.

IADJPRESS: 0: Default: Berendsen barostat, adjusting pressure by scaling the position of each atom by a factor of $\left[1 - \frac{hstep0}{taup}(P_0 - P)\right]^{1/3}$ for

cubic and cuboid cells. For triclinic cells, the scaling is achieved by using a scaling matrix $\boldsymbol{\mu} = 1 - \frac{\beta\delta t}{3\tau_p}(\mathbf{P}_0 - \mathbf{P}(t))$.

See Ref. 28 in Section XV.

Other barostats have not been implemented yet.

For the different thermostats and barostats, see also Refs. 23 and 24 in Section XV.

- IADJTEMP: 0: Default: Berendsen thermostat, adjusting temperature by scaling the momentum with a factor of $\sqrt{1 + \frac{hstep0}{taut}(T_0/T - 1)}$. This is equivalent to coupling the system to a bath with temperature T_0 and a coupling factor $HSTEP0/TAUT$. The default value of $HSTEP0/TAUP$ is 0.0025. See Ref. 28 in Section XV.
- 1: Adjusting temperature by scaling the momentum with a factor of $\sqrt{T_0/T}$.
- 2: Adjusting temperature with Andersen thermostat. Input VFREQ is required. See Ref. 25 in Section XV.
- 3: Adjusting temperature with Nosé-Hoover two-chain thermostat. See Refs. 26 and 27 in Section XV. It cannot be used with simple Verlet, velocity Verlet and Beeman integrator, but can be used with Liouville approach to velocity Verlet. More details about these thermostats are given in Section A2.
- IEQTHERM: Integer input to control the ensemble used for the equilibration run. The choice of thermostat and barostat is controlled by IADJTEMP and IADJPRESS.
- 0: Default: fixed-energy ensemble.
- 1: Fixed-temperature ensemble.
- 2: Fixed-pressure ensemble.
- IPICKTRJ: Integer input control the configuration pick up method during the equilibration run.
- 0: Default, once the AG is found dissociated during equilibration run, jump out equilibration run and abandon the previously saved configurations and restart a new equilibration run.
- 1: Once the AG is found dissociated during equilibration run, jump out equilibration run but DO NOT abandon the previously saved configurations and restart a new equilibration run until enough configurations are saved.
- 2: Effectively put a hard wall before an atom if it breaks a bond with others by pulling it back.

- ITOSAVE: Integer input: Used for reactive collision run and unimolecular fragmentation run (TERMFLAG=7). During the equilibration run the initial coordinates and momenta start being saved as soon as this number of steps is reached. Default: 5000.
- KEEPTRANS: Do not remove CoM motion (total translational momentum). Default: remove.
- KEEPANGMOM: Tells the program not to remove the initial overall angular momentum. Default: Keep for reactive collision simulation, atom-diatom simulation, and NVT simulation with Andersen thermostat.
- N_RAMP: Integer input: after momenta rescaling or temperature change wait for N_RAMP steps before starting to average properties. Default: 20000 steps.
- NEQUILRAMP: Integer input: averaging properties over NEQUILRAMP steps after momenta rescaling or temperature change.
- NOEQUILIBRIUM: Tells the program not to do an equilibration run. Used only for reactive collision runs with TERMFLAG=7.
- NOREINITROT: Tells the program not to remove the angular momentum after the equilibration run.
- NOZEROCOM: Do not move the CoM to origin of the coordinate system. Default: move.
- NRAMP: Integer input: Rescaling momenta or change temperature for NRAMP times. Default: 1.
- NREINIT: Integer input: remove overall CoM motion, angular momentum and move the CoM to origin of the coordinate system every NREINIT time. Remove angular momentum will not be done for reactive collision run, atom-diatom run, periodic condition and if KEEPANGMOM is specified. The CoM of AG is moved back to origin every step if Andersen thermostat is used because the CoM motion in Andersen thermostat is not conserved. Default: 10000. Related input: NOZEROCOM, KEEPTRANS, KEEPANGMOM.
- NTRAJ: Integer input: number of trajectories to be run.
- PICKTHR: Double precision: control the probability to choose a configuration during the equilibration run. Default: 0.1.

- RAMPFACT:** Double precision: Momenta rescaling factor (greater than one is heating while less than one is cooling) or temperature change interval (positive value corresponds to heating while negative to cooling). Default: 1.0.
- RAMPSTEP0:** Double precision: Initial number of steps used for the first momenta rescaling or temperature change. Default: 20000 steps.
- RESTART:** A list of trajectory indices to be restarted is read from the next line of this keyword. For example, if the user wants to restart 5 out of 1000 trajectories with indices 5, 33, 100, 211, and 877, then the input file is as follows:

```
NTRAJ=5
RESTART
5 33 100 211 877
```

The original input file only specified

```
NTRAJ=1000
```
- Note that the explicit knowledge of initial trajectory random numbers is not useful to restart a given trajectory since each trajectory corresponds to one random number stream. The whole information on random numbers is therefore contained in the trajectory number. For more details about the SPRNG random number generator, the user can refer to the documentation provided in `/sprng/DOCS/sprng.html.tar.Z` (see Appendix A4. SPRNG documentation).
- SYSFREQ:** Double precision: Used for Nosé-Hoover thermostat, the characteristic vibrational frequency of the system (unit: 1/fs). Default: 1.0.
- TAUT:** Double precision: Used for Berendsen thermostat, coupling parameter whose magnitude determines how tightly the bath and the system are coupled together (unit: fs). Default: $HSTEP0/0.0025$ fs.
- TAUP:** Double precision: Used for Berendsen barostat, coupling parameter whose magnitude determines how tightly the bath and the system are coupled together (unit: fs atm). Default: $HSTEP0*p0/0.0025$ fs atm, where $p0$ is the input pressure.
- TFLAG1:** 0: Default: no special options.
1: Nuclear momenta are set to zero at every step, i.e., steepest-descent minimization.
2: Temperature rescaling. RAMPSTEP0, NEQUILRAMP, RAMPFACT, N_RAMP, and NRAMP keywords are required.

- 3: Simulated heating/cooling. RAMPSTEP0, NEQUILRAMP, RAMPFAC, N_RAMP, and NRAMP keywords are required.
- 4: After simulated cooling, do an additional geometry optimization with the BFGS method.
- 5: During simulated cooling / heating, do BFGS geometry optimization at steps with a probability determined by PICKTHR.

VFREQ: Double precision: Used for Andersen thermostat, collision frequency between the atom of the system and the bath (unit: fs⁻¹). Default: 0.1/HSTEP0.

WITHROTINEQ: Tells the program not to remove the initial overall angular momentum during the equilibration run.

XII.H. \$TUNNELING input deck

\$TUNNELING Tunneling options deck; it is only applicable to unimolecular processes

ETA: The η value used in the army ants algorithm; the default is 0.95.

NBEND Number of bend coordinates (bond angles). Following this keyword, a list of the bend coordinates should be given; each bend coordinate is represented by three atoms that form a bond angle. For example:

```
NBEND=2
1 2 3
2 3 4
```

NGAUSS Number of nodes for Gauss-Legendre quadrature for the imaginary action integral. Default is 6. The program is able to handle up to 512 nodes. This keyword is only used for a single-surface tunneling case.

NIMPTOR number of improper torsion/out-of-plane bending coordinates. Following this keyword, a list of the improper torsion coordinates should be given; each torsion coordinate is represented by four atoms I-J-K-L, in which the center atom must be the second one, i.e. the atom denoted as J. The out-of-bending angle is defined as the angle between the vector bond I-J and the plane formed by the atoms J-K-L (e.g., note that the out-of-plane angles denoted by the sequence of the atoms I-J-K-L and I-K-J-L are not equivalent). For example:

```
NIMPTOR=1
1 2 3 4
```

NSTR Number of stretching coordinates. Following this keyword, a list of the stretching coordinates should be given; each stretching coordinate is represented by two atoms that form a chemical bond. For example:

```
NSTR=2
1 2
1 3 *
```

In the above example, the * symbol indicates that this coordinate is the tunneling coordinate.

NTOR Number of torsion coordinates (dihedral angles). Following this keyword, a list of the torsion coordinates should be given; each torsion coordinate is represented by four atoms that specify a dihedral angle. For example:

```
NTOR=1
1 2 3 4
```

Below it is explained how to specify tunneling coordinates. The *ANT* program can handle two kinds of tunneling coordinates: a single internal coordinate and a combination of two stretch coordinates. The two kinds coordinates require different input styles, and no additional keyword is required to tell which kind of coordinates to be used.

1) A single internal coordinate as a tunneling coordinate:

The * symbol can be added after any of the internal coordinates to denote that it is a tunneling coordinate. If more than one internal coordinate is denoted by the * symbol, the tunneling path is defined by using them one at a time, not as a linear combination of them.

2) A combination of two stretch coordinates as a tunneling coordinate.

A combination of two stretch coordinates can be used as a tunneling coordinate for atom-transfer reactions. Below is an example to show how to specify such a combination:

```
NSTR=4
3 1
1 2
2 4 + 1.0
1 4 - 1.0
```

This example shows the tunneling coordinate is a combination of increasing of 2-4 bond length (+ denotes increasing) and decreasing of 1-4 bond length (- denotes decreasing). The number after symbol + or - denotes the relative changing rate of two coordinates, i.e., a stretch coordinate changes as $r \pm \Delta r/l$, where number l is the

number that is given after symbol + or -. This example is for the case in which atom 4 is transferred from atom 2 to atom 1.

Note that one can use either a single internal coordinate as a tunneling coordinate or a combination of two stretch coordinates as a tunneling coordinate, but one cannot use both of them at one time.

XIII.I. \$OUTPUT input deck

\$OUTPUT: Output print information control deck.

IDEBUG: Tells the program to print out debug information (very lengthy).
Default: not used.

NPRINT: Integer input: Print information every NPRINT steps.

MAXPRINT: Tells the program to print out everything. Default: not used.

MINPRINTICON: Tells the program to skip information about the selection of initial conditions. Useful for constant-energy initial conditions. Default: not used.

MINPRINTTRAPZ: Tells the program to skip some printings (frequencies at each time steps, some warnings when the system seems to get close to a conical intersection, etc.) when a TRAPZ-like method is used.
Default: not used.

OUTFLAG: 0: Write output to all units as listed in Section XIII, which is the default.
1~99: Write output to unit 6 and to units (integers) listed from the next line of this keyword. See Section XIII for the description of output files.

XIII.J. \$ANALYSIS input deck

\$ANALYSIS: Result analysis control deck.

COHESIVE: Averaging on cohesive energy, and its standard deviation.

FRAGCON: Averaging on the density of the fragments.

HEATCAPACITY: Averaging on heat capacity.

KINETIC: Averaging on kinetic energy, and its standard deviation.

- NSTAT: Integer input: Start averaging on properties only after NSTAT steps.
DEFAULT: 1.
- POTENTIAL: Averaging on potential energy, and its standard deviation.
- RBIN: Double precision: bin distance (in Å) used to calculate binned Berry parameter, radial distribution functions. Default: 1.0 Å.

XII.K. \$DATA input deck

\$DATA: Geometry, molecule properties, initial conditions, and control panel. Before given all keywords for this input deck, an input example is shown below with initial vibrational states and rotational energy (assuming the molecule is non-linear):

```
$data
nmol=1
natom=6 initx=0 initp=-1 temp0im=300.0
# Charge and multiplicity
0 1
# Atomic symbol, atomic weight (in amu), x, y, z (in Å)
C 12.0 0.000000 0.000000 0.000000
H 1.0 0.000000 0.000000 1.089000
H 1.0 1.026719 0.000000 -0.363000
H 1.0 -0.513360 -0.889165 -0.363000
O 16.0 -0.659966 1.143095 -0.466667
H 1.0 -0.659966 1.143095 -1.416667
vibstates
# Integer input
1 2 1 1 1 1 0 0 0 1 3 (for local minimum)
rotenergies
#Double precision (The actual rotation energies are 0.045  $k_B T$ , 0.010  $k_B T$ , and 0.20  $k_B T$ )
0.045 0.010 0.20
$end
```

Cartesian coordinates of the AG should follow the order of atomic symbol, charge of the atom (if indicated by READINCHG), atomic mass in amu, and the Cartesian coordinates in Å.

- NMOL: Integer input: Number of AGs, provided in a separate line. The *ANT* program can handle either one or two AGs.

INITX, INITP, VIBSELECT, VIBDIST, VERTE, BANDWD, TEMP0IM, READINCHG, and ERELTRANS must be provided in one *single* line after NMOL.

- ERELTRANS: Double precision: Relative translational energy for reactive collision run only. The actual relative energy is $ERELTRANS * k_B T$.

Alternatively, the user can provide ERELTRANS by specifying COMPP in the \$COMPP input deck. If ERELTRANS is provided, that means the relative translational energy is fixed. If both ERELTRANS and COMPP are not provided, the program will randomly generate a value according to Boltzmann distribution for reactive collision run.

INITX:

Integer input.

- 0: Read the input Cartesian coordinates (see the above example).
 1: Generate random atom coordinates in a sphere. The user must provide the radius (in Å) of the sphere. Following is an example in which a random sphere with a radius of 20.0 Å, with 5 carbon atoms, 6 aluminum atoms will be generated:

```
20.0
5 C 12.0
6 Al 27.0
```

Note: If R is the atomic distance between two atoms, the radius of the sphere generated would be $0.5 R (N/0.75)^{1/3} \approx 0.5 * 1.10 R N^{1/3}$, where N is the number of atoms in the cluster. In a realistic run, one really doesn't want the generated sphere to be closely packed. Therefore, the radius should be set to a larger value. It should be safe to set the radius of the sphere as $R N^{1/3}$. However, the radius provided should not be too large, since the cluster generated may not be spherical.

- 2: Generate random atom coordinates in an $a \times b \times c$ cuboid. The user must provide a , b , c (in Å). The remaining inputs are similar to those used for $initx=1$. For example, a random $10.0 \times 15.0 \times 20.0$ cuboid cell with 5 carbon atoms and 6 aluminum atoms:

```
10.0 15.0 20.0
5 C 12.0
6 Al 27.0
```

- 3: Generate random atom coordinates with arbitrary shape. The inputs are similar to those used for $initx=1$ and 2 except no input for radius or a , b , and c .

- 4: Special atom-diatom input. Example for C-H-O:

```
C 12.0
H 1.0
O 16.0
```

- 5: Generate random molecules in an $a \times b \times c$ cuboid. User must provide a , b , c (in Å) and the rest input are the Cartesian geometry of the building molecule. For example, a random $10.0 \times 15.0 \times 20.0$ cuboid with 20 Al_2 molecules:

```
10.0 15.0 20.0
20 2 ! number of building mol.; number of atom
Al 27.0 0.0 0.0 0.0
Al 27.0 0.0 0.0 2.50
```

6: Special diatom–diatom input. Example for OH₃:

H 1.00794
 H 1.00794
 H 1.00794
 O 15.99940

INITP: Integer input.

0: The initial momenta are set to zero.

1: Default, random thermal distribution. The user can provide temperatures different from the global temperature provided in the \$control deck by providing a TEMP0IM input.

−1: Initial momenta are determined by other choices, such as VIBSELECT and ROTSTATES.

READINCHG: Tells the program to read in charge information for each atom. Charges of the atoms are read from the second column of the geometry input data, after atomic symbols. Default: not to.

TEMP0IM: Double precision: temperature for this AG to generate random rotational energies, translational energies, etc..., according to the Boltzmann distribution. Default, equal to the global temperature specified in the \$CONTROL deck.

VIBSELECT: 0: Default: Determined by other choices. For example, using keywords INITX=0, INITP =1, and TE0FIXED= E , the program uses a fixed input geometry for all trajectories and the momenta are randomly determined based on the total energy E .

1: The user provides vibrational states. The structure provided can be a local minimum or a saddle point. Vibrational states are provided by the keyword VIBSTATE.

2: The user provides an energy minimum structure. The program assigns vibrational states at random, selected out of a Boltzmann distribution at a user specified temperature that is specified by keyword TEMP0IM. This option only applies to minimum-energy structures (not saddle points).

3: The program performs a normal mode frequency analysis and uses it to generate an initial velocity from a Maxwell thermal distribution at a given temperature TEMP0IM. This option should be combined with the keyword INITP=1. This is an option for canonical ensemble, not an option for state-selected ensemble. This option only applies to minimum-energy structures (not saddle points).

4. The user provides an energy minimum structure. The amount of energy in each mode is the same for each mode and is given by the VIBENE keyword.

5. The user provides an energy minimum structure. The amount of energy in each mode can be different for each mode. To give energy for each mode, use the keyword VIBENE.
6. Like VIBSELECT=4 except that vibrational mode m energy E_m is calculated by the program as $\min[(0.5 h\nu_m, \text{input } E_m)]$.
7. Like VIBSELECT=5 except that E_m is calculated by the program as $\min[(0.5 h\nu_m, \text{input } E_m)]$.

VIBDIST: Determines the type of phase space distribution for initial conditions prepared with normal mode analysis (see Section IV and Section A1 for more details). When VIBDIST is 0, 1, or 2, all the modes are treated in the same way.

- 0: Default: classical or quasiclassical distribution. This distribution is quasiclassical if VIBSELECT = 1 or 2, and it is classical if VIBSELECT \geq 4. With this option, the initial displacements are distributed between $-q_{\text{turn},m}$ and $+q_{\text{turn},m}$ in the same way as for a classical harmonic oscillator with the energy specified by VIBENE, where $q_{\text{turn},m}$ is the magnitude of the turning point determined by

$$\frac{1}{2}k_m q_{\text{turn},m}^2 = E_m$$

where q_m is the normal mode displacement coordinate, and k_m is the force constant. When this option is selected, the following steps are taken:

- (i) a random number λ is chosen (random numbers are always evenly distributed between 0 and 1), and the initial displacement is

$$q_m = q_{\text{turn},m} \cos(2\pi\lambda)$$

- (ii) The potential energy is evaluated with the actual potential function. If $V(q_m) - V(0) > E_m$, then $|q_m|$ is decreased by 10%, and this is repeated if necessary until

$$V(q_m) \leq V(0) + E_m.$$

Note that $V(0)$ denotes all the modes m' not yet assigned at $q_{m'} = 0$, those modes already assigned at their assigned values, and the current mode m at $q_m = 0$, whereas $V(q_m)$ denotes modes m' not yet assigned at $q_{m'} = 0$, those modes already assigned at their assigned values, and the current

mode m at q_m . Because of this complication, the results depend on the order that the modes are assigned. For each trajectory the modes are assigned in a different order, as determined by random numbers.

(iii) Another random number λ' is chosen to determine the sign of the momentum p_m in mode m .

(iv) The momentum is assigned as

$$p_m = \text{sign}(\lambda') \sqrt{2\mu \left(E_m - [V(q_m) - V(0)] \right)}$$

where m is the normal-mode reduced mass.

1: If VIBSELECT=1, this option should be used only when n_m is 0. It may be called the ground-state harmonic oscillator distribution.

Using a random number, the coordinate q_m is selected from the quantum mechanical harmonic oscillator coordinate distribution, which is the square of the ground-state wave function and is a Gaussian. This means that

$$\Delta q = \sigma_x \sqrt{-2 \ln(\lambda_1)} \cos(2\pi\lambda_2)$$

where λ_1 and λ_2 are two random numbers, and

$$\sigma_x = \sqrt{E_m / k_m} .$$

Then steps ii, iii, and iv above are repeated.

2: If VIBSELECT=1, this option should be used only when n_m is 0. A

Wigner distribution obtained from the separable harmonic oscillator wave function in the normal mode representation. The distribution is generated using the Box-Muller algorithm for normal mode coordinate displacement and momentum. In particular the normal mode displacement and momentum is calculated as

$$q_m = \sigma_x \sqrt{-2 \ln(\lambda_1)} \cos(2\pi\lambda_2)$$

$$p_m = \sigma_p \sqrt{-2 \ln(\lambda_1)} \cos(2\pi\lambda_2)$$

$$\sigma_p = 1 / (2\sigma_x) \text{ and}$$

$$\sigma_x = \sqrt{E_m / k_m} .$$

Note that we use the same set of random numbers λ_1 and λ_2 in determining displacement and momentum.

9. This option allows one to use select option 1, 2, or 3 individually for each mode. If VIBDIST = 9, the one must supply another keyword VIBDISTN = (vibdist₁, vibdist₂, ..., vibdist_{3N-6}) for minima and VIBDISTN = (vibdist₁, vibdist₂, ..., vibdist_{3N-7}) for saddle points.

VIBTYPE: Type of initial geometry stationary point.
 0: Default: local minimum.
 1: Saddle point.

The following keywords should be provided after the coordinates of the AG.

ROTENERGIES: The user provides rotational energies in the next line where ROTENERGIES is. This means that state selection on rotational energies (values provided will be fixed) is achieved.

ROTSTATES: The user provides rotational quantum numbers in the next line where ROTSTATES is. Only linear AG can be dealt with at present. This means that state selection on rotational states is achieved. If both ROTSTATES and ROTENERGIES are not provided, by default, the program will randomly generate the rotational state or rotational energies needed according to the Boltzmann distribution for every trajectory.

VIBDISTN If VIBDIST=9, user must supply this keyword to select VIBDIST (0, 1, or 2) individually for each vibrational mode. For example, if one wants to choose different phase space distribution method for a molecule with 6 vibrational modes (vibrational modes are in order of decreasing magnitude of their frequencies)

```
VIBDISTN
0 0 0 1 1 1
```

VIBENE Double precision: fixed energy for each vibrational mode in eV. The default is 0.02 eV for all modes.

(i) When VIBSELECT = 4 or 6, the amount of energy for each mode is the same so only one value is needed after this keyword

(ii) When VIBSELECT = 5 or 7, user provides $3N-6$ (local minimum) or $3N-7$ (first order saddle point) energies for each mode individually. For example, a molecule with 5 vibrational modes has following input

```
VIBENE
0.02 0.02 0.02 0.01 0.01
```

VIBSTATES: For a local minimum, the user provides vibrational quantum numbers of each mode in the line following the keyword VIBSTATES. Using this keyword means to do a normal mode analysis to provide initial coordinates and also means VIBSELECT=1. For a saddle point, the user provides the $3N-6$ (linear molecule) or $3N-7$ (nonlinear molecule) vibrational quantum numbers for the bound normal modes, and a positive or negative real number meaning the

translational energy along the unbound normal mode in its positive or negative direction, respectively (in eV).

The vibrational quantum numbers can be fractional (e.g. 0.5). This is useful to distribute excitations equally along degenerate components of a normal mode. For example, for a doubly degenerate normal mode, a single excitation could be specified assigning 0.5 to both components in the input file.

```
VIBSTATES
0 0 0 1
```

XII.L. \$COMXX input deck

\$COMXX: The Cartesian coordinates (in Å) of the center of mass for all the AGs. For example, the first AG is placed at the origin, while the second AG is placed 20.0 Å away on the z axis:

```
$COMXX
  0.0 0.0 0.0
  0.0 0.0 20.0
$END
```

XII.M. \$COMPP input deck

\$COMPP: The three components of momenta (in atomic units) of the center of mass for all the AGs.

```
For example:
$COMPP
  0.0 0.0 0.0
  0.0 0.0 20.0
$END
```

XIII. Output files

Unit 6 (standard output): General output.

General information and error warnings are written to the standard output (unit 6).

Unit 10: Initial coordinates.

The first line contains the trajectory index and potential energy in eV, followed by (one line for each atom)

1. Atomic symbol
2. Atomic mass in amu
3. The Cartesian coordinates in Å.

Unit 11: Initial momenta.

The first line contains the trajectory index and kinetic energy in eV, followed by (one line for each atom)

1. Atomic symbol
2. Atomic mass in amu
3. The Cartesian components of the nuclear momentum in atomic units.

Unit 20: Final coordinates.

The first line contains the trajectory index and potential energy in eV, followed by (one line for each atom)

1. Atomic symbol
2. Atomic mass in amu
3. The Cartesian coordinates in Å.

Unit 21: Final momenta.

The first line contains the trajectory index and kinetic energy in eV, followed by (one line for each atom)

1. Atomic symbol
2. Atomic mass in amu
3. The Cartesian components of the nuclear momentum in atomic units.

Unit 22: Intermediate coordinates; step interval printing is controlled by NPRINT.

The first line contains the number of atoms, and the second line contains trajectory index, the step index, the time (fs), and the potential energy in eV, followed by (one line for each atom)

1. Atomic symbol
2. The Cartesian coordinates in Å.

This file is essentially xyz format so that it can be visualized by various visualization programs, e.g. molden.

Unit 221: Adiabatic potential energies in eV. Each line contains: index of trajectory, time (fs), weight of the trajectory at the current time, mean potential energy, adiabatic

potential energies for electronic surface 1, 2, 3, ..., NSURFT. In case of single surface trajectory, mean potential and electronic surface 1 are the same values.

Unit 222: Upper triangle of density matrix elements. The representation of the density matrix is determined by REPFLAG keyword. Each line contains: index of trajectory, time (fs), weight of the trajectory at the current time, $(\text{Re}(\rho_{ij}), j = 1, nsurft), i = 1, nsurft)$.

Unit 223: Upper triangle of diabatic energy matrix (in eV). Each line contains: index of trajectory, time (fs), weight of the trajectory at the current time, $(U_{ij}, j = 1, nsurft), i = 1, nsurft)$.

Unit 23: Intermediate momenta; step interval printing is controlled by NPRINT. The first line contains the trajectory index, index of this geometry for this trajectory, the step index, the time (fs), and the kinetic energy in eV, followed by (one line for each atom)

1. Atomic symbol
2. Atomic mass in amu
3. The Cartesian components of the nuclear momentum in atomic units.

Unit 24 and Unit 25 are used to save the coordinates and momentum of a fragments during fragmentation analysis run (TERMFLAG=7) and are only written when a fragmentation occurs.

Unit 24: fragment coordinates.

The first line contains the trajectory index and fragment index for this dissociated trajectory, followed by (one line for each atom)

1. Original index
2. Atomic symbol
3. Atomic mass in amu
4. The Cartesian coordinates in Å.

Unit 25: fragment momentum.

The first line contains the trajectory index and fragment index for this dissociated trajectory, followed by (one line for each atom)

1. Original index
2. Atomic symbol
3. Atomic mass in amu
4. The Cartesian components of the nuclear momentum in atomic units.

Unit 26: Geometry at the end of momentum rescaling/temperature changing.

The first line contains the trajectory index, the times of the momentum rescalings/temperature changes, average temperature, and potential energy at this geometry, followed by (one line for each atom)

1. Atomic symbol
2. Atomic mass in amu
3. The Cartesian coordinates in Å.

Unit 27: Information on the dynamics. By default, some information is printed out at the beginning and at the end of the dynamics for mean-field approaches, but also at each allowed for surface-hopping methods.

This file contains the trajectory index, the current step, the current surface (the adiabatic surface n which the dynamics is performed for surface-hopping methods, but the adiabatic surface to which the average surface tends to decay for the CSDM method), the current time (related to the current step, and expressed in fs), the populations on each surface, and the adiabatic or diabatic energies (depending on the representation used for the dynamics).

Unit 28: Used by TFLAG1=5 only.

Optimized geometry. A geometry optimization is sometimes performed to calculate some thermal properties of the system during the dynamics. The first line contains the number of iterations needed for optimization, the optimized potential energy at this geometry, the current step at which the geometry is optimized, the current time (related to the current step, and expressed in fs), the average temperature, and is followed by the optimized geometry itself (one line for each atom):

1. Atomic symbol.
2. Atomic mass in amu.
3. The Cartesian coordinates in Å.

Unit 29: Information on geometries and relative translational energies between each H atom and NH₂ fragment for the NH₃ potential (printed out as often as Unit 27 for NH₃). When LMODPOP is false, each line contains the trajectory index, the current step, the current surface index, the current number of allowed hops (0 for mean-field approaches), the current time (related to the current step, and expressed in fs), the adiabatic and diabatic energies (in eV), the three relative translational energies between H and NH₂ (in eV), the three N-H distances (in Å), the three H-N-H angles (in deg), the nonplanarity angle (in deg, see Ref 14).

When LMODPOP is true, we also add the mode populations at the end of each line.

Remark 1: The definition of the current surface on which the dynamics is performed is not exactly the same within the framework of multi-surface simulations according to the dynamical method used. In surface hopping methods (TFS and FSTU methods), the current surface is the index of the surface on which the system has hopped. This surface may be a diabatic or adiabatic one, this depending on the chosen representation. When using mean-field methods with decay of mixing (SCDM and CSDM methods), the current surface is in fact the surface (diabatic or adiabatic) through which the system will relax to asymptotically reach a physical surface. The propagation in mean-field methods is indeed performed on an averaged surface.

Remark 2: Relative energies are derived from the subroutine RELENERG that was designed to give the three meaningful relative energies of NH₃ (that is, relative energies between H and NH₂).

Unit 30: Atom–diatom scattering output (for INITX=4 only).

Note: The rovibrational quantum numbers are not accurate for the semiclassical Ehrenfest method because the code assumes a single potential energy surface when the simulation terminates.

1. Trajectory index
2. Final surface label
3. Final arrangement label
Note: 1 = AB + C, 2 = BC + A, 3 = CA + B
4. Total time for the trajectory in (fs)
5. Total number of integration steps
6. Final value of the electronic state density matrix for state 1
7. Final value of the electronic state density matrix for state 2
8. Final total energy (eV)
9. Potential energy of the classical minimum of the final arrangement (eV)
10. Final kinetic energy corresponding to the relative atom–diatom translational motion (eV)
11. Final internal (rovibrational) energy of the diatomic fragment (eV)
12. Final vibrational energy of the diatomic fragment (eV)
13. Final rotational energy of the diatomic fragment (eV)
14. Final classical (unquantized) vibrational quantum number.
15. Final classical (unquantized) rotational quantum number.

Unit 31: Bimolecular collision output (for TERMFLAG=3 only)

1. Trajectory index
2. Final surface label
3. Final outcome index
4. Time in fs
5. Final relative translational energy in eV for fragment 1
6. Final angular momentum of fragment 1 about the origin in atomic units
7. Final angular momentum of fragment 1 about the center of mass of fragment 1
8. Final relative translational energy in eV for fragment 2
9. Final angular momentum of fragment 2 about the origin in atomic units
10. Final angular momentum of fragment 2 about the center of mass of fragment 2.

Unit 34: Geometries along tunneling paths.

The starting point, maximum of potential, and ending point of each accepted tunneling path are printed in this file in xyz format. This file can be visualized using *Molden*. The tunneling probability and weight of each path is printed along with the starting geometry.

Unit 340: Adiabatic, diabatic potential energies (in eV) and real part of density elements along tunneling path. Density matrix depends on representation used.

Every three lines contains following information

1. Length of tunneling path (Å), mean potential, adiabatic potential ($V_1, V_2, \dots, V_{\text{nsurft}}$)
2. Length of tunneling path (Å), diabatic potentials ($U_{ij}, j = 1, \text{nsurft}, i = 1, \text{nsurft}$)
3. Length of tunneling path (Å), density elements ($\text{Re}(\rho_{ij}), j = 1, \text{nsurft}, i = 1, \text{nsurft}$)

For each tunneling path, the first three lines are for starting of tunneling, the second three lines are for maximum-effective-potential point, and the last three lines are for the end of tunneling path.

Unit 40: Temperature ramping output.

Note: This output is written only if TFLAG1= 2, 3, or 4.

Data is written every time after momenta ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. Berry parameter (the relative second moment of the bond distances, averaged over all atom pairs)

$$\delta = \frac{2}{N(N-1)} \sum_i \sum_{j>i} \sqrt{(\langle R_{ij}^2 \rangle - \langle R_{ij} \rangle^2)} / \langle R_{ij} \rangle,$$

where N is the number of atoms and R_{ij} is the distance between atoms i and j .

6. Time average heat capacity in eV/K
7. Time average cohesive energy in eV/atom
8. Time average kinetic energy
9. Time average total energy
10. Time average sphericity L calculated by

$$L = \frac{I_{unique}}{I_{average}}$$

$$I_{unique} = I_i (i = i\delta \left[I_i - \max_{i=A,B,C} |I_i - I_{average}| \right])$$

$$I_{average} = \frac{1}{3} (I_A + I_B + I_C)$$

I_{unique} is the principal moment of inertia deviating most from the average. I_A , I_B , and I_C are the three principal moments of inertia

11. Standard deviation of L
12. Time average distance between the atoms and the CoM in Å:

$$RCoM = \left\langle \frac{1}{N} \sum_i |\vec{r}_i - \vec{r}_{CoM}| \right\rangle$$

13. Time average square distance between the atoms and the CoM in Å²:

$$RCoM2 = \left\langle \frac{1}{N} \sum_i |\vec{r}_i - \vec{r}_{CoM}|^2 \right\rangle$$

14. If file unit 50 is required, time average volume (in Å³) of the Atom Group (AG) calculated by an overlap sphere method (currently only pure aluminum is available)
15. If file unit 50 is required, standard deviation of the volume of the cluster calculated by the overlap sphere method
16. If file unit 50 is required, time average density (in g/cm³) of the AG calculated by the overlap sphere method

17. If file unit 50 is required, standard deviation of the density (in g/cm³) of the AG calculated by the overlap sphere method
18. Time average volume (in Å³) of the AG estimated by the radius of gyration method (Vol_g):

$$R_{g(i)} = \sqrt{I_i/M}, \quad i = 1-3,$$
 where $\{I_i, i = 1-3\}$ are the three principal moments of inertia. The volume of the cluster is calculated by:

$$Vol_g \approx \frac{4}{3} \pi \left(\frac{5}{2}\right)^{3/2} R_{g(1)} R_{g(2)} R_{g(3)}.$$
19. Standard deviation of the Vol_g
20. Time average density (in g/cm³) of the cluster calculated by the radius of gyration method
21. Standard deviation of the density (in g/cm³) calculated by the radius of gyration method.

Note: Entries 4 - 21 are calculated between temperature rescalings/changing.

Unit 41: Radial distribution function

Data is written for every NPRINT steps and at the end of each trajectory.

1. Trajectory index
2. Time in fs
3. A series of numbers representing the radial distribution function binned into equally spaced bins and averaged over the trajectory. The radial distribution function is normalized to unit area. The bin size [RBIN] is hard coded in RADIALDIST to be 1/8 the bulk Al nearest-neighbor distance (i.e., 1/8 of 4.02 Å)

Unit 42: Honeycutt-Andersen parameter.

This output is written when the temperature is rescaled (TFLAG1=2) and when each trajectory finishes.

For a definition of the Honeycutt-Andersen (HA) index see Ref. 29 in Section XV. Briefly, the HA index is a set of four indices which describes the local geometry of a bonded pair of atoms (i.e., a pair of atoms with a bond distance less than some cutoff distance R_{NN}). Here we record the fraction of bonded pairs $H(i, j, k, l)$ with HA indices (i, j, k, l) . R_{NN} is hard-coded in HONEY with the value 3.5 Å.

1. Trajectory index
2. Time in fs
3. The sum of $H(1, 2, k, l)$ for all k and l
4. The sum of $H(1, 3, k, l)$ for all k and l
5. The sum of $H(1, 4, k, l)$ for all k and l
6. The sum of $H(1, 5, k, l)$ for all k and l
7. The sum of $H(1, 6, k, l)$ for all k and l
8. $H(1, 4, 2, 1)$
9. $H(1, 4, 2, 2)$

Unit 43: Time average of the distance of each atom to the CoM.

Data is written at the end of momentum ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. RCoM in Å.
6. RCoM(*i*) of all the atoms:

$$RCoM(i) = \langle |\vec{r}_i - \vec{r}_{CoM}| \rangle$$

Unit 430: Same as unit 43 but written for every NPRINT steps.

Unit 44: Time average of the square distance of each atom to the CoM.

Data is written at the end of momentum ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. RCoM2 in Å.
6. RCoM2(*i*) of all the atoms:

$$RCoM2(i) = \langle |\vec{r}_i - \vec{r}_{CoM}|^2 \rangle$$

Unit 440: Same as unit 44 but written for every NPRINT steps.

Unit 45: Single-atom-Berry parameter of each atom.

Data is written at the end of momentum ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. Total Berry parameter
6. Single-atom-Berry parameter of all the atoms:

$$\delta_i = \frac{1}{N-1} \sum_{j \neq i} \sqrt{(\langle R_{ij}^2 \rangle - \langle R_{ij} \rangle^2)} / \langle R_{ij} \rangle$$

Unit 450: Same as unit 45 but written for every NPRINT steps.

Unit 46: Binned Berry parameter.

Data is written at the end of momenta ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs

4. Time average of the temperature
5. Total Berry parameter
6. Binned Berry parameter:

$$\delta_{bin_m} = \frac{1}{\langle N_{bin_m} \rangle} \sum_{i \in bin_m} \delta_i$$

$\langle N_{bin_m} \rangle$ is the time average of the number of atoms in bin m .

Unit 460: Same as unit 46 but written for every NPRINT steps.

Unit 49: Radial atom number distribution.

Data is written at the end of momentum ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. Time average of number of atoms in bins ($\langle N_{bin_m} \rangle$)

Unit 490: Same as unit 49 but written for every NPRINT steps.

Unit 500: Volume and density of the AG the overlap sphere method.

Data is written for every NPRINT steps. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. Time average volume (in \AA^3) of the AG calculated by the overlap sphere method
6. Standard deviation of the volume calculated by the overlap sphere method
7. Time average density (in g/cm^3) of the AG calculated by the overlap sphere method
8. Standard deviation of the density (in g/cm^3) of the AG calculated by the overlap sphere method

Unit 51: Binned RCoM.

Data is written at the end of momentum ramping or temperature changing. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Time average of the temperature
5. RCoM in \AA .
6. Binned RCoM:

$$RCoM_{bin_m} = \frac{1}{\langle N_{bin_m} \rangle} \sum_{i \in bin_m} RCoM(i)$$

Unit 510: Same as unit 51 but written for every NPRINT steps.

Unit 60: Initial structure data saved from the equilibration run for the first AG
Records (ITRAJ-1)*NATOM(1)+1 to ITRAJ*NATOM(1) is the x, y, z coordinates of the ITHAJth trajectory.

Unit 61: Initial momentum data saved from the equilibration run for the first AG.
Records (ITRAJ-1)*NATOM(1)+1 to ITRAJ*NATOM(1) is the x, y, z components of the momentum of the ITHAJth trajectory.

Unit 62: Initial structure data saved from the equilibration run for the second AG.
Records (ITRAJ-1)*NATOM(1)+1 to ITRAJ*NATOM(1) is the x, y, z coordinates of the ITHAJth trajectory.

Unit 63: Initial momentum data saved from the equilibration run for the second AG.
Records (ITRAJ-1)*NATOM(1)+1 to ITRAJ*NATOM(1) is the x, y, z components of the momentum of the ITHAJth trajectory.

Unit 77: Used only for reactive collision simulation.

Data are written every step. Each line contains:

1. Trajectory index
2. Step
3. Time in fs
4. Distance (in Å) between the CoMs of the two collision AGs
5. Kinetic energy (in eV) of the CoM motion of the first AG
6. Kinetic energy (in eV) of the CoM motion of the second AG (incident AG)
7. Projection of the CoM motion momentum (in atomic units) of the second AG (incident AG) onto the CoM vector between the two AGs ($\vec{R}_{CoM(2)} - \vec{R}_{CoM(1)}$)
8. Kinetic energy (in eV) of the projected CoM motion momentum of the second AG (incident AG).

XIV. Test suite

The test suite for using analytic potential energy surfaces is in the directories *tests_bimol/* and *tests_unimol/*, and the test suite for direct dynamics is in the directory *tests_dd/*.

XIV.A. Test suite for bimolecular processes using analytic potential energy surfaces

The entire test suite in the directory *tests_bimol/* may be compiled and run by executing

```
./runall
```

from the *tests_bimol/* directory. Notice that the *oh3_diatom_diatom* example may be slow. The generated outputs are placed in the *tests_bimol/output/* subdirectory. The output may be compared to output obtained using this version or previous versions of the code, stored in the subdirectory *tests_bimol/outputVN*, where *VN* is an *ANT* version number.

The following are brief descriptions of the runs in this test suite.

SINGLE-SURFACE RUNS

Al2-Al2-rx-normod-400-1.0.in

Ten trajectories simulating the collision of an Al₂ molecule with another Al₂ molecule using the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are prepared with normal mode analysis with randomly generated vibrational states. The initial rotational states of the two Al₂ are also randomly generated. The products are monitored with the fragment merge termination condition (TERMFLAG=4) with a default TERMSTEPS (50).

Al2-Al-rx-normod-400-1.0.in

Ten trajectories simulating the collision of an Al₂ molecule with an Al atom using the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are prepared with normal mode analysis with randomly generated vibrational states. The initial rotational states of the two Al₂ are also randomly generated.

Al-Al59-rx-2000.in

Three trajectories simulating the collision of an Al atom with an Al₅₉ cluster using the NP-B potential. This is a single-surface calculation (METHFLAG=0). The Al₅₉ cluster is equilibrated for 20000 fs before saving configurations for the later bimolecular collision simulation.

LiFH-u22.in

Three single-surface (METHFLAG=0) diabatic (REPFLAG=1) bimolecular trajectories for the LiFHJ potential. The initial conditions are set by INITX=4, and INITP is not used.

n2o-3pp.in

This is a single-surface run that tests the atom–diatom input for the case where ECOL, B_MIN, and B_MAX are specified.

OH+H2-rx-normod-1000-0.5.in

Two thousand trajectories simulating the bimolecular reactive collision of OH + H₂ using the OH3 potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are prepared with normal mode analysis with randomly generated vibrational states. The initial rotational states of OH and H₂ are also randomly generated. The products are monitored with OH bond forming condition (TERMFLAG=3). The reaction rate constant at 1000 K is calculated, and it is about 3.6 times of the experimental value.

MULTI-STATE RUNS

LiFH-SEa.in

Three trajectories for adiabatic (REPFLAG=0) semiclassical Ehrenfest (METHFLAG= 2) atom–diatom scattering calculations using the LiFHJ potential. The Bulirsch-Stoer integrator with the method of Hack et al. [Ref. 4 in Section XV] of calculating hopping probabilities (BULSTOINTHACK) is employed in this and in the other LiFH calculations. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INTP is not used.

LiFH-SEd.in

Three trajectories for diabatic (REPFLAG=1) semiclassical Ehrenfest (METHFLAG=2) atom–diatom scattering calculations using the LiFHJ potential. Note: the SE method gives identical trajectories for the adiabatic and diabatic representations for two electronic surfaces. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INTP is not used.

LiFH-v1.in

Three single-surface (METHFLAG=0) adiabatic (REPFLAG=0) bimolecular trajectories for the LiFHJ potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INTP is not used.

MCH-SCDMa.in

Three adiabatic-representation (REPFLAG=0) SCDM (METHFLAG=3) bimolecular trajectories for the MCH(SB) potential. This calculation involves two coupled electronic states. The Bulirsch-Stoer integrator with the method of Hack et al. [Ref. 4 in Section XV] of calculating hopping probabilities (BULSTOINTHACK) is employed in this and in the other MCH calculations. The initial conditions are set by INITX=4, and INTP is not used.

MCH-SCDMd.in

Three diabatic-representation (REPFLAG=1) SCDM (METHFLAG=3) trajectories for the MCH(SB) potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INTP is not used.

MCH-CSDMa.in

Three adiabatic-representation (REPFLAG=0) CSDM (METHFLAG=4) bimolecular trajectories for the MCH(SB) potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INITP is not used.

MCH-CSDMd.in

Three diabatic-representation (REPFLAG=1) CSDM (METHFLAG=4) bimolecular trajectories for the MCH(SB) potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INITP is not used.

oh3_diatom_diatom.in

This is an adiabatic representation OH + H₂ collision dynamics example with CSDM using the 3-state OH₃ surfaces published in *J. Chem. Phys.* **2019**, *151*, 104311. This example also shows how to use the diatom–diatom initial conditions.

o+o2_q1_quintetAp.in

This is a O+O₂ electronically nonadiabatic collision dynamics example with CSDM on adiabatic representation using the 6-state quintet A' surfaces. All trajectories start on the first quintet state.

o+o2_q2_quintetAp.in

This is a O+O₂ electronically nonadiabatic collision dynamics example with CSDM on adiabatic representation using the 6-state quintet A' surfaces. All trajectories start on the second quintet state. Notice that in the atom–diatom region, the first and second electronic states are degenerate.

YRH-FSa.in

Three adiabatic-representation (REPFLAG=0) fewest-switches surface hopping (METHFLAG=1) trajectories for the YRH(0.2) potential. This calculation involves two coupled electronic states. The Bulirsch-Stoer integrator with the method of Hack et al. [Ref. 4 in Section XV] of calculating hopping probabilities (BULSTOINTHACK) is employed in this and in the other YRH calculations. The initial conditions are set by INITX=4, and INITP is not used.

YRH-FSd.in

Three diabatic-representation (REPFLAG=1) fewest-switches surface hopping (METHFLAG=1) trajectories for the YRH(0.2) potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INITP is not used.

YRH-FSTUa.in

Three adiabatic-representation (REPFLAG=0) fewest-switches with time uncertainty surface hopping (METHFLAG=5) trajectories for the YRH(0.2) potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INITP is not used.

YRH-FSTUd.in

Three diabatic-representation (REPFLAG=1) fewest-switches with time uncertainty surface hopping trajectories (METHFLAG=5) for the YRH(0.2) potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=4, and INITP is not used.

XIV.B. Test suite for unimolecular processes using analytic potential energy surfaces

The test suite for unimolecular processes in the directory *tests_unimol/* may be compiled and run by executing

```
./runall
```

from the *tests_unimol/* directory. Notice the thioanisole_kCSDMa example may be slow. The generated outputs are placed in the *tests_unimol/output/* subdirectory. The output may be compared to output obtained using previous versions of the code, stored in the subdirectory *tests_unimol/outputVN*, where *VN* is an *ANT* version number.

The following are brief descriptions of the runs in this test suite.

SINGLE-SURFACE RUNS

A12-opt.in

Steepest descent minimization of Al₂ using the NP-B potential. This is a single-surface calculation (METHFLAG=0). This run tests the steepest-descent option (TFLAG1 = 1). The initial conditions are set by INITX=1 and INITP=0. The termination condition is the RMS of gradient smaller than 0.0001 eV/Å (TERMFLAG= 2, T_GRADMAG=0.0001).

A13-frag.in

100 trajectories of unimolecular dissociation simulation of Al₃, propagated for 20000 time steps using the fourth-order Runge-Kutta integrator with a time step of 2.0 fs and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial geometry is the global minimum. The initial conditions are prepared with an equilibration run whose initial conditions are prepared by normal mode analysis. The temperature of the system is controlled using a Nosé-Hoover two-chain thermostat with system characteristic frequency of 0.05 1/fs.

A113-melt.in

One trajectory of the simulated heating of Al₁₃, propagated using the fourth-order Runge-Kutta integrator with a time step of 2.0 fs and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial geometry is the global minimum. The initial conditions are prepared by normal mode analysis. The temperature of the system is controlled using a Nosé-Hoover two-chain thermostat with system characteristic frequency of 0.05 1/fs. The Atom Group (AG) is heated from 1100 K to 1300 K with a

temperature step of 100 K. At each temperature, the temperature is controlled by the thermostat for 11 ps, with the last 10 ps used to average various properties.

[Al20-ransph-dyn-nvt-400-1.0-BS.in](#)

Three trajectories of randomized Al₂₀ clusters, propagated for 1000 time steps using the Bulirsch-Stoer integrator and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are set by INITX=1 (in a sphere with radius 6 Å) and INITP=1. The temperature of the system is controlled using a Berendsen thermostat with a default HSTEP0/TAUT=0.0025.

[Al20-rancub-dyn-nvt-400-1.0-RK4.in](#)

Three trajectories for randomly generated Al₂₀ clusters, propagated for 1000 time steps using the fourth-order Runge-Kutta integrator and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are set by INITX=2 (in a cubic cell with length 6 Å) and INITP=1. The temperature of the system is controlled using a Berendsen thermostat with a default HSTEP0/TAUT=0.0025.

[Al20-ransph-dyn-nvt-400-1.0-RK4.in](#)

Three trajectories for randomly generated Al₂₀ clusters, propagated for 1000 time steps using the fourth-order Runge-Kutta integrator and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are set by INITX=1 (in a sphere with radius 6 Å) and INITP=1. The temperature of the system is controlled using a Berendsen thermostat with a default HSTEP0/TAUT=0.0025.

[Al20-ransph-dyn-nvt-400-1.0-nh-RK4.in](#)

Three trajectories for randomly generated Al₂₀ clusters, propagated for 1000 time steps using the fourth-order Runge-Kutta integrator and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are set by INITX=1 (in a sphere with radius 6 Å) and INITP=1. The temperature of the system is controlled using a Nosé-Hoover two-chain thermostat with a system characteristic frequency of 0.05 1/fs.

[Al20-ransph-dyn-nvt-400-1.0-an-RK4.in](#)

Three trajectories for randomly generated Al₂₀ clusters, propagated for 1000 time steps using the fourth-order Runge-Kutta integrator and the NP-B potential. This is a single-surface calculation (METHFLAG = 0). The initial conditions are set by INITX=1 (in a sphere with radius 6 Å) and INITP=1. The temperature of the system is controlled using an Andersen thermostat with a collision frequency of 0.01 1/fs.

[Al20-arb-dyn-nvt-400-1.0-RK4.in](#)

Three trajectories for randomly generated Al₂₀ clusters, propagated for 1000 time steps using the fourth-order Runge-Kutta integrator and the NP-B potential. This is a single-surface calculation (METHFLAG=0). The initial conditions are set by INITX=3 (arbitrary shape) and INITP=1. The temperature of the system is controlled using an Andersen thermostat with a default HSTEP0/TAUT=0.0025.

HN2-tunneling.in

Ten single-surface trajectories for H-N dissociation. Tunneling is included using the army ants tunneling algorithm. The total energy is 0.65 eV, and initial conditions are selected with INITX=0 and INITP=1.

HN2-tunneling.in

Ten single-surface trajectories for H-N dissociation. Tunneling is included using the army ants tunneling algorithm. The total energy is 0.65 eV, and initial conditions are selected with INITX=0 and INITP=1.

MULTI-STATE RUNS

CH2BrCIPES-CSDMd7en50ev.in

Two diabatic-representation (REPFLAG=1) CSDM (METHFLAG=4) spin-coupled photodissociation trajectories for the BrCH₂Cl dissociation system. The initial conditions are prepared for $\nu=0$ vibrational state of the ground-state potential for all normal modes, using a Wigner distribution generated by using the Box-Muller algorithm [Refs. 2 and 3 in Section XV]. The Bulirsch-Stoer integrator with the method of Hack et al. [Ref. 4 in Section XV] (BULSTOINTHACK) is employed. The option for minimal printout of the selection of initial conditions step (MINPRINTICON) is defined. The dynamics starts in the $n=7$ potential at constant energy (5 eV) and the trajectory dissociates in electronic state $n=7$ to produce Br(²P_{3/2}) + CH₂Cl(X¹A').

HBr-FSTUa.in

One hundred adiabatic-representation (REPFLAG=0) FSTU (METHFLAG=5) spin-coupled photodissociation trajectories for the HBr diatomic (see Ref. 11 in Section XV). The initial conditions are prepared for $\nu=0$ vibrational state of the ground-state potential using a Wigner distribution generated by using the Box-Muller algorithm [Refs. 2 and 3 in Section XV] with projected Hessian for the initial normal mode (NTRAPZ=1). The Bulirsch-Stoer integrator with the method of Hack et al. [Ref. 4 in Section XV] of calculating hopping probabilities (BULSTOINTHACK) is employed. The option for minimal printout of the selection of initial conditions step (MINPRINTICON) is defined. The dynamics starts in the $n=8$ potential at constant energy (7 eV) corresponding to the spin-orbit coupled ¹Π₁ state and dissociates in three different electronic states ($n=4$ corresponding to ³Π₁, $n=8$ corresponding to ¹Π₁, and $n=11$ corresponding to ³Σ₁). The first two electronic states correlate with bromine in its lower fine-structure level (H(²S) + Br(²P_{3/2})) and the third electronic state correlates with the bromine higher fine-structure level (H(²S) + Br(²P_{1/2})).

HBr-FSTUSDa.in

One hundred adiabatic-representation (REPFLAG=0) FSTU/SD (METHFLAG=5, STODECOFLAG=1) spin-coupled photodissociation trajectories for the HBr diatomic (see Ref. 11 in Section XV). The initial conditions and the rest of options are the same as for the 'HBr-FSTUa.in' job.

HBr-CSDMa.in

One hundred adiabatic-representation (REPFLAG=0) CSDM (METHFLAG=4) spin-coupled photodissociation trajectories for the HBr diatomic (see Ref. 11 in Section XV). The initial conditions and the rest of options are the same as for the FSTU and FSTU/SD jobs.

nh3-SCDMa.in

One adiabatic-representation (REPFLAG=0) SCDM (METHFLAG=3) photodissociation trajectory for the nh3potg-new potential. This calculation involves two coupled electronic states. The Bulirsch-Stoer integrator with the method of Hack et al. [Ref. 4 in Section XV] of calculating hopping/switching probabilities (BULSTOINTHACK) is employed in this and in the other NH₃ calculations. The initial conditions are set by INITX=1, VIBSELECT=2, and INITP is not used.

nh3-SCDMd.in

One diabatic-representation (REPFLAG=1) SCDM (METHFLAG=3) photodissociation trajectory for the nh3potg-new potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=1, VIBSELECT=2, and INITP is not used.

nh3-CSDMa.in

One adiabatic-representation (REPFLAG=0) CSDM (METHFLAG=4) photodissociation trajectory for the nh3potg-new potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=1, VIBSELECT=2, and INITP is not used.

nh3-CSDMd.in

One diabatic-representation (REPFLAG=1) CSDM (METHFLAG=4) photodissociation trajectory for the nh3potg-new potential. This calculation involves two coupled electronic states. The initial conditions are set by INITX=1, VIBSELECT=2, and INITP is not used.

nh3-FSTUa.in

Three adiabatic-representation (REPFLAG=0) FSTU (METHFLAG=5) photodissociation trajectories for the nh3potg-new potential. The frustrated hops are ignored (FRUSMETH=0). This calculation involves two coupled electronic states starting from the vibrational ground state of the first electronic excited state minimum of NH₃. The initial conditions are set by INITX=1, VIBSELECT=1, and VIBDIST=0, and INITP is not used. The projected Hessian is used to generate initial conditions, but TRAPZ-like methods are not used during the dynamics (NTRAPZ=1).

nh3-FSTUd.in

Three diabatic-representation (REPFLAG=1) FSTU (METHFLAG=5) photodissociation trajectories for the nh3potg-new potential. The frustrated hops are treated using the gradV method (FRUSMETH=2). This calculation involves two coupled electronic states starting from the vibrational ground state of the first electronic excited state minimum of NH₃. The initial conditions are set by INITX=1, VIBSELECT=1, and VIBDIST=0, and INITP is not used.

nh3-FSTUSDamTRAPZ.in

One adiabatic-representation (REPFLAG=0) FSTU/SD (METHFLAG=5) photodissociation trajectory for the nh3potg-new potential. This calculation involves two coupled electronic states starting from the vibrational ground state of the first electronic excited state minimum of NH₃. The initial conditions are set by INITX=1, VIBSELECT=1, VIBDIST=0, and INITP is not used. The projected Hessian is used to generate initial conditions, and the mTRAPZ method is used in the dynamics (NTRAPZ=3, NVERS=1). The option for minimal printout of information related to TRAPZ-like methods (MINIPRINTTRAPZ) is used.

nh3-FSTUSDa.in

One adiabatic-representation (REPFLAG=0) FSTU/SD (METHFLAG=5) photodissociation trajectory for the nh3potg-new potential. This calculation has most of its input options defined as in the previous calculation, but here the unprojected Hessian is used to generate initial conditions and none of the TRAPZ-like methods is used in the dynamics (NTRAPZ=0).

nh3-FSTUaSaddle.in

Three adiabatic-representation (REPFLAG=0) FSTU (METHFLAG=5) photodissociation trajectories for the nh3potg-new potential. This calculation starts at the saddle point of the excited adiabatic PES (V2). The initial conditions are set by INITX=0, INITP=-1, VIBSELECT=1, VIBDIST=0, and VIBTYPE=1. The bound modes at the saddle point are at their ground state and an energy of 0.1 eV is added along the positive direction of the unbound normal mode.

phohaprp-CSDMtunn.in

One three-surface trajectory for phenol photodissociation using anchor-points reactive potentials. This example performs CSDM in the adiabatic representation. Nonadiabatic tunneling is included using the army ants tunneling algorithm. The initial conditions are selected with INITX=0, INITP=-1, VIBSELECT=5 VIBDIST=1 keywords for a state-selected initial condition with the initial population on adiabatic state 2 (using NSURFI=2 and NSURF0=2). The vibrational energies for each vibrational state are specified by keyword VIBENE. Note carefully that this test isn't actually long enough to observe a successful tunneling event. To properly test this option the integration time should be greatly increased, but then the run will be very expensive.

thioanisole-kCSDMa.in

One three-surface trajectory for thioanisole photodissociation using anchor-points reactive potentials. This is an example using curvature-driven CSDM method, which uses the adiabatic representation

XIV.C. Direct dynamics test suite

Two test runs for direct dynamics are in the *tests_dd/* directory. In each subdirectory, a .pbs file is given to illustrate how to run the job in a system with the PBS scheduler.

SINGLE-SURFACE RUNS

DH2

This test run is for the reactive collision of D with H₂ in the ground electronic state. The *Gaussian09* package is used for energy and gradient calculations on the fly (QCPACK=1). The potential energy surface is calculated by the MP2/6-31G(d) method.

Gaussian16_DH2_MP2

This test run is for a reactive collision of D with H₂ in the ground electronic state. The *Gaussian16* package is used for energy and gradient calculations on the fly (QCPACK=1). The potential energy surface is calculated by the MP2/6-31G(d) method.

HCOH-torsion

Ten trajectories for the isomerization of *cis*-HCOH to *trans*-HCOH in the ground electronic state. The potential energy (PM3/PDDG) is calculated by the *MOPAC-mn* program. Tunneling is included using the army ants tunneling algorithm.

HCOH-Htransfer

Ten trajectories for the H transfer reaction in the ground electronic state. The potential energy (PM3/PDDG) is calculated by the *MOPAC-mn* program. Tunneling is included using the army ants tunneling algorithm

Molpro_DH2_CASSCF

This test run is for a reactive collision of D with H₂ in the ground electronic state. The *Molpro* package is used for energy and gradient calculations on the fly (QCPACK=2). The potential energy surface is calculated by the CASSCF/6-31G** method.

MULTI-STATE RUNS

Molpro_ethylene

This test run is for CSDM nonadiabatic dynamics of ethylene calculated in the adiabatic representation with three states. The *Molpro* package is used for energy and gradient calculations by direct dynamics, i.e., “on the fly” (QCPACK=2). The potential energy surface is calculated by the SA-CASSCF/6-31G** method, where 6-31G** is the same as 6-31G(d,p).

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XVI. Parallelization

The six nested loops in the subroutine *getdvec3.for* are parallelized by using the OpenMP DO directive. This collapses loops and thereby speeds calculations with a large number of electronic surfaces, e.g., the CH₂BrCl molecule with 24 surfaces.

If the potential is parallelized with OpenMP, the program can run as a parallel computation. Two potentials in *pot/* directory are parallelized with OpenMP; they are *BrCH2Cl-openmp.for* and *NP-Bd-v3-openmp.for*. To use more than one processors, one could use the shell environment variable to specify the number of threads to be used, for example

```
export OMP_NUM_THREADS = 8 (in bash)
setenv OMP_NUM_THREADS 8 (in tcsh)
```

Note that the suffix *.for* is reserved for the OpenMP code in the Makefile so that all the files with *.for* suffix have the correct compiler flags for OpenMP.

XVII. Appendices

A1. Generation of initial conditions (appendix to sections IV.A and IV.C)

Rotational states

For a linear AG, if a rotational quantum state is not provided, the program will randomly generate rotational states with a Boltzmann distribution:

1. Generate a random number ξ .
2. $E_{\text{rot}} = -k_B T \ln(1-\xi)$
3. Since $E_{\text{rot}} = \frac{J(J+1)}{2I}$ (in atomic units), where I is the inertia of rotation of the AG, thus the quantum rotational number J can be obtained by solving

$$J^2 + J + 2Ik_B T \ln(1-\xi) = 0$$
4. Once the rotational state J and the corresponding rotational energy

$$E_{\text{rot}} = \frac{J(J+1)}{2I}$$

are obtained, from

$$E_{\text{rot}} = \frac{1}{2} I \dot{\theta}^2$$

$$\dot{\theta} = \sqrt{\frac{2E_{\text{rot}}}{I}}$$

Then

$$\dot{\theta} = \frac{\sqrt{J(J+1)}}{I} \text{ and } p_{i\perp} = m_i r_i \dot{\theta}$$

where $p_{i\perp}$ is the momentum component of atom i perpendicular to the axis where the AG is on, r_i is the distance between the atom and the center of mass of this AG.

5. Generate another random number ξ_i to generate the direction of $\dot{\theta}$.
6. Add $p_{i\perp}$ to original p_i .

For non-linear AG, the steps to generate $p_{i\perp}$ is similar to linear AG, except that E_{rot} generated is $-0.5 k_B T \ln(1-\xi)$, there is no step 3 to calculate J , and steps 1 to 5 (without 3) are repeated 3 times to produce three sets of $\dot{\theta}$ and thus three rotational momenta ($I\dot{\theta}$) around each principal axis of rotation. In step 6, NOANG is called to add the rotational momenta onto the original momenta (See III.B).

Vibrational states

The Boltzmann-like distribution of vibrational quantum numbers is determined as follows:

1. Frequencies are firstly calculated in subroutine NORMOD called by PREMOL.

2. Generate a random number ξ .
3. Vibrational energy of i th vibrational mode: $E_{\text{vib}(i)} = -k_B T \ln(1 - \xi) = n_m \omega_m$, n_m is the vibrational quantum number and ω_m is the vibrational frequency in atomic units.
4. Vibrational quantum number $n_m = -\frac{k_B T \ln(1 - \xi)}{\omega_m}$
5. Steps 2-4 are repeated until $3 * N - 5$ (or 6) (N is the atom number of this AG) vibrational quantum numbers are generated.

Once vibrational quantum numbers are generated, the following steps are used to generate the initial momenta and position of the atoms. [Steps 1–7 are performed in NORMOD, which is called by PREMOL.]

1. The Hessian is computed numerically

$$H_{ij,i'j'} = \left[\nabla V(\mathbf{X}_0 + h\hat{X}_{ij}) - \nabla V(\mathbf{X}_0 - h\hat{X}_{ij}) \right]_{ij,i'j'} / 2h$$
 where i and i' run over atoms, j and j' run over x,y,z, h is the step size for the numerical second derivative, and the notation $\nabla V(\mathbf{X}_0 + h\hat{X}_{ij})$ indicates the gradient at a geometry where a small step (of magnitude h) is taken away from the initial structure in the direction of X_{ij} . Currently, h is hard-coded to be 0.00001 a0.

2. The Hessian is mass-scaled

$$H_{ij,i'j'} \rightarrow H_{ij,i'j'} \frac{\mu}{\sqrt{M_j M_{j'}}} \text{ [HESS]}$$

where μ [MU] is hard-coded in PARAM and has the value 1 amu.

3. The Hessian is diagonalized using the LAPACK routine DSYEV.
4. The 6 or 5 smallest eigenvalues (7 or 6 when this is a saddle point) are automatically ignored without any checks (to see if the system is linear, for example).
5. The remaining eigenvalues λ_m (force constants) are converted to harmonic frequencies

$$\omega_m = \sqrt{\lambda_m / \mu} \text{ [FREQ]}$$

where λ_m labels the modes in order of decreasing magnitude.

6. The mass-scaled eigenvectors \hat{X}_m^{ij} are stored, where j labels atoms, and i labels x,y,z.
7. The user specifies the vibrational quantum number n_m [NMQN] for each mode, and the energy for each mode is computed

$$E_m^{\text{HO}} = \hbar \omega_m (n_m + 1/2)$$

Steps 8–13 are performed in POPNORM.

8. The turning points are computed from

$$R_m^\pm - R_m^0 = \sqrt{\frac{2E_m^{\text{HO}}}{\omega_m^2 \mu}} \text{ [RTURN]}$$

9.

- a) VIBDIST=0 or $n_m \neq 0$ (Classical harmonic oscillator): Random numbers ζ_m are obtained, and displacements are made about the minimum energy structure

$$X^{ij} = X_0^{ij} + \sum_m \hat{X}_m^{ij} (R_m^\pm - R_m^0) \cos(2\pi\zeta_m), \text{ [XXNM]}$$

where $\{X_0^{ij}\}$ is the initial mass-scaled geometry.

- b) VIBDIST=1 (Semi-classical harmonic oscillator): Two random numbers ζ_m and ξ_m' are obtained, and displacements are made about the minimum energy structure

$$X^{ij} = X_0^{ij} + \sum_m \hat{X}_m^{ij} \sigma_m^X \sqrt{-2 \ln \xi_m} \cos(2\pi\zeta_m), \text{ [XXNM]}$$

where $\sigma_m^X = \sqrt{\frac{1}{2\mu\omega_m}}$.

- c) VIBDIST=2 (Quantum Wigner distribution): Same as b).

10.

- a) VIBDIST=0 or $n_m \neq 0$: Calculate the kinetic energy of the m th normal mode:

$$T_m = E_m^{\text{HO}} - \frac{1}{2} \omega_m^2 \mu \left[(R_m^\pm - R_m^0) \cos(2\pi\zeta_m) \right]^2 \text{ [KINHO]}$$

The random numbers ζ_m are the same as used in 9a)

- b) VIBDIST=1: The same as a), repeat step 9b) until $T_m \geq 0$.
c) VIBDIST=2: none

11.

- a) VIBDIST=0 or $n_m \neq 0$: The velocity is set to

$$\dot{X}^{ij} = \dot{X}_0^{ij} \pm \sum_m \hat{X}_m^{ij} \sqrt{2T_m / \mu}, \text{ [VVNM]}$$

where for a saddle point, the translational energy along the unbound normal mode is added separately.

The sign is randomized for each mode m .

- b) VIBDIST=1: The same as a).
c) VIBDIST=2: The velocity is set to

$$\dot{X}^{ij} = \dot{X}_0^{ij} \pm \sum_m \hat{X}_m^{ij} \sigma_m^P \sqrt{-2 \ln \xi_m} \sin(2\pi\xi_m') / \mu, \text{ [VVNM]}$$

where $\sigma_m^P = 1/(2\sigma_m^X)$, and the two random numbers are the same as used in 9b).

12. Finally, the quantities are transformed back to unscaled coordinates, and the velocity is converted into momentum.

$$X^{ij} \leftarrow X^{ij} \sqrt{\frac{\mu}{m_j}}$$

$$P^{ij} \leftarrow \dot{X}^{ij} \sqrt{\frac{\mu}{m_j} m_j}$$

Comparison of different distributions

The following plots are prepared using the ammonia potential energy surface (nh3potg.f). The distributions are always obtained for the vibrational ground state of mode 3 (asymmetric stretch) of the first electronic adiabatic excited state (V_2) of ammonia.

Figure 2 Normalized distribution of mass scaled displacement (mass scaled Bohr) of the third normal mode of the planar minimum of ammonia on the V_2 adiabatic potential energy surface.

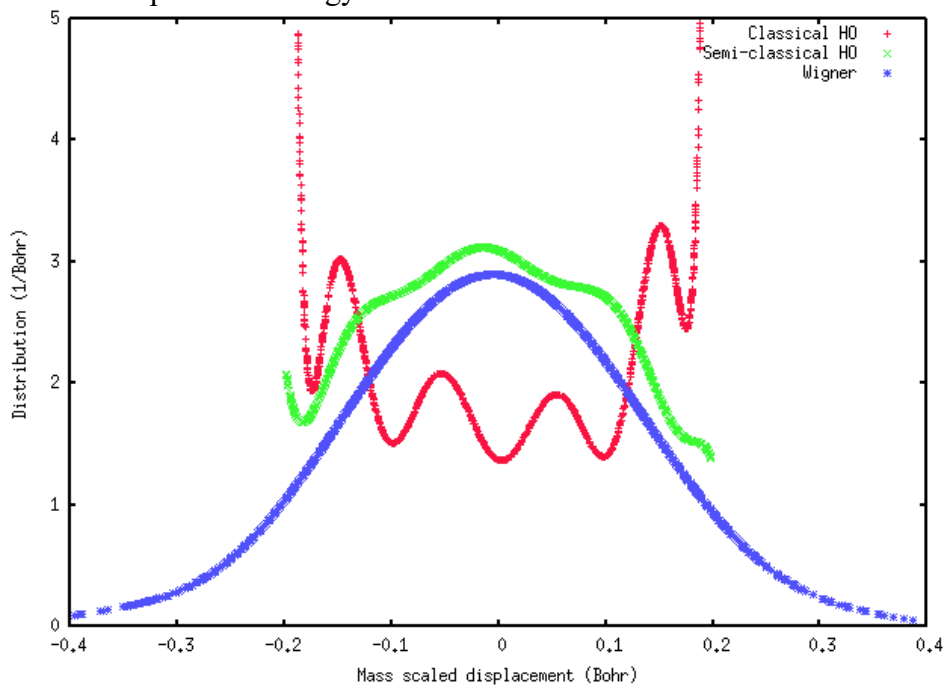
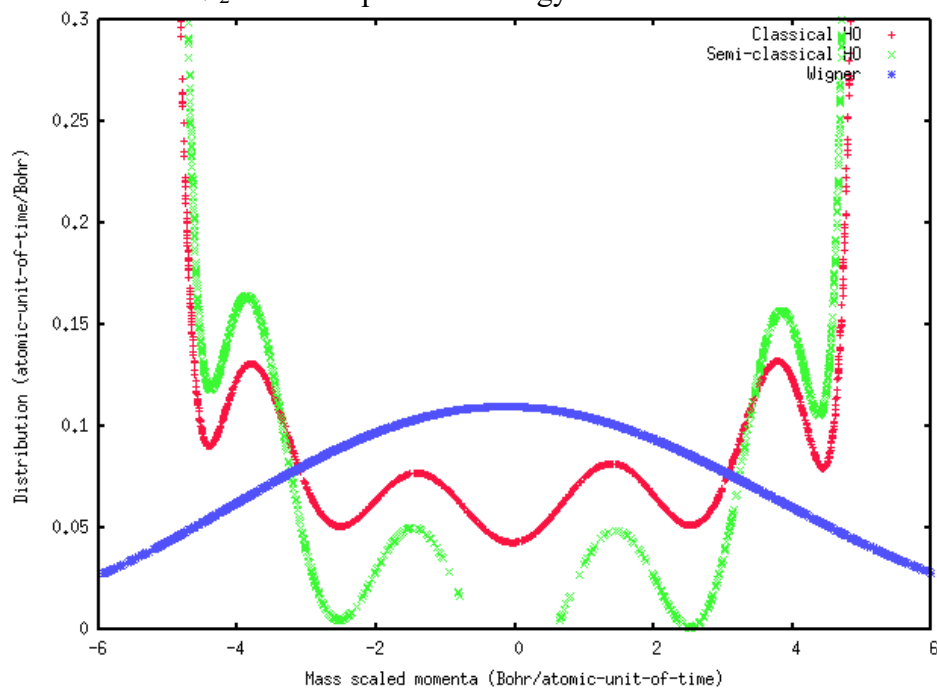


Figure 3 Normalized distribution of mass scaled momentum (mass scaled Bohr/atomic-unit-of-time) of the third normal mode of the planar minimum of ammonia on the V_2 adiabatic potential energy surface.



Notice that for the classical and semi-classical harmonic oscillators, the displacements fall into the range of $[R_m^- - R_m^0, R_m^+ - R_m^0]$.

Figure 4 Normalized distribution of total kinetic energy of the planar minimum of ammonia on the V_2 adiabatic potential energy surface.

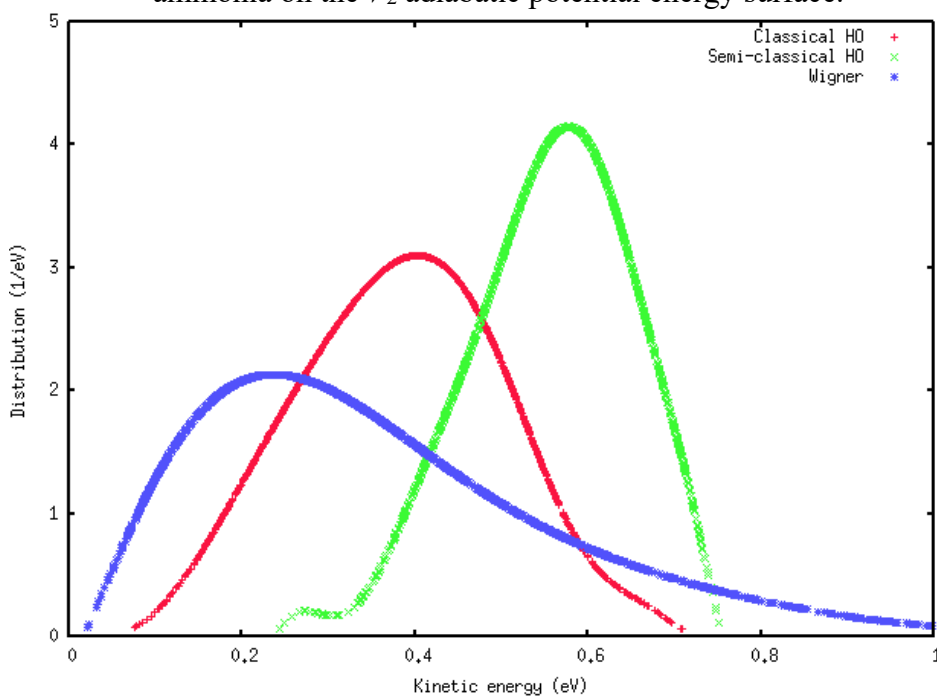


Figure 5 Normalized distribution of potential energy of the planar minimum of ammonia on the V_2 adiabatic potential energy surface.

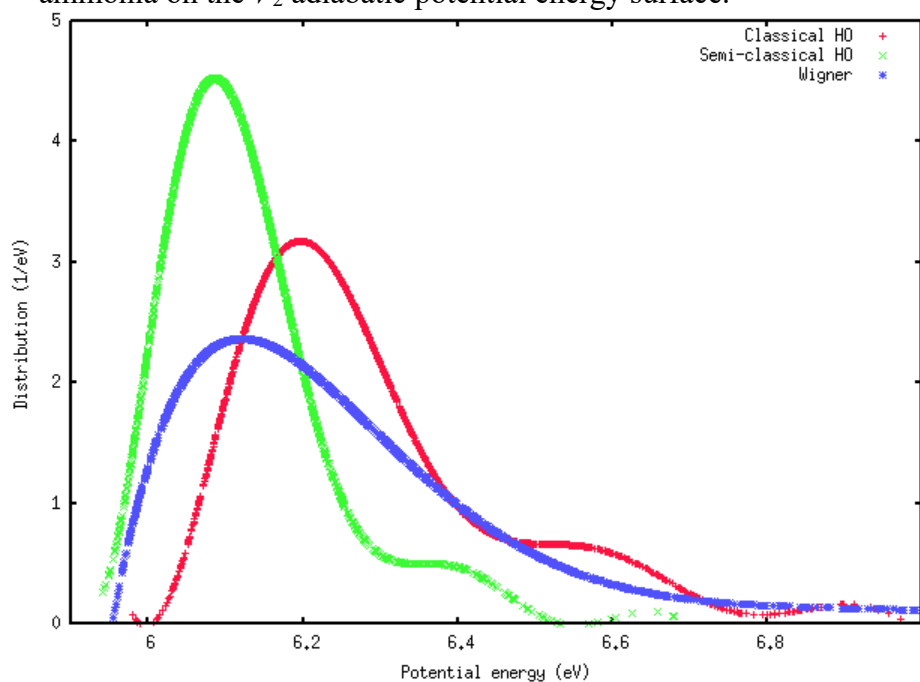


Figure 6 Normalized distribution of total energy of the third normal mode of the planar minimum of ammonia on the V_2 adiabatic potential energy surface.

Generation of initial condition between two AGs in a reactive collision run

a) Initial relative position between two AGs in a reactive collision run

1. The user provides or the program will generate a maximum distance R_0 (input parameter $R_0COLLISION$) between two AGs
2. Place the center of mass (CoM) of the first AG at the origin of the coordinate system.
3. Generate a random number ξ .
4. Calculate $b_1 = R_0\sqrt{\xi}$, $b_2 = R_0\sqrt{1-\xi}$. If the user provides b_1 (impact parameter, input parameter $B_0IMPACT$), b_2 is set as $\sqrt{R_0^2 - b_1^2}$;
5. Set the CoM coordinate of the second AG as:
 $COMXX(1,2) (x) = 0.0$
 $COMXX(2,2) (y) = b_1$
 $COMXX(3,2) (z) = -b_2$
 where $COMXX(i,2)$, $i = 1, 3$ are the coordinates of the CoM of the second AG.

b) Initial relative translation between two AGs in a reactive collision run

1. Generate a random number ξ .
2. Calculate u by an iterative method, initial guess $u_1=1$:

$$u_{i+1} = u_i + \frac{u_i + 1 + (1 - \xi)e^{u_i}}{u_i}$$

3. Relative translation energy $E_{\text{trans}}=u k_B T$.
4. Set all the x and y components of the CoM momentum of both the two AGs as zero, while the z component of the first AG as $-\sqrt{2\mu E_{\text{trans}}}$, and that of the second AG as $\sqrt{2\mu E_{\text{trans}}}$, where μ is the reduced mass of the two AG.

A2. Choice of thermostats

Currently, three thermostats are implemented: Andersen thermostat, Berendsen thermostat, and Nosé-Hoover thermostat with two chains.

The Berendsen thermostat is the least expensive one, but it fails for diatomic systems if too small of a value of TAUT value is set, but even with large TAUT, it still cannot reproduce the correct canonical momentum distribution for diatomic systems.

The Andersen thermostat and the Nosé-Hoover thermostat with two chains (hereafter called the NH thermostat) can both well reproduce the correct canonical momentum distribution for diatomic systems. However, it is well known that the Andersen thermostat does not give a continuous trajectory and its kinetic properties are greatly affected by the VFREQ value (the value determining how often the momentum of an atom is reset). Basically any result can be obtained by changing VFREQ. Nevertheless, the average static properties, such as the energies, are well predicted by the Andersen thermostat.

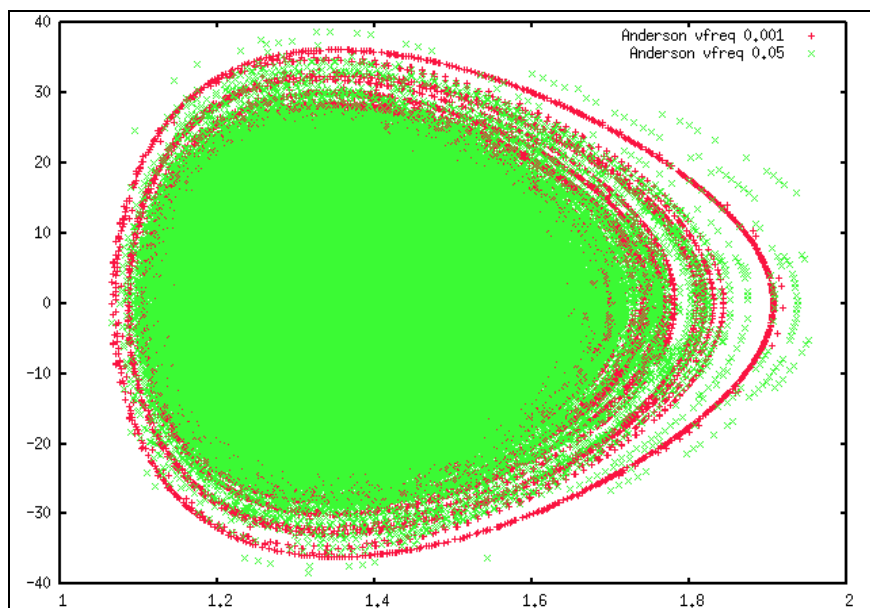
The NH thermostat seems to be the best of the three methods, but there are still debates about this. Although the results are not very sensitive to the choice of the QNOSE value (the “MASS” of the two additional thermostat degrees of freedom), Nosé suggested that QNOSE should properly be chosen so that the oscillation period of the added degree of freedom is equal to the typical vibrational period of the system studied or the collision period of the system with the bath [Ref. 30 in Section XV]. The actual QNOSE value is calculated using the following equation by setting $\langle s \rangle^2 = 1$.

$$Q_{\text{nose}} = \frac{2fk_B T}{\langle s \rangle^2} \left(\frac{t_0}{2\pi} \right)^2,$$

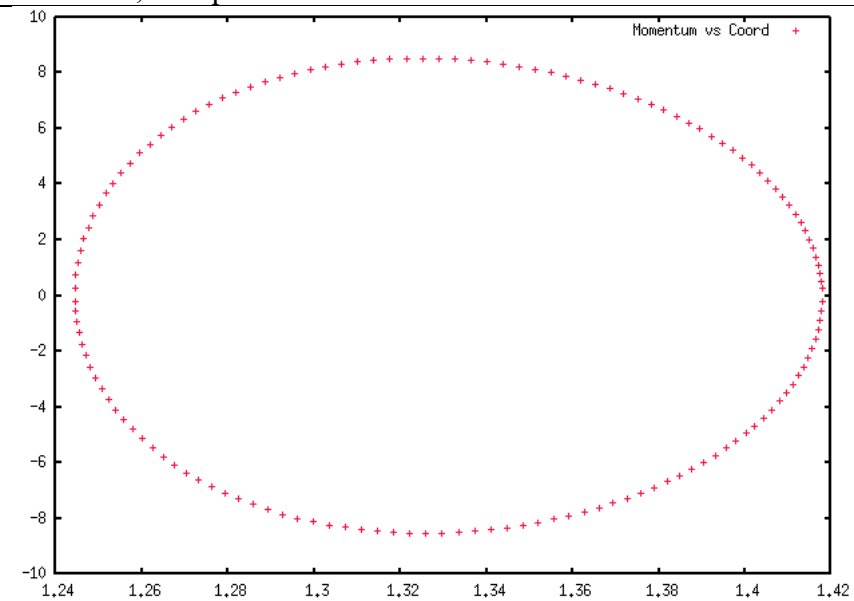
where t_0 is the vibrational period of collision, and f is the number of degrees of freedom of the system.

A comparison of the three thermostats for aluminum dimer:

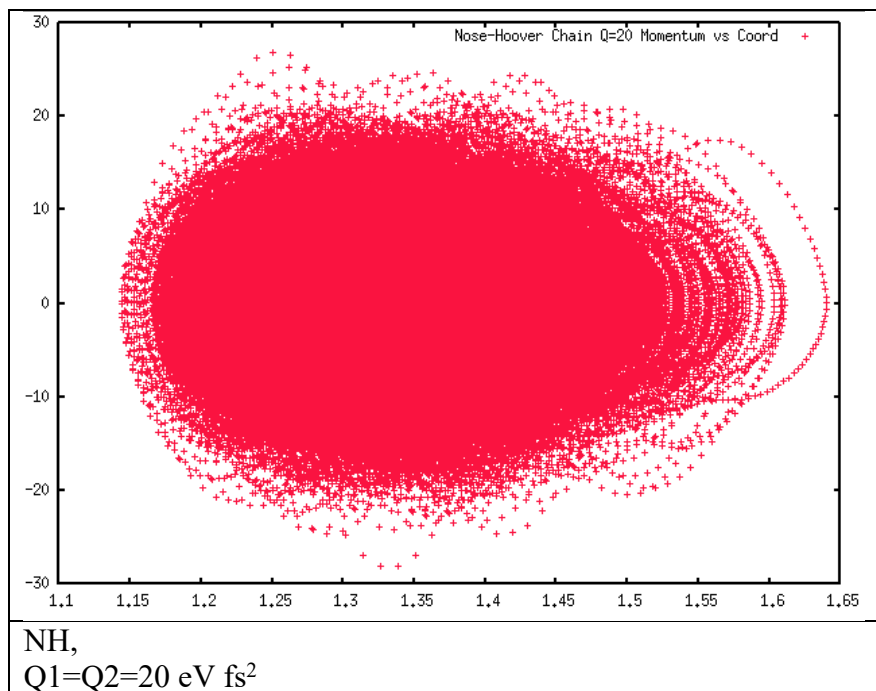
1. Plots of momentum of one Al atom with respect to half of the Al-Al bond distance.



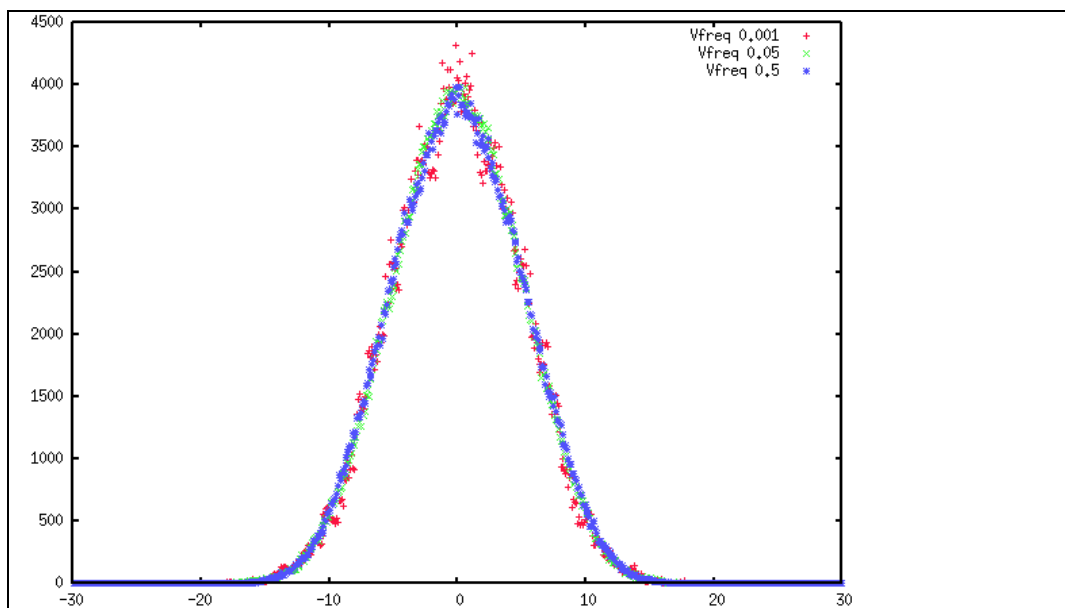
Andersen, vfreq=0.001 and 0.05 1/fs



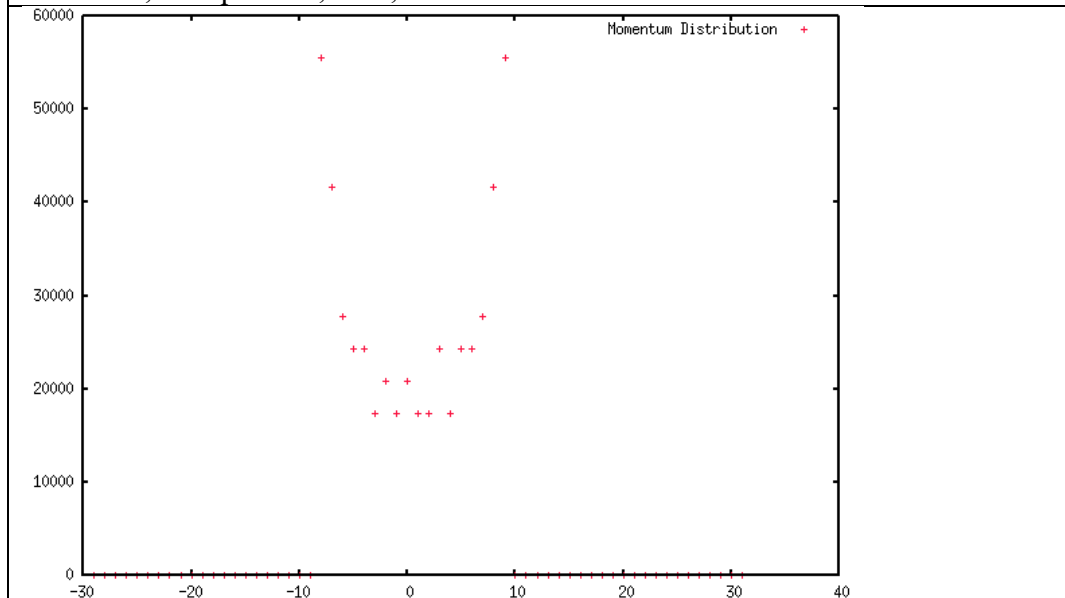
Berendsen, $\tau = 1000$ fs



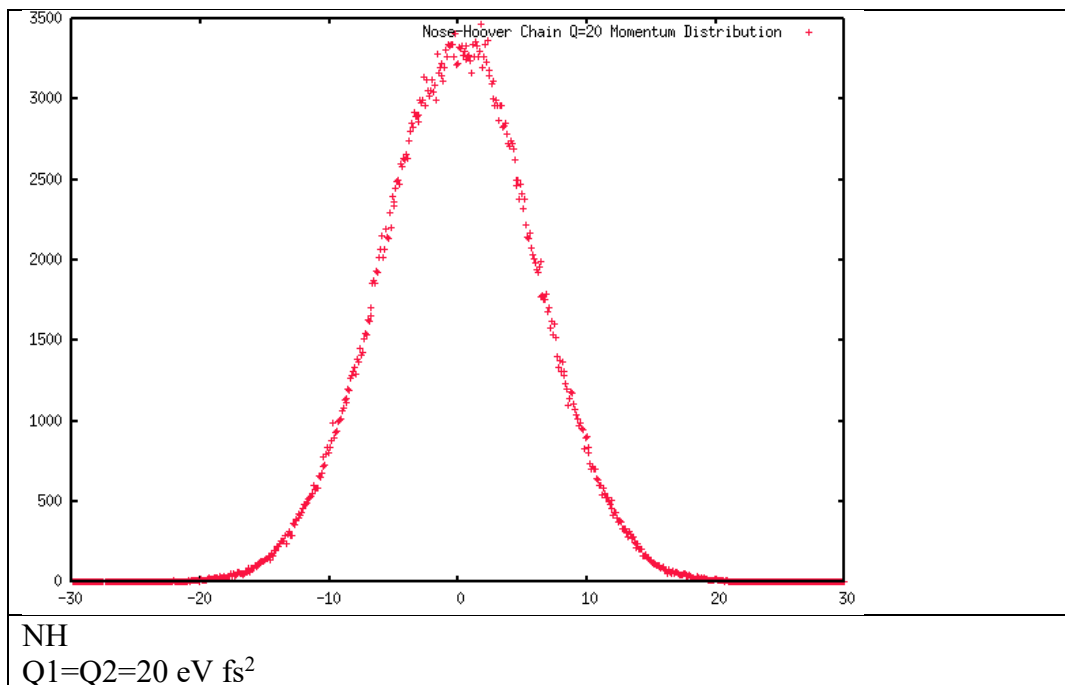
2. Plot of momentum distribution (dN_p/dp vs p , where N_p is the number of points falling in the range from p to $p+dp$).



Andersen, vfreq=0.001, 0.05, 0.5 1/fs



Berendsen, $\tau = 1000$ fs



A3. Description of potential interfaces (appendix to section III.B)

(1) Molecular mechanics interfaces, which allow for a variable number of atoms and are labeled

T-MM-D

where *T* = "HO" or "HE" for a homonuclear or heteronuclear potential energy subroutine, respectively, MM stands for "molecular mechanics", and *D* is the number of analytic derivatives available.

The following molecular mechanics interfaces are currently standard in POTLIB-online: HO-MM-0, HO-MM-1.

More interfaces can be added as new potential energy subroutines become available.

(2) Interfaces for a fixed number of atoms. These interfaces are labeled

N-DM

where *N* is the number of bodies, *D* is the number of analytic derivatives available plus one (e.g., for *D* = 1, only the potential energy is available, for *D* = 2, the potential energy and the first derivatives are available), and *M* is S for scalar mode (i.e., the energy for one geometry is computed per subroutine call, and the geometries, energies, and derivatives (when available) are passed using common blocks) and V for vector mode (i.e., the energies and derivatives (when available) for an array of geometries are calculated per subroutine call and are passed as arguments). Note if *D* = X, the potential interface is general enough to handle more than one value of *D*.

The following interfaces for a fixed number of atoms are currently standard in POTLIB-online: POTLIB-2001, 3-XS, 3-1V, 3-2V, 4-XS, 4-1S, 5-1S, 6-1S, and 7-1S.

(3) Interfaces for specific systems

Interfaces for the NH₃, HBr, and CH₂BrCl photodissociation systems.

A3.1 HO-MM-0 interface

The HO-MM-0 interface is used for potential energy subprograms capable of handling an arbitrary number of identical atoms. The driver program passes the geometry as a set of Cartesian coordinates for each atom, and the potential energy is returned.

Format and selected details:

In general, a HO-MM-0 potential energy routine has the following format:

```

SUBROUTINE POT( X, Y, Z, E, NATOM, MAXATOM)
DIMENSION X(MAXATOM), Y(MAXATOM), Z(MAXATOM)
E = SOME FUNCTION OF ( X, Y, and Z )
RETURN
END

```

Required variables:

The subroutine POT takes the following arguments

```

POT ( X(NATOM), Y(NATOM), Z(NATOM), E, NATOM, MAXATOM )
where

```

NATOM	input, integer	The number of identical atoms.
MAXATOM	input, integer	Sets the dimension of the cartesian variables X, Y, and Z. MAXATOM must be greater than or equal to NATOM.
X(NATOM) Y(NATOM) Z(NATOM)	input, double precision	One-dimensional arrays containing the X, Y, and Z components of all NATOM atoms, where the index labels the atoms.
E	output, double precision	The potential energy.

A3.2 HO-MM-1

The HO-MM-1 interface is used for potential energy subprograms capable of handling an arbitrary number of identical atoms. The driver program passes the geometry as a set of cartesian coordinates for each atom, and the potential energy and first derivatives are returned.

Format and selected details:

In general, a HO-MM-1 potential energy routine has the following format:

```

SUBROUTINE POT(X, Y, Z, E, DEDX, DEDY, DEDZ, NATOM, MAXATOM)
DIMENSION X(MAXATOM), Y(MAXATOM), Z(MAXATOM)
DIMENSION DEDX(MAXATOM), DEDY(MAXATOM), DEDZ(MAXATOM)

```

E = SOME FUNCTION OF X, Y, and Z
 DEDX = SOME FUNCTION OF X, Y, and Z
 DEDY = SOME FUNCTION OF X, Y, and Z
 DEDZ = SOME FUNCTION OF X, Y, and Z

RETURN

END

Required variables:

The subroutine POT takes the following arguments

POT (X(NATOM), Y(NATOM), Z(NATOM), E, DEDX(NATOM), DEDY(NATOM),
 DEDZ(NATOM), NATOM, MAXATOM)

where

NATOM	input, integer	The number of identical atoms.
MAXATOM	input, integer	Sets the dimension of the cartesian variables X, Y, and Z. MAXATOM must be greater than or equal to NATOM.
X(NATOM) Y(NATOM) Z(NATOM)	input, double precision	One-dimensional arrays containing the X, Y, and Z components of all NATOM atoms, where the index labels the atoms.
E	output, double precision	The potential energy.
DEDX(NATOM) DEDY(NATOM) DEDZ(NATOM)	output, double precision	One-dimensional arrays containing the first derivatives of the energy E with respect to the X, Y, and Z components of all NATOM atoms, where the index labels the atoms.

A3.3. POTLIB-2001

The POTLIB-2001 interface is described in detail in the [Computer Physics Communications](#) article accompanying the POTLIB-2001 program entry in the [CPC program library](#).

The reference is:

R. J. Duchovic, Y. L. Volobuev, G. C. Lynch, D. G. Truhlar, T. C. Allison, A. F. Wagner, B. C. Garrett, and J. C. Corchado, "POTLIB: A Potential Energy Surface

Library for Chemical Systems", Computer Physics Communications 144, 169-187 (2002), 156, 319-322(E) (2004).

3-XS:

The interface 3-XS is the standard interface for a 3-body system, where common blocks are used to pass data between the calling routine and the potential energy routine. The potential energy (and possibly the derivatives) are calculated for a single geometry for each call to POT. The subroutine POT requires no arguments. The common block PT1CM is required by the POT subroutine; this common block is used to pass the geometry of the triatomic system from the calling program to the potential routine and to return the electronic state energy and derivatives to the calling program. There are several other optional common blocks that may be used to further refine calls to POT. This interface may be used with or without derivatives.

Format and selected details:

SUBROUTINE POT

```
COMMON /PT1CM/ R, ENERGY, DEDR
DIMENSION R(3), DEDR(3)
```

Note: The following common blocks are optional and are used to pass control variables to the potential subroutine.

```
COMMON /PT2CM/ NSURF, NDER, NFLAG
COMMON /PT3CM/ LFLAG
COMMON /PT4CM/ IPTPRT, IDUM
COMMON /PT5CM/ EASYAB, EASYBC, EASYAC
DIMENSION NFLAG(21), LFLAG(20), IDUM(19)
```

Note: The following common blocks are optional and are used to pass excited-state energies and derivatives if available.

```
COMMON /PT6CM/ ENGY2, DE2DR
COMMON /PT7CM/ ENGY12, DE12DR
COMMON /PT8CM/ ENGY12
COMMON /PT9CM/ D2E1D, D2E2D, D2E12D
DIMENSION DE2DR(3), DE12DR(3), ENGY12(9), D2E1D(3,3), D2E2D(3,3),
D2E12D(3,3)
```

```
ENERGY = SOME FUNCTION OF R . . .
DEDR(:) = . . .
```

```
RETURN
```

```
END
```


Description of the common blocks:

The common block PT1CM is the only common block that is always required.

```
COMMON /PT1CM/ R, ENERGY, DEDR
DIMENSION R(3), DEDR(3)
```

R(3)	input, double precision	An array of the three internuclear bond distances. Atomic units are used.
ENERGY	output, double precision	The computed potential energy. Atomic units are used.
DEDR(3)	output, double precision	The computed derivatives with respect to the three internuclear distances. This field is included even when derivatives are not available. Atomic units are used.

The common block PT2CM is optional. It is used when there is more than one electronic state and/or derivatives are computed.

```
COMMON /PT2CM/ NSURF, NDER, NFLAG
DIMENSION NFLAG(21)
```

NSURF	input, integer	For a single surface routine, NSURF is not used. For a multiple surface routine, NSURF controls which surface is computed. When NSURF is equal to 0, the ground electronic state is used. When NSURF is equal to 1, the energy for the first excited electronic surface is computed. When both the ground and first excited surfaces are to be computed, NSURF is 2. Not all potential routines support NSURF=1 or 2.
NDER	input, integer	NDER controls the calculation of the derivatives of the energy with respect to the internuclear coordinates. If NDER is equal to 0, the derivatives are not

calculated. If NDER is equal to 1, the energy and the first derivatives are calculated. If NDER is equal to 2, the energy and the first and second derivatives are calculated. Not all potential routines support NDER=1 or NDER=2. NDER controls the derivative calculations for whichever electronic surface or combination of surfaces is called for by NSURF. Therefore, if NSURF and NDER are both equal to 1, the energy and first derivatives for the first excited electronic state are computed. If NSURF is equal to 2 and NDER is equal to 1, the subprogram computes the energy and the derivatives for both the ground and the first excited electronic states.

NFLAG(21) input, integer

This is included for compatibility with existing codes. These flags may be used to control various options in the potential routine.

The common block PT3CM is optional.

```
COMMON /PT3CM/ LFLAG
DIMENSION LFLAG(20)
```

LFLAG(20) input, logical

This is included for compatibility with existing codes. These flags may be used to control various options in the potential routine.

The common block PT4CM is optional and is used to control input/output.

```
COMMON /PT4CM/ IPTPRT, IDUM
DIMENSION IDUM(19)
```

IPTPRT input, integer

This potential routine will write data to the file fort.IPTPRT.

IDUM(19) input, integer This potential routine will read data from zero or more of the files fort.IDUM(1), fort.IDUM(2), etc...

The common block PT5CM is optional.

COMMON /PT5CM/ EASYAB, EASYBC, EASYAC

EASYAB, EASYBC, output, double precision The asymptotic energies at the minimum of the diatomic potential well.
EASYAC

The common block PT6CM is optional and is used to return excited surface energies and their derivatives when they are available.

COMMON /PT6CM/ ENGY2, DE2DR
DIMENSION DE2DR(3)

ENGY2, DE2DR(3) output, double precision The same as ENERGY and DEDR(3) (PT1CM) except for the first excited state. This common block is used with NSURF=1 or NSURF=2, where NSURF is set in PT2CM.

The common block PT7CM is optional and is used when a two-state system is represented in the diabatic representation.

COMMON /PT7CM/ ENGY12, DE12DR
DIMENSION DE12DR(3)

ENGY12, DE12DR(3) output, double precision The same as ENERGY and DEDR(3) (PT1CM) except for the diabatic coupling surface. This common block is used with NSURF=1 or NSURF=2, where NSURF is set in PT2CM.

The common block PT8CM is optional and is used when a two-state system is represented in the adiabatic representation.

COMMON /PT8CM/ ENGY12
DIMENSION ENGY12(8)

ENGY12(9)	output, double precision	The nine-dimension vector of the nonadiabatic coupling between the two electronic states.
-----------	--------------------------	---

The common block PT9CM is optional and is used when the potential routine is used to compute analytic Hessians.

```
COMMON /PT9CM/ D2E1D, D2E2D, D2E12D
DIMENSION D2E1D(3,3), D2E2D(3,3), D2E12D(3,3)
```

D2E1D(3,3)	output, double precision	The Hessian of the ground state.
------------	--------------------------	----------------------------------

D2E2D(3,3)	output, double precision	The Hessian of the first-excited state.
------------	--------------------------	---

D2E12D(3,3)	output, double precision	The Hessian of the diabatic coupling surface.
-------------	--------------------------	---

3-1V:

The 3-1V interface is used with potential energy subprograms for 3-body systems. The driver program obtains the energy at one or more nuclear geometries by passing them as arguments between the subprogram and the driver program.

Format and selected details:

The subroutine PREPOT, which takes no arguments, is called once before subsequent calls to the subroutine POT. PREPOT is usually used to initialize constant parameters of the surface, which are stored using the FORTRAN command save. Alternatively, the parameters may be stored in common blocks. Once the surface has been initialized, the subroutine POT may be called whenever the potential energy is needed.

In general, a 3-1V potential energy routine has the following format:

```
SUBROUTINE PREPOT
```

```
DATA STORAGE/HERE/,ETC...
```

```
SAVE
```

```
RETURN
```

```
ENTRY POT( R, E, NVALS, NSURF)
```

```
DIMENSION R(NVALS,3), E(NVALS)
```

```
DO I=1,NVALS
```

```
  E(I) = SOME FUNCTION OF ( R(I,1), R(I,2), R(I,3), and NSURF )
```

```
ENDDO
```

RETURN

END

Required variables:

The subroutine POT takes the following arguments

POT(R, E, NVALS, NSURF)
 DIMENSION R(NVALS,3), E(NVALS)
 where

NVALS	input, integer	The energy and the derivatives are computed for NVALS different geometries.
NSURF	input, integer	NSURF labels the potential energy surface. For a single-surface potential, NSURF=1. For a two-state potential, NSURF=1 and 3 for the two diagonal diabatic potential energy surfaces, and NSURF=2 for the diabatic coupling surface.
R(NVALS,3)	input, double precision	A two dimensional array containing the internuclear bond distances. The first index labels the NVALS different geometries, and the second index labels the three internuclear distances. Atomic units are used.
E(NVALS)	output, double precision	An array containing the potential energies of surface NSURF at each of the NVALS geometries. Atomic units are used.

3-2V:

The 3-2V interface is used with potential energy subprograms that calculate the potential energy and the analytical derivatives for a 3-body system. The driver program obtains the energy and its derivatives at one or more nuclear geometries by passing them as arguments between the subprogram and the driver program.

Format and selected details:

The subroutine PREPOT, which takes no arguments, is called once before subsequent calls to the subroutine POT. PREPOT is usually used to initialize constant parameters of the surface, which are stored using the FORTRAN command save. Alternatively, the parameters may be stored in common blocks. Once the surface has been initialized, the subroutine POT may be called whenever the potential energy and its derivatives are needed.

In general, a 3-2V potential energy routine has the following format:

```
SUBROUTINE PREPOT
```

```
DATA STORAGE/HERE/,ETC...
```

```
SAVE
```

```
RETURN
```

```
ENTRY POT( R, E, DE, NVALS, NSURF)
```

```
DIMENSION R(NVALS,3), E(NVALS), DE(3,NVALS)
```

```
DO I=1,NVALS
```

```
  E(I) = SOME FUNCTION OF ( R(I,1), R(I,2), R(I,3), and NSURF )
```

```
  DE(1,I) = . . .
```

```
  DE(2,I) = . . .
```

```
  DE(3,I) = . . .
```

```
ENDDO
```

```
RETURN
```

```
END
```

Required variables:

The subroutine POT takes the following arguments

```
POT( R, E, DE, NVALS, NSURF)
```

```
DIMENSION R(NVALS,3), E(NVALS), DE(3,NVALS)
```

where

NVALS input, integer

The energy and the derivatives are computed for NVALS different geometries.

NSURF input, integer

NSURF labels the potential energy surface. For a single-surface potential, NSURF=1. For a two-state potential, NSURF=1 and 3 for the two diagonal diabatic potential energy surfaces, and

		NSURF=2 for the diabatic coupling surface.
R(NVALS,3)	input, double precision	A two dimensional array containing the internuclear bond distances. The first index labels the NVALS different geometries, and the second index labels the three internuclear distances. Atomic units are used.
E(NVALS)	output, double precision	An array containing the potential energies of surface NSURF at each of the NVALS geometries. Atomic units are used.
DE(3,NVALS)	output, double precision	A two dimensional array of the first derivatives of state NSURF with respect to the three internuclear distances. The first index labels the three internuclear distances, and the second index labels the NVALS different geometries. Atomic units are used.

4-XS:

The interface 4-XS is a standard interface for a 4-body system, where common blocks are used to pass data between the calling routine and the potential energy routine. The 4-XS calling protocol is the most general 4-body calling protocol in POTLIB-online. The [4-1S interface](#) may be more convenient for systems that are dimers of diatomic molecules.

The potential energy (and possibly the derivatives) are calculated for a single geometry for each call to POT. The subroutine POT requires no arguments. The common block PT1CM is required by the POT subroutine; this common block is used to pass the geometry of the system from the calling program to the potential routine and to return the electronic state energy and derivatives to the calling program. There are several other optional common blocks that may be used to further refine calls to POT. This interface may be used with or without derivatives.

The 4-XS calling interface protocol was added to POTLIB-online on May 7, 2003.

Format and selected details:

The following common blocks are used to pass control variables and data to and from the potential subroutine.

SUBROUTINE POT

```
COMMON /PT1CM/ R, ENGYGS, DEGSDR
DIMENSION R(N3ATOM), DEGSDR(N3ATOM)
```

```
COMMON /INFOCM/
CARTNU,INDEXES,IRCTNT,NATOMS,ICARTR,MDER,MSURF,REF
DIMENSION CARTNU(NATOM,3),INDEXES(NATOM)
```

```
COMMON /USRICM/ CART,ANUZERO,NULBL,NFLAG,NASURF,NDER
DIMENSION
CART(NATOM,3),NULBL(NATOM),NFLAG(20),NASURF(ISURF+1,ISURF+1)
```

```
COMMON /USROCM/
PENGYGS,PENGYES,PENGYIJ,DGSCART,DESCART,DIJCART
DIMENSION PENGYES(ISURF),PENGYIJ(JSURF),DGSCART(NATOM,3),
+      DESCART(NATOM,3,ISURF),DIJCART(NATOM,3,JSURF)
```

```
COMMON /PT3CM/ EZERO(ISURF+1)
DIMENSION EZERO(ISURF+1)
```

```
COMMON /PT4CM/ ENGYES,DEESDR
DIMENSION ENGYES(ISURF),DEESDR(N3ATOM,ISURF)
```

```
COMMON /PT5CM/ ENGYIJ,DEIJDR
DIMENSION ENGYIJ(JSURF),DEIJDR(N3ATOM,JSURF)
```

```
ENGYGS = ENERGY AS SOME FUNCTION OF R . . .
DEGSDR(:) = . . .
```

```
RETURN
```

```
END
```

A detailed description of the common blocks is provided in:

R. J. Duchovic, Y. L. Volobuev, G. C. Lynch, D. G. Truhlar, T. C. Allison, A. F. Wagner, B. C. Garrett, and J. C. Corchado, "POTLIB: A Potential Energy Surface Library for Chemical Systems", *Computer Physics Communications* 144, 169-187 (2002).

The common block PT1CM is the only common block that is always required.

```
COMMON /PT1CM/ R, ENGYGS, DEGSDR
DIMENSION R(N3ATOM), DEGSDR(N3ATOM)
```

R(N3ATOM)

input, real*8

An array of the N3ATOM
internuclear bond distances.

ENGYGS	output, real*8	The computed potential energy.
DEGSDR(N3ATOM)	output, real*8	The computed derivatives with respect to the N3ATOM internuclear distances. This field is included even when derivatives are not available.

4-1S:

The 4-1S interface is used with potential energy subprograms for 4-body systems. The coordinate system used is useful for systems that are dimers of two diatomic molecules. (The 4-XS interface is designed for more general 4-body systems.) The driver program obtains the energy at one or more nuclear geometries by passing them as arguments between the subprogram and the driver program.

Format and selected details:

The subroutine PREPOT, which takes no arguments, is called once before subsequent calls to the subroutine POT. PREPOT is usually used to initialize constant parameters of the surface, which are stored using the FORTRAN command save. Alternatively, the parameters may be stored in common blocks. Once the surface has been initialized, the subroutine POT may be called whenever the potential energy is needed.

In general, a 4-1S potential energy routine has the following format:

```
SUBROUTINE PREPOT
```

```
DATA STORAGE/HERE/,ETC...
```

```
SAVE
```

```
RETURN
```

```
ENTRY POT( R1, R2, R, TH1, TH2, TAU, E )
```

```
E = . . .
```

```
RETURN
```

```
END
```

Required variables:

The subroutine POT takes the following arguments

```
POT ( R1, R2, R, TH1, TH2, TAU, E )
```

where

Throughout this discussion we will consider a dimer of diatomics (AB)(AB) as our four-body system, although the interface is more general. Atomic units are used throughout.

R1,R2	input, double precision	Diatomic internuclear distances for each dimer.
R	input, double precision	Distance between the centers of mass of the dimers.
TH1,TH2	input, double precision	The angles between the AB diatom bonds and the vector connecting the centers of mass of the two diatoms.
TAU	input, double precision	The dihedral angle between two planes; the first plane contains the first AB diatom bond and the vector connecting the centers of mass of the two diatoms, and the second plane contains the second AB diatom bond and the vector connecting the centers of mass of the two diatoms.
E	output, double precision	The potential energy.

5-1S:

The interface 5-1S (5-body system, scalar mode) provides a set of calling conventions for a subroutine that calculates single-point potential energy of a 5-body system on a ground surface. This interface follows the calling conventions imposed by POLYRATE.

6-1S:

The interface 6-1S (6-body system, scalar mode) provides a set of calling conventions for a subroutine that calculates single-point potential energy of a 6-body system on a ground surface. This interface follows the calling conventions imposed by POLYRATE.

7-1S:

The interface 7-1S (7-body system, scalar mode) provides a set of calling conventions for a subroutine that calculates single-point potential energy of a 7-body system on a ground surface. This interface follows the calling conventions imposed by POLYRATE.

A3.4. NH_3

Reference: "Improved Direct Diabatization and Fitting of Coupled Potential Energy Surfaces for the Photodissociation of Ammonia," Z. H. Li, R. Valero, and D. G. Truhlar, *Theoretical Chemistry Accounts* 118, 9-24 (2007).

The interface NH_3 calculates the potential energy and the analytical derivatives for the lowest two adiabatic states or the two equivalent diabatic states and their coupling for the NH_3 system. The driver program obtains the energy and its derivatives at a given nuclear geometry by passing them as arguments between the subprogram and the driver program.

The subroutine PREPOT, which takes no arguments, is called once before subsequent calls to the subroutine POT. PREPOT is used to initialize constant parameters of the surface, which are stored in a common block. Once the surface has been initialized, the subroutine POT may be called whenever the potential energies and coupling their derivatives are needed.

The NH_3 potential energy routine has the following format:

```
SUBROUTINE PREPOT
```

```
  call potcoeff
```

```
RETURN
```

```
END
```

```
SUBROUTINE POT(Xcart, U11, U22, U12, V1, V2, gU11, gU22, gU12, gV1, gV2)
```

```
DOUBLE PRECISION Xcart(12),
```

```
U11,U22,U12,V1,V2,gU11(12),gU22(12),gU12(12),gV1(12),gV2(12)
```

```
  parameter(autoang=0.5291772108d0)
```

```
  parameter (EV_TO_HARTREE= 1.d0/autoev)
```

```
  parameter (ANG_TO_BOHR=1.0d0/autoang)
```

```
  parameter (gconv = EV_TO_HARTREE/ANG_TO_BOHR)
```

```
do i=1,12
```

```
  cart(i)= Xcart(i)*autoang
```

```
end do
```

```
  call packpot(cart,U11,U22,U12,V1,V2,gU11,gU22,gU12,gV1,gV2)
```

```
U11 = U11 * EV_TO_HARTREE
```

```
U22 = U22 * EV_TO_HARTREE
```

```
U12 = U12 * EV_TO_HARTREE
```

```
V1 = V1 * EV_TO_HARTREE
```

```
V2 = V2 * EV_TO_HARTREE
```

```
do i=1,12
```

```

gU11(i) = gU11(i) * gconv
gU22(i) = gU22(i) * gconv
gU12(i) = gU12(i) * gconv
gV1(i) = gV1(i) * gconv
gV2(i) = gV2(i) * gconv
enddo

```

RETURN

END

Required variables:

The subroutine POT takes the following arguments:

POT(Xcart, U11, U22, U12, V1, V2, gU11, gU22, gU12, gV1, gV2)

where

Xcart	input, double precision	Cartesian coordinates of input geometry in bohr.
U11, U22	output, double precision	The two diagonal diabatic potential energy surfaces. Energies are given in hartrees.
U12	output, double precision	The diabatic coupling surface. The coupling is given in hartrees.
V1, V2	output, double precision	The two adiabatic potential energy surfaces. Energies are given in hartrees.
gU11, gU22	output, double precision	Nuclear Cartesian derivatives of the two diagonal diabatic potential energies. Units are hartree/bohr.
gU12	output, double precision	Nuclear Cartesian derivatives of the diabatic coupling. Units are hartree/bohr.
gV1, gV2	output, double precision	Nuclear Cartesian derivatives of the adiabatic potential energies. Units are hartree/bohr.

A3.5. HBr

Reference: "Adiabatic States Derived from a Spin-Coupled Diabatic Transformation: Semiclassical Trajectory Study of Photodissociation of HBr and the Construction of Potential Curves for LiBr^+ ," R. Valero, D. G. Truhlar, and A. W. Jasper, *Journal of Physical Chemistry A* 112, 5756-5769 (2008).

The interface HBr calculates the potential energy and the analytical derivatives for the twelve spin-coupled adiabatic states of HBr that correlate with ground-state atoms ($\text{H}(^2\text{S}) + \text{Br}(^2\text{P})$), or the twelve equivalent diabatic states and their couplings. The driver program obtains the energy and its derivatives at a given nuclear geometry by passing them as arguments between the subprogram and the driver program.

The subroutine PREPOT, which takes no arguments, is called once before subsequent calls to the subroutine POT. PREPOT is used to initialize constant parameters of the surface, which are stored in a common block. Once the surface has been initialized, the subroutine POT may be called whenever the potential energies and their derivatives and the nonadiabatic couplings are needed.

The HBr potential energy routine has the following format:

```
SUBROUTINE PREPOT
```

```
  call potcoeff
```

```
RETURN
```

```
END
```

```
SUBROUTINE POT(Xcart, UI, UIJ, VI, gUI, gUIJ, gVI, dvec)
```

```
DOUBLE PRECISION Xcart(6), UI(12), UIJ(12, 12), VI(12), gUI(3,2,12),  
gUIJ(3,2,12,12), gVI(3,2,12)
```

```
parameter(autoang=0.5291772108d0)
```

```
parameter (EV_TO_HARTREE= 1.d0/autoev)
```

```
parameter (ANG_TO_BOHR=1.0d0/autoang)
```

```
parameter (gconv = EV_TO_HARTREE/ANG_TO_BOHR)
```

```
do i=1,6
```

```
  cart(i)= Xcart(i)*autoang
```

```
end do
```

```
call packpot(cart, UI, UIJ, VI, gUI, gUIJ, gVI, dvec)
```

```
do i=1,12
```

```
  UI(i) = UI(i) * EV_TO_HARTREE
```

```
  VI(i) = VI(i) * EV_TO_HARTREE
```

```
do j=1,12
```

```
  UIJ(i,j) = UIJ(i,j) * EV_TO_HARTREE
```

```

enddo
enddo
do i=1,3
do j=1,2
do k=1,12
gUI(i,j,k) = gUI(i,j,k) * gconv
gVI(i,j,k) = gVI(i,j,k) * gconv
do l=1,12
gUIJ(i,j,k,l) = gUIJ(i,j,k,l) * gconv
enddo
enddo
enddo
enddo

do i1 = 1,3
do i2 = 1,2
do j = 1,12
do k = 1,12

dvec(i1,i2,j,k) = dvec(i1,i2,j,k) * autoang

enddo
enddo
enddo
enddo

```

RETURN

END

Required variables:

The subroutine POT takes the following arguments:

POT(Xcart, UI, UIJ, VI, gUI, gUIJ, gVI, dvec)

where

Xcart	input, double precision	Cartesian coordinates of input geometry in bohr.
UI	output, double precision	Array with the twelve diagonal diabatic potential energy surfaces. Energies are given in hartrees.

UIJ	output, double precision	12×12 matrix with the diabatic coupling surfaces. The coupling is given in hartrees.
VI	output, double precision	Array with the twelve adiabatic potential energy surfaces. Energies are given in hartrees.
gUI	output, double precision	Array with the nuclear Cartesian derivatives of the twelve diagonal diabatic potential energies. Units are hartree/bohr.
gUIJ	output, double precision	12×12 matrix with nuclear Cartesian derivatives of the diabatic couplings. Units are hartree/bohr.
gVI	output, double precision	Array with the nuclear Cartesian derivatives of the twelve adiabatic potential energies. Units are hartree/bohr.
dvec	output, double precision	Nonadiabatic coupling vector. Units are bohr ⁻¹ .

A3.6. *BrCH₂Cl*

Reference: "Photochemistry in a Dense Manifold of Electronic States: Photodissociation of CH₂ClBr," R. Valero and D. G. Truhlar, *Journal of Chemical Physics* 137, 22A539/1-14 (2012).

The interface *BrCH₂Cl* calculates the potential energies and the analytical derivatives for the twenty-four spin-coupled adiabatic states of *BrCH₂Cl* that correlate with ground- and excited state polyatomic fragments and ground- and spin-orbit excited atomic fragments derived from the dissociations *Br + CH₂Cl* and *Cl + CH₂Br*; therefore, eight asymptotic states in total (*Br*(²P_{3/2} + *CH₂Cl*(X ¹A'), *Br*(²P_{1/2} + *CH₂Cl*(X ¹A'), *Br*(²P_{3/2} + *CH₂Cl*(A ¹A''), *Br*(²P_{1/2} + *CH₂Cl*(A ¹A''), *Cl*(²P_{3/2} + *CH₂Br*(X ¹A'), *Cl*(²P_{1/2} + *CH₂Br*(X ¹A'), *Cl*(²P_{3/2} + *CH₂Br*(A ¹A''), and *Cl*(²P_{1/2} + *CH₂Br*(A ¹A'')), or the twenty-four equivalent diabatic states and their couplings. The driver program obtains the energy and its derivatives at a given nuclear geometry by passing them as arguments between the subprogram and the driver program.

The subroutine *PREPOT*, which takes no arguments, is called once before subsequent calls to the subroutine *POT*. *PREPOT* is used to initialize constant parameters of the surface, which are stored in a common block. Once the surface has been initialized, the

subroutine POT may be called whenever the potential energies and their derivatives and the nonadiabatic couplings are needed.

The BrCH₂Cl potential energy routine has the following format:

```
SUBROUTINE PREPOT
```

```
  call potcoeff
```

```
RETURN
```

```
END
```

```
SUBROUTINE pot(Xcart,UI,UIJ,VI,gUI,gUIJ,gVI,dvec,icall)
```

```
real*8 cart(15)
```

```
real*8 UI(24),VI(24),gUI(3,5,24),gVI(3,5,24)
```

```
real*8 UIJ(24,24),gUIJ(3,5,24,24)
```

```
real*8 mat(24,24),UIJpl(24,24),UIJmin(24,24)
```

```
real*8 dvec(3,5,24,24)
```

```
real*8 VIpl(24),VImin(24),UIpl(24),UImin(24)
```

```
real*8 cartpl(15),cartmin(15)
```

```
integer icall
```

```
parameter(autoang=0.5291772108d0)
```

```
parameter(autoev=27.2113845d0)
```

```
parameter (EV_TO_HARTREE= 1.d0/autoev)
```

```
parameter (ANG_TO_BOHR=1.0d0/autoang)
```

```
parameter (gconv = EV_TO_HARTREE/ANG_TO_BOHR)
```

```
do i=1,15
```

```
  cart(i)= Xcart(i)*autoang
```

```
end do
```

C Finite differences

```
do i=1,15
```

```
  cartpl(i)= cart(i)
```

```
  cartmin(i) = cart(i)
```

```
end do
```

```
DELTA = 0.0001d0
```

```
kk = 0
```

```
do j=1,5
```

```
do i=1,3
```

```
  kk = kk + 1
```

```
cartpl(kk) = cart(kk) + DELTA
```



```

call packpot(cartpl,UIpl,UIJpl,VIpl,mat,icall)

cartmin(kk) = cart(kk) - DELTA

call packpot(cartmin,UImin,UIJmin,VImin,mat,icall)

do l=1,24
  gVI(i,j,l) = (VIpl(l) - VImin(l)) / (2.d0*DELTA)
  gUI(i,j,l) = (UIpl(l) - UImin(l)) / (2.d0*DELTA)
do m=1,24
  gUIJ(i,j,l,m) = (UIJpl(l,m) - UIJmin(l,m)) / (2.d0*DELTA)
enddo
enddo

cartpl(kk) = cart(kk)
cartmin(kk) = cart(kk)

enddo
enddo

call packpot(cart,UI,UIJ,VI,mat,icall)

do i=1,24
  UI(i) = UI(i) * EV_TO_HARTREE
  VI(i) = VI(i) * EV_TO_HARTREE
do j=1,24
  UIJ(i,j) = UIJ(i,j) * EV_TO_HARTREE
enddo
enddo
do i=1,3
do j=1,5
do k=1,24
  gUI(i,j,k) = gUI(i,j,k) * gconv
  gVI(i,j,k) = gVI(i,j,k) * gconv
do l=1,24
  gUIJ(i,j,k,l) = gUIJ(i,j,k,l) * gconv
enddo
enddo
enddo
enddo

do k=1,24
do i=1,3
do j=1,5
  gUIJ(i,j,k,k) = gUI(i,j,k)
enddo

```

```

    enddo
enddo

```

C Compute the nonadiabatic coupling vectors

```
call getdvec3(5,UI,gUIJ,VI,dvec,mat)
```

```

RETURN
END

```

Required variables:

The subroutine POT takes the following arguments:

```
POT(Xcart, UI, UIJ, VI, gUI, gUIJ, gVI, dvec, icall)
```

where

Xcart	input, double precision	Cartesian coordinates of input geometry in bohr.
UI	output, double precision	Array with the 24 diagonal diabatic potential energy surfaces. Energies are given in hartrees.
UIJ	output, double precision	24×24 matrix with the diabatic coupling surfaces. The coupling is given in hartrees.
VI	output, double precision	Array with the 24 adiabatic potential energy surfaces. Energies are given in hartrees.
gUI	output, double precision	Array with the nuclear Cartesian derivatives of the 24 diagonal diabatic potential energies. Units are hartree/bohr.
gUIJ	output, double precision	24×24 matrix with nuclear Cartesian derivatives of the diabatic couplings. Units are hartree/bohr.
gVI	output, double precision	Array with the nuclear Cartesian derivatives of the 24 adiabatic potential energies. Units are hartree/bohr.

dvec	output, double precision	Nonadiabatic coupling vector. Units are bohr ⁻¹ .
icall	input, integer	Variable controlling the calculation of adiabatic potential surfaces. Only if icall=1 will they be calculated.

A4. SPRNG documentation

The user's guide for the SPRNG (Scalable Parallel (Pseudo-) Random Number Generator) library can be found in the subdirectory `sprng/DOCS` of the *ANT* distribution and also at the web address <http://sprng.cs.fsu.edu/>

The version of SPRNG in the present version of the *ANT* package is version 1.0.

A5. *Gaussian09* documentation

The user's guide for *Gaussian09* is available at the web address http://www.gaussian.com/g_tech/g_ur/l_keywords09.htm. The version of *Gaussian09* tested with the *ANT* program is G09 C.01. But we expect that the *ANT* program will also work with other versions of the *Gaussian09* program and also the *Gaussian03* program.

A6. *Molpro* documentation

The user's guide for *Molpro* is available at the web address <http://www.molpro.net/info/2012.1/doc/manual/>. The version of *Molpro* tested with the *ANT* program is version 2010.1.24. But we expect that the *ANT* program will also work with other versions of the *Molpro* program.

A7. Surface couplings in non-BO calculations

The couplings in an adiabatic representation are called nonadiabatic couplings. These are vectors. They are the "derivative" couplings, caused by the nuclear momentum, which is a vector derivative operator (i.e., a gradient). The couplings in a diabatic representation are scalars. The vector couplings are assumed to vanish in a diabatic representation. The scalar couplings vanish in an adiabatic representation.

However, in an FSTU calculation, even in the diabatic representation, we compute a special "nonadiabatic coupling" vector as described on page 389 of

“Non-Born-Oppenheimer Molecular Dynamics for Conical Intersections, Avoided Crossings, and Weak Interactions,” A. W. Jasper and D. G. Truhlar, in *Conical Intersections: Theory, Computation, and Experiment*, edited by W. Domcke, D. R. Yarkony, and H. Köppel (World Scientific, Singapore, 2011), pp. 375-412. (chapter 10) [Adv. Ser. Phys. Chem. 17, 375-412 (2011)]. [A PDF of this book chapter is available at <http://comp.chem.umn.edu/Truhlar/bookchap.htm>]

This is the nonadiabatic coupling that one would have if one temporarily switched to a special adiabatic representation. If one is considering a hop between diabatic states K and K' , this special adiabatic representation is what one gets if one temporarily drops all states except K and K' and diagonalizes the resulting two-by-two matrix. The resulting coupling is given by the two-by-two version of equation 13. For a two-by-two case, the sum in eq 13 just has $i,j = K,K$ and $i,j = K',K$. For example, if $K = a$ and $K' = b$, we just need W_{ab} and W_{ba} , where the latter equals W_{ab} .

A8. Computation of the reduced nonadiabatic couplings

This appendix section describes the correction of a bug in the calculation of the reduced nonadiabatic couplings that has been fixed in version-2014-2 (and later versions) of the code. This bug is related to the use of unclear notation in equation (46) of the book chapter

"Non-Born-Oppenheimer Molecular Dynamics for Conical Intersections, Avoided Crossings, and Weak Interactions," A. W. Jasper and D. G. Truhlar, in *Conical Intersections: Theory, Computation, and Experiment*, edited by W. Domcke, D. R. Yarkony, and H. Köppel (World Scientific, Singapore, 2011), pp. 375-412. (Chapter 10)

[The citation as a periodical would be A. W. Jasper and D. G. Truhlar, Adv. Ser. Phys. Chem. 17, 375-412 (2011)].

A clearer version of the equation is included in the present section.

A concise background summary of the relevant issues concerning nonadiabatic coupling is presented next, followed by a description of the code change.

The energy matrix in the diabatic representation is represented as \mathbf{W} , with w_{ij} being the ij element of the matrix; the matrix is symmetric. Adiabatic energies and couplings are calculated from these diabatic potential energy matrix elements w_{ij} and their gradients. The adiabatic energies V_i are the eigenvalues of the diabatic energy matrix \mathbf{W} , and d_{ij} are the coefficients of the linear combination of the adiabatic states (φ_i) that represents the diabatic electronic wave functions:

$$\varphi_j^d = \sum_i d_{ij} \varphi_i \quad (1)$$

Note the \mathbf{d} matrix, formed by the elements d_{ij} , is the matrix whose columns are the eigenvalues of \mathbf{W} . The gradients of the adiabatic surfaces are

$$\nabla_n V_i = \sum_{j,k} d_{ij}^* d_{ik} \nabla_n W_{jk} \quad (2)$$

and the nonadiabatic couplings are

$$\mathbf{F}_{ij} = \begin{cases} \frac{1}{V_j - V_i} \sum_{k,l} d_{ik}^* d_{jl} \nabla_n W_{kl} & (i \neq j) \\ 0 & (i = j) \end{cases} \quad (3)$$

where the subindexes i, j denote the coupling between electronic state surfaces i and j . Thus, the element \mathbf{F}_{21} is given by the equation

$$\mathbf{F}_{21} = \frac{1}{V_1 - V_2} \sum_{k,l} d_{2k}^* d_{l1} \nabla_n W_{kl} \quad (4)$$

In the surface hopping and decay of mixing algorithms, the direction that is used for the change in momentum due to hopping or the decay of mixing is called the hopping direction. When propagation is carried out in the adiabatic representation or when propagation is carried out in a two-state diabatic representation, the hopping direction is the direction of the nonadiabatic coupling vector, as calculated from eq. (3). However, if propagation is carried out in a diabatic representation with more than two states, $\mathbf{F}_{KK'}$ (where K and K' represent any two electronic states) cannot be used as the hopping direction because the adiabatic and diabatic state labels do not generally correlate to a

globally consistent pair of states. Instead of using the nonadiabatic coupling vectors, one uses the reduced nonadiabatic coupling vectors computed from the submatrix:

$$\mathbf{W}^r = \begin{pmatrix} W_{KK} & W_{KK'} \\ W_{K'K} & W_{K'K'} \end{pmatrix}, \quad (5)$$

The expression

$$\mathbf{F}_{KK'}^r = \frac{d_{KK}^{r,*} d_{K'K}^r \nabla_n W_{KK} + (d_{KK}^{r,*} d_{K'K'}^r + d_{KK}^{r,*} d_{K'K}^r) \nabla_n W_{KK'} + d_{KK}^r d_{K'K'}^r \nabla_n W_{K'K'}}{W_+ - W_-} \quad (6)$$

is given for the reduced nonadiabatic coupling vectors in equation (46) of the book chapter cited above; see also equation (A9) of

"Quantum Mechanical and Quasiclassical Trajectory Surface Hopping Studies of the Electronically Nonadiabatic Predissociation of the \tilde{A} State of NaH_2 ," M. D. Hack, A. W. Jasper, Y. L. Volobuev, D. W. Schwenke, and D. G. Truhlar, *Journal of Physical Chemistry A* 103, 6309-6326 (1999).

The notation used for the eigenvalues, W_+ and W_- , of the submatrix \mathbf{W}^r is incorrect (or at least confusing) in the book chapter, and this led to an error in the sign of the denominator for some of the reduced nonadiabatic coupling vectors in early versions of the code. Equation (46) can be written in a clearer way as follows:

$$\mathbf{F}_{KK'}^r = \frac{d_{KK}^{r,*} d_{K'K}^r \nabla_n W_{KK} + (d_{KK}^{r,*} d_{K'K'}^r + d_{KK}^{r,*} d_{K'K}^r) \nabla_n W_{KK'} + d_{KK}^r d_{K'K'}^r \nabla_n W_{K'K'}}{W_{K'}^r - W_K^r} \quad (6)$$

where $W_{K'}^r$ and W_K^r are the eigenvalues corresponding to states K' and K respectively. Thus, the reduced nonadiabatic coupling vector between surface 1 and 2 is given by

$$\mathbf{F}_{12}^r = \frac{d_{11}^{r,*} d_{21}^r \nabla_n W_{11} + (d_{11}^{r,*} d_{22}^r + d_{12}^{r,*} d_{21}^r) \nabla_n W_{12} + d_{12}^r d_{22}^r \nabla_n W_{22}}{W_2^r - W_1^r} \quad (7)$$

Note that only some elements of the full reduced coupling vectors matrix are computed, and in the correct code they can fall in either the upper or the lower triangular part of the matrix; e.g. for a three-state system propagating on the second surface, only the reduced couplings \mathbf{F}_{12}^r , and \mathbf{F}_{32}^r are computed. Here is the corrected code:

```
do k=1,nsurft
  if(k.ne.nsurf) then
```

```

u2b2(1,1) = pemd(k,k)
u2b2(1,2) = pemd(k,nsurf)
u2b2(2,1) = pemd(nsurf,k)
u2b2(2,2) = pemd(nsurf,nsurf)
do i=1,3
do j=1,NCLU
  gu2b2(i,j,1,1) = gpemd(i,j,k,k)
  gu2b2(i,j,1,2) = gpemd(i,j,k,nsurf)
  gu2b2(i,j,2,1) = gpemd(i,j,nsurf,k)
  gu2b2(i,j,2,2) = gpemd(i,j,nsurf,nsurf)
enddo
enddo
call getdvec2(NCLU,u2b2,gu2b2,dvec2b2)
do i=1,3
do j=1,NCLU
  dvec(i,j,k,nsurf) = dvec2b2(i,j)
  dvec(i,j,nsurf,k) = -dvec2b2(i,j)
enddo
enddo
endif
enddo

```

However in the subroutine `getdvec2`, which computes the reduced nonadiabatic coupling vectors, the numerator was originally written to compute the upper triangular matrix element of the 2×2 matrix while the denominator computed the lower matrix element. This created an inconsistency in the sign of the reduced nonadiabatic couplings. This has been fixed, and here is the corrected code as of version 2014:

1. Changing the `getdvec2` subroutine for computing $\mathbf{F}_{KK'}$ being $K' < K$ (e.g., the element \mathbf{F}_{21} for a system with two surfaces)

```

do i1 = 1,3
do i2 = 1,nclu
  dvec2b2(i1,i2) = 0.d0
  do k = 1, 2
  do l = 1, 2
    dvec2b2(i1,i2) = dvec2b2(i1,i2)
&      +cc(k,2)*cc(l,1)*gu2b2(i1,i2,k,l)
  enddo
  enddo
  if ((v1-v2) .ne. 0.0d0) then
    dvec2b2(i1,i2) = dvec2b2(i1,i2)/(v1-v2)
  else
    dvec2b2(i1,i2) = 0.0d0
  endif
enddo

```



```
enddo
```

2. Keeping track of the indexes of the surfaces and changing the sign if necessary when the reduced nonadiabatic coupling is computed.

```
do k=1,nsurft
  if(k.ne.nsurf) then
    u2b2(1,1) = pemd(k,k)
    u2b2(1,2) = pemd(k,nsurf)
    u2b2(2,1) = pemd(nsurf,k)
    u2b2(2,2) = pemd(nsurf,nsurf)
    do i=1,3
      do j=1,NCLU
        gu2b2(i,j,1,1) = gpemd(i,j,k,k)
        gu2b2(i,j,1,2) = gpemd(i,j,k,nsurf)
        gu2b2(i,j,2,1) = gpemd(i,j,nsurf,k)
        gu2b2(i,j,2,2) = gpemd(i,j,nsurf,nsurf)
      enddo
    enddo
    call getdvec2(NCLU,u2b2,gu2b2,dvec2b2)
    do i=1,3
      do j=1,NCLU
        if(k.gt.nsurf) then
          dvec(i,j,k,nsurf) = dvec2b2(i,j)
        else
          dvec(i,j,k,nsurf) = -dvec2b2(i,j)
        endif
        dvec(i,j,nsurf,k) = -dvec(i,j,k,nsurf)
      enddo
    enddo
  endif
enddo
```

This bug is fixed in version-2014 of the *ANT* code and hence in all later versions as well.

A9. Wigner distribution of a ground-state harmonic oscillator

This section presents a derivation of the ground-state Wigner distribution for a vibrational mode in term of energy for a given force constant and reduced mass. The purposes of expressing the distribution in terms of energy is that it be applied even when the energy in a mode is not the zero-point energy (sometimes we want it to be smaller than the zero point energy in order to minimize unphysical zero point vibrational energy leak).

Let the Hamiltonian H be given by $\frac{p^2}{2m} + \frac{kx^2}{2}$, where p is the momentum, m is the mass or reduced mass, k is the force constant, and x is the displacement coordinate. The Wigner distribution for the ground state of a harmonic oscillator (HO) is

$$P = Ne^{-ax^2} e^{-bp^2}$$

where N , a , and b are constants. If the energy of the oscillator is E , we know by the HO virial theorem that $\langle T \rangle = \langle V \rangle = E/2$. The Wigner distribution must be normalized and give these expectation values. Therefore

$$N \int dx dp e^{-ax^2} e^{-bp^2} = 1$$

$$N \int dx dp \frac{p^2}{2m} e^{-ax^2} e^{-bp^2} = E/2$$

$$N \int dx dp \frac{kx^2}{2} e^{-ax^2} e^{-bp^2} = E/2$$

All integrals are $(-\infty, \infty)$. These three equations can be solved for N , a , and b . Doing the integrals:

$$N \sqrt{\frac{\pi}{a}} \sqrt{\frac{\pi}{b}} = 1$$

$$N \sqrt{\frac{\pi}{a}} \sqrt{\frac{\pi}{b}} \frac{1}{4mb} = \frac{1}{4mb} = E/2$$

$$N \sqrt{\frac{\pi}{a}} \sqrt{\frac{\pi}{b}} \frac{k}{4a} = \frac{k}{4a} = E/2$$

So we have

$$N = \frac{\sqrt{ab}}{\pi}$$

$$b = \frac{1}{2mE}$$

$$a = \frac{k}{2E}$$

This should reduce to the usual result if $E = \frac{\hbar}{2} \sqrt{\frac{k}{m}}$.

A10. Time-averaged decoherence time

The time-averaged decoherence time is printed out automatically for all decay-of-mixing methods. It is defined by

$$\frac{1}{\tau} = \frac{\sum_j \Delta t_j \sum_{i \neq K} \frac{\rho_{ii,j}}{\tau_{iK,j}}}{\sum_j \Delta t_j \rho_{KK,j} > 0.98},$$

where Δt_j is time of integration step j . Notice that this using the working hypothesis that when $\rho_{KK,j} > 0.98$, the decay of mixing is essentially finished, so we don't count the decoherence time in the time average in either the numerator or the denominator. Thus the time average of the decoherence time only counts the strong-interaction region.

When the COUPLINGDECAY option is invoked, $\rho_{KK,j}$ will typically be larger than 0.98 in the regions where the coupling is zeroed, i.e., the decay of mixing will be finished, and the trajectory will be basically be propagating on a single surface. So these regions are not counted because of the $\rho_{KK,j} > 0.98$ condition.